



Size- and position-dependent cytoplasm viscoelasticity through hydrodynamic interactions with the cell surface

Javad Najafi^{a,b} , Serge Dmitrieff^{a,b}, and Nicolas Minc^{a,b,1}

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Many studies of cytoplasm rheology have focused on small components in the submicrometer scale. However, the cytoplasm also bathes large organelles like nuclei, microtubule asters, or spindles that often take significant portions of cells and move across the cytoplasm to regulate cell division or polarization. Here, we translated passive components of sizes ranging from few up to ~50 percents of the cell diameter, through the vast cytoplasm of live sea urchin eggs, with calibrated magnetic forces. Creep and relaxation responses indicate that for objects larger than the micron size, the cytoplasm behaves as a Jeffreys material, viscoelastic at short timescales, and fluidizing at longer times. However, as component size approached that of cells, cytoplasm viscoelastic resistance increased in a nonmonotonic manner. Flow analysis and simulations suggest that this size-dependent viscoelasticity emerges from hydrodynamic interactions between the moving object and the static cell surface. This effect also yields to position-dependent viscoelasticity with objects initially closer to the cell surface being harder to displace. These findings suggest that the cytoplasm hydrodynamically couples large organelles to the cell surface to restrain their motion, with important implications for cell shape sensing and cellular organization.

cytoplasm | hydrodynamics | cell mechanics | viscoelasticity | confinement

The cytoplasm is a complex heterogeneous medium crowded with macromolecules and entangled cytoskeleton networks (1). These define rheological properties that may influence molecular processes ranging from molecular diffusion to reaction kinetics and protein folding (2–5). However, the cytoplasm also hosts the motion of much larger elements closer to the cellular scale, for which the impact of cytoplasm properties remains much less understood. For instance, during critical events such as fertilization, cell polarization, or asymmetric divisions, cells actively displace large nuclei, microtubule asters, or mitotic spindles across their cytoplasm (6, 7). These organelles are moved by forces generated from active polar cytoskeletal networks such as actomyosin bundles or microtubule asters and associated motors, that need to overcome mechanical resistance from the cytoplasm medium (8). Therefore, addressing the nature and magnitude of frictional interactions of large components with the cytoplasm remains an important endeavor for cellular spatial organization.

Many past studies have measured rheological properties of bulk cytoplasm, using either extracts *in vitro*, or by actuating endogenous or foreign probes in living cells. These have shown that cytoplasm response will depend on timescale, force amplitude, or component size (9–14). The question of object size has notably raised important notions for cytoplasm mechanics, as for components smaller or larger than a typical mesh size, the cytoplasm may exhibit different rheological signatures transiting from fluid, to viscoelastic, poroelastic, or even glassy materials (15–20). However, these studies were restricted to regimes of relatively small objects typically below the micron size, as well as low force and displacement amplitudes. As objects reach closer to the cell size and move across longer distances, they are predicted to drag and shear large portions of the cytoplasm fluid (21–23). In such a regime, cytoplasm resistance may be influenced by boundary conditions at the static cell surface, through so-called wall effects. These effects have been well documented in fluid mechanics, and rely on hydrodynamic interactions that couple a moving object with a static wall. They can enhance frictional coefficients by a significant amount if the object contained by the walls approaches the size of the container (24). They were taken into consideration in few recent studies addressing force-balances moving nuclei, asters, or mitotic spindle organelles, to correct drag coefficients (21–23, 25, 26). Yet, evidence that these effects are relevant to living cells is still lacking, in part given the technical difficulty of applying calibrated forces onto large components *in vivo*, and of properly discerning contributions of active cytoskeleton forces from more passive resistive elements in the cytoplasm.

Significance

Large-sized organelles like nuclei or mitotic spindles typically translocate through the cytoplasm to regulate cell division or polarity, but their frictional interactions with the cytoplasm and the cell surface remain poorly addressed. We used *in vivo* magnetic tweezers, to move passive components in a range of sizes in the cytoplasm of living cells. We found that the mobility of objects with sizes approaching that of cells, can be largely reduced as a result of hydrodynamic interactions that couple objects and the cell surface through the cytoplasm fluid.

Author affiliations: ^aUniversité de Paris, CNRS, Institut Jacques Monod, 75006 Paris, France; and ^bEquipe Labellisée Ligue Contre le Cancer, 75013 Paris, France

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¹To whom correspondence may be addressed. Email: nicolas.minc@ijm.fr.

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Here, we employed calibrated *in vivo* magnetic tweezers to move passive components of sizes ranging from ~ 1 to $\sim 50\%$ of the cell diameter across the cytoplasm of living cells. By tracking resultant cytoplasm shear flows and using finite element hydrodynamic simulations, we demonstrate how object size disproportionately restrains its mobility as a result of hydrodynamic interactions with the cell surface. We also find that these interactions can yield to position-dependent cytoplasm resistance with objects initially closer to the cell surface becoming harder to pull or push. This work suggests that large organelles may be coupled to the cell surface with no requirement for any direct cytoskeletal connections, and highlights the underappreciated impact of confinement by cell boundaries to organelle motion.

Results

Probing Bulk Cytoplasm Rheology at Multiple Length Scales. We sought to probe the rheology of bulk cytoplasm in response to the typical translational motion of relatively large organelles, such as, e.g., micrometric acidic organelles or even larger nuclei or mitotic spindles. These objects are commonly moved by molecular motors with directional speeds ranging from fractions up to tens of $\mu\text{m/s}$, across distances in the scale of few to few tens of microns (27). We used sea urchin unfertilized eggs as model cell types. These are large cells, with a diameter of ~ 95 to $100\ \mu\text{m}$, amenable to quantitative injection, that are arrested in a G0- or G1-like state of the cell cycle before fertilization (28). Importantly, in contrast to fertilized eggs, unfertilized eggs do not feature any large-scale cytoskeletal organization, with F-actin and microtubule filaments distributed throughout the cytoplasm, and no detectable thick actin cortex (*SI Appendix, Fig. S1 A and B*) (29). In addition, particle imaging velocimetry (PIV) of relatively large granules did not reveal any persistent cytoplasm flows, suggesting that the cytoplasm material may be considered at rest in these cells (*SI Appendix, Fig. S1 C*).

To compute the viscoelastic response of the cytoplasm at different length scales, we injected single magnetic beads of $1\ \mu\text{m}$ in diameter, as well as hydrophilic beads that form compact aggregates of variant diameters from few up to $10\ \mu\text{m}$ when injected in the cytoplasm (26, 30). To reach component sizes closer to cell size, we injected a suspension of soya oil mixed with hydrophobic $\sim 1.2\text{-}\mu\text{m}$ magnetic beads inside eggs. Upon injection, this suspension formed large magnetized oil droplets that ranged in size from 18 to $45\ \mu\text{m}$ (corresponding to ~ 20 to 48% of the cell diameter) (21). Inside oil droplets, hydrophobic beads also formed compact aggregates, with sizes that were not necessarily correlated with oil droplet size. In typical experiments, we applied forces to these probes by approaching a magnet tip close to the cell surface. This caused components to translate through the cytoplasm along the magnetic gradient (Fig. 1A). Magnetic forces depended on bead type (hydrophilic vs hydrophobic), magnet tip-beads distance and aggregate size, and were calibrated *in vitro* using test viscous fluids (*SI Appendix, Fig. S2 A–C*). Using these calibrations, in each cell, and during each pull, we computed the magnetic force by measuring both the size of aggregates (in the cytoplasm or in the oil droplet) and the distance between the magnet tip and the magnetic probe (26, 31). Finally, given the variations in the number of injected beads, their initial position, and their motion during pulls, that all modulate the magnetic force, we systematically rescaled object displacement by force to plot and quantify creep responses (21, 31).

Interestingly, all these objects exhibited similar creep responses to an applied force. First, objects moved at constant speed, indicating a viscous behavior. Then the displacement-time curve inflected reflecting elastic responses. At longer timescales the

behavior was linear again indicating a fluidization of elastic elements (21, 30, 32) (Fig. 1B). Accordingly, when the force was released, objects recoiled back toward their initial positions with partial recoils that reflected a dissipation of stored elastic energy. However, during recoils, small beads were more prone to random forces and space exploration, exhibiting a much less directional recoiling behavior (Fig. 1C and *Movie S1*).

To quantify cytoplasm viscoelastic parameters, we fitted both creep and recovery curves with a 1D Jeffreys model, consisting of a Kelvin–Voigt viscoelastic element in series with a dashpot, which represents the dissipation of the material in the long asymptotic time (30, 33) (Fig. 1B, *Inset*). Other linear 2-elements Kelvin–Voigt or Maxwell or 3-elements solid Zener viscoelastic models (34) were also assayed but failed to account for the generic experimental shape of creep and relaxation responses (*SI Appendix, Fig. S3 A–C*). Using Jeffreys model, we computed a short-term viscous drag of the translating object, γ_1 , a restoring stiffness k , and thus the viscoelastic relaxation timescale of the cytoplasm material $\tau_1 = \gamma_1/k$. Mean values of viscous drags increased with object size, from $11 \pm 6\ \text{pN}\cdot\text{s}/\mu\text{m}$ (mean \pm SD) for small $1\text{-}\mu\text{m}$ beads, to $67 \pm 49\ \text{pN}\cdot\text{s}/\mu\text{m}$ for larger aggregates and up to $660 \pm 312\ \text{pN}\cdot\text{s}/\mu\text{m}$ for very large oil droplets. Similarly, the restoring stiffness increased from $4 \pm 3\ \text{pN}/\mu\text{m}$, to $54 \pm 57\ \text{pN}/\mu\text{m}$ and $191 \pm 112\ \text{pN}/\mu\text{m}$, respectively (Fig. 1D and E). Importantly, however, the relaxation timescales was mostly independent of object size, and was around $\sim 4\ \text{s}$ during force loading and $\sim 7\ \text{s}$ during relaxation (Fig. 1F and G). These results suggest similar general rheological responses of the cytoplasm to translating objects ranging in size from few up to 50% of cell size.

Cytoplasm Crowding and Bulk F-Actin Networks Contribute to Cytoplasm Viscoelasticity at the Scale of Large Objects. To assay if viscoelastic responses and parameters reflected bulk cytoplasm properties, we next injected magnetic droplets and rinsed eggs in diluted (50%) or concentrated (120%) artificial sea water (ASW) to vary extracellular osmolarity and, respectfully decrease or increase macromolecular crowding (3, 35–37) (Fig. 2A and B and *Movie S2*). By measuring the osmolarity of these different ASWs, we estimated a corresponding hypoosmotic pressure drop of $-1.02\ \text{MPa}$ for 50% ASW and hyperosmotic pressure drop $+0.52\ \text{MPa}$ for 120% ASW. In response to hypoosmotic treatments, both eggs and their female nuclei, expanded in size, and conversely decreased in size in hyperosmotic conditions (*SI Appendix, Fig. S4A*) (38, 39). These observations support that cytoplasm crowding is modulated as compared with controls, in these osmotic treatments.

Upon treatment, both creep and relaxation responses had similar shapes as in controls, but viscous drag and restoring stiffness values were markedly different (Fig. 2C). In hypoosmotic conditions, they were reduced by $\sim 4.2\times$ and $\sim 3.8\times$, respectively, and increased by $\sim 1.6\times$ and $\sim 2.8\times$ in hyperosmotic conditions. Accordingly, characteristic viscoelastic timescales during the pulling phase were similar in control and hypoosmotic conditions ($4.1 \pm 2.8\ \text{s}$ and $3.9 \pm 2.4\ \text{s}$), but slightly reduced to $2.2 \pm 1.5\ \text{s}$ in hyperosmotic conditions. Therefore, the frictional interaction between cytoplasm elements and large translating objects appears to depend on the degree of macromolecular crowding and solvent availability.

As an alternative mean to modulate cytoplasm mechanics, we also affected cytoskeleton elements. As shown in *SI Appendix, Fig. S1A*, unfertilized eggs feature a relatively dense meshwork of bulk F-actin filaments that span the cytoplasm, and microtubules that are more sparsely distributed. When F-actin was depolymerized with Latrunculin B, the viscous drag and restoring stiffness

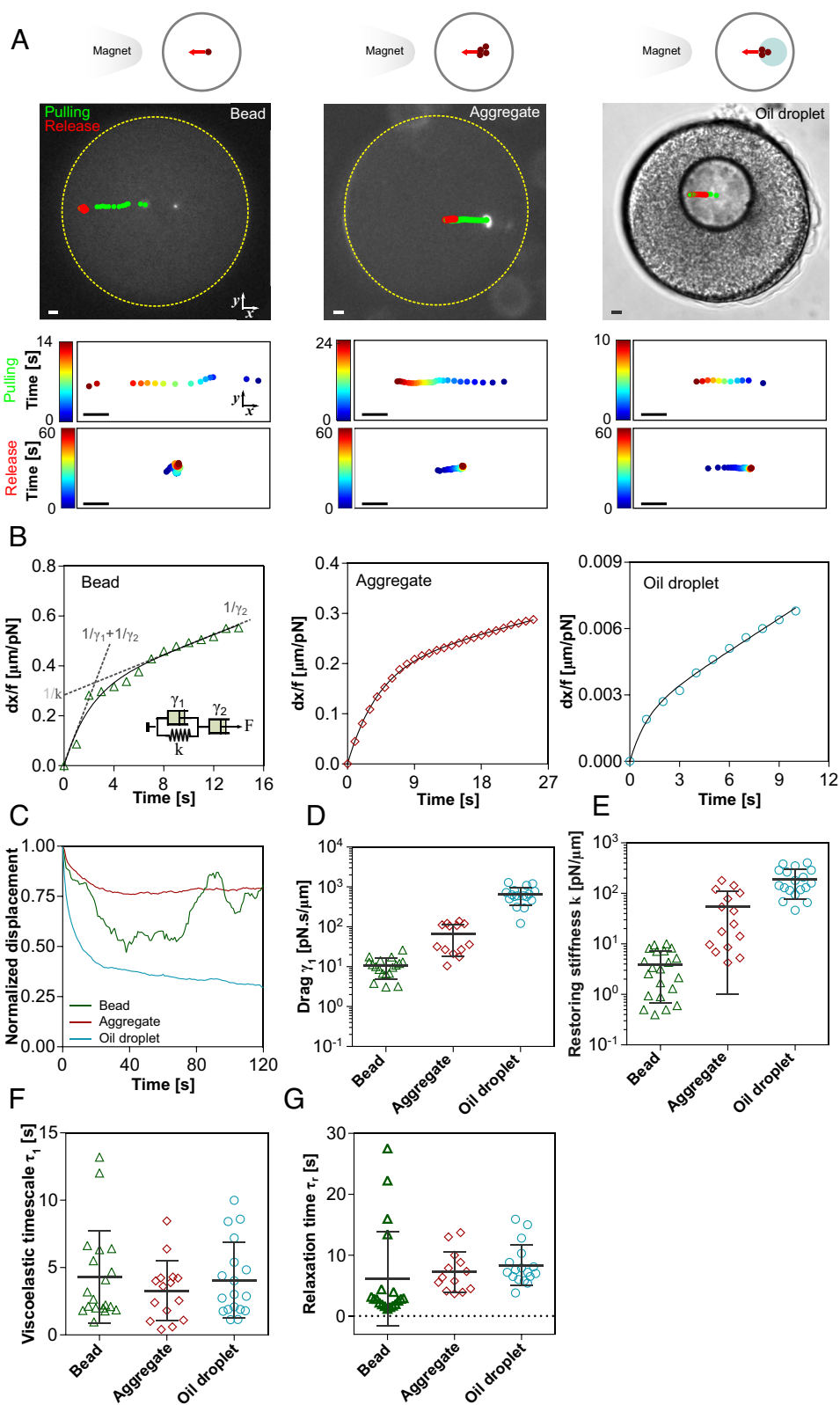


Fig. 1. Probing cytoplasm rheology at large length-scales. (A) Sea urchin unfertilized eggs injected with single 1-μm diameter beads, beads aggregate with diameters ranging from ~4 to 12 μm and large oil droplets containing hydrophobic beads. Calibrated magnetic forces were applied to translate these magnetized objects in the cytoplasm. The trajectories of the objects tracked at 1 Hz during force application (green) and force release (red) are overlaid on the cells, and also represented in time color coded graphs at the bottom of cells. (B) Representative displacement curves scaled by forces plotted as a function of time for beads, aggregates and magnetized oil droplets. Jeffreys viscoelastic model is depicted as an *Inset* in the graph for single beads, with representative constants overlaid on the curve. Solid lines are fits of Jeffreys model. (C) Normalized recoiling displacements plotted as a function of time for the same objects as in B. Note that the recoil of small beads toward their initial position is nondirectional due to intrinsic cytoplasm noise. (D–G) Cytoplasm viscoelastic parameters for objects of variant sizes computed by fitting creep and relaxation curves with Jeffreys model ($n = 21, 15$ and 18 , respectively): viscous drags (D), restoring stiffness (E), viscoelastic timescale during the rising phase (F) and in the releasing phase (G). Error bars correspond to \pm SD. (Scale bars, 5 μm.)

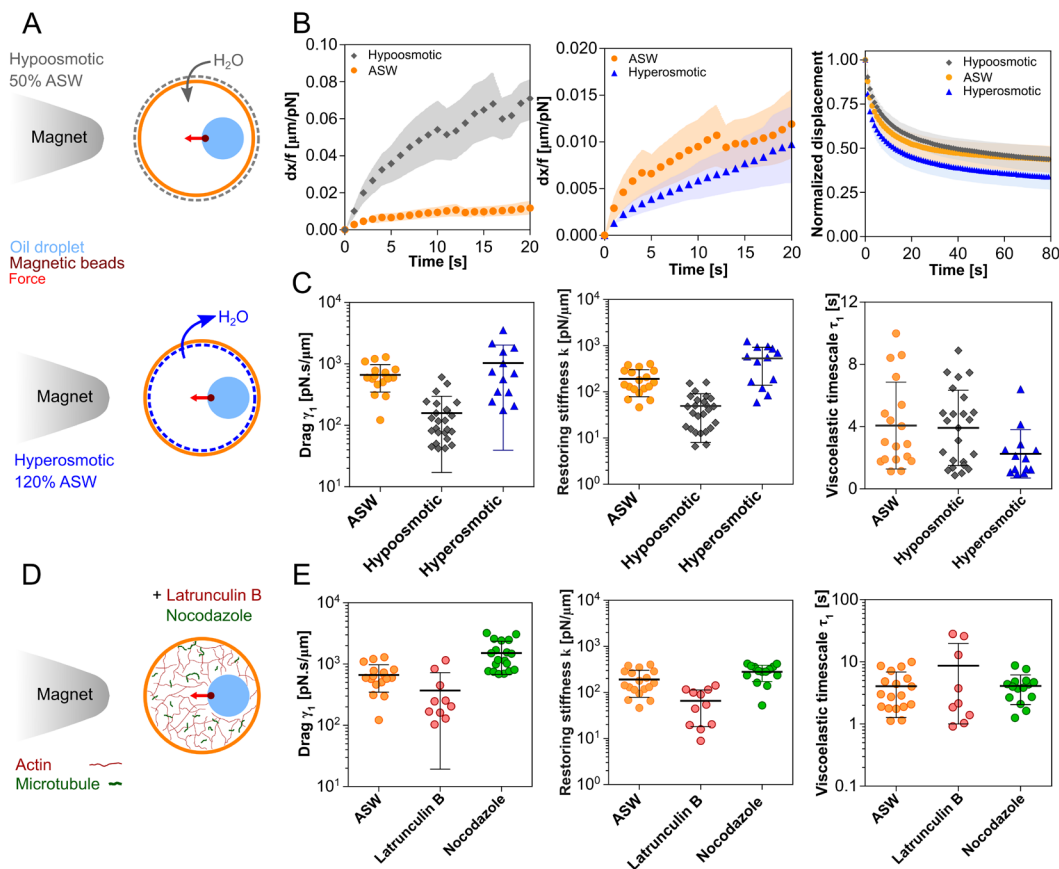


Fig. 2. Viscoelastic properties depend on cytoplasm crowding and bulk cytoskeleton networks. (A) Schematic of experiments in which cytoplasm crowding is modified by placing cells in hypoosmotic or hyperosmotic ASW. (B) Displacement curves scaled by forces during pulling phases, and normalized relaxation curves after force retraction for control ($n = 18$), hypoosmotic ($n = 26$), and hyperosmotic ($n = 13$) conditions for oil droplets. (C) Viscous drag, restoring stiffness, and viscoelastic timescale in the rising phase at different osmotic conditions. (D) Schematic of experiments in which F-actin or microtubule were depolymerized using Latrunculin B or Nocodazole, respectively. (E) Viscoelastic drag, restoring stiffness, and viscoelastic timescale in the rising phase for controls ($n = 18$) and for eggs treated with Latrunculin B ($n = 11$) and Nocodazole ($n = 19$). Shaded areas represent \pm SEM and error bars correspond to \pm SD.

of oil droplets were reduced by $\sim 1.8\times$ and $\sim 2.9\times$, respectively. In contrast, these values were increased by $\sim 2.3\times$ and $\sim 1.5\times$ when microtubules were depolymerized with Nocodazole (Fig. 2 D and E). These results suggest that bulk F-actin networks constitute one important resistive mechanical element for the cytoplasm, while microtubules may rather fluidize or soften the cytoplasm, as proposed in other contexts (11, 21, 40).

Cytoplasm Viscoelastic Shear Flows Associated with the Motion of Large Objects. To understand how the motion of different-sized objects impacts cytoplasm organization, we mapped cytoplasm flows upon force application on different components, by tracking granules visible in bright field with PIV. This analysis yields a 2D projection of experimental flows in the plane of force application (Fig. 3 A and B). The movement of small beads did not create notable large-scale flows, reflecting the high viscosity of the cytoplasm that screens perturbations at long length-scales (SI Appendix, Fig. S4B). In contrast, the motion of very large droplets, yielded notable and reproducible cytoplasm flow fields. The maximum cytoplasm flow speed was on the order of droplet speed at the front and back of the droplet along the pulling direction and dropped rapidly away from the droplet (Fig. 3 B and G). Moreover, two vortices were generated at the upper and lower parts of the pulling axis, often asymmetric in size when the droplet and force axis were, for instance, off-center (Fig. 3 B–D and Movie S3). This suggests that large translating objects

create significant shear in the cytoplasm with magnitudes and organization that may depend on object size and its distance to cell boundaries.

To test if experimental flows and viscoelastic responses could correspond to a simple interaction of the moving object with the surrounding cytoplasm fluid, we set up 3D finite-element hydrodynamic simulations. We represented the oil droplet as a solid spherical object and displaced it with a constant force inside a confined Jeffreys viscoelastic medium (implemented as an Oldroyd-B model) and then released the force. As inputs of this model, we used the two viscosities and the second viscoelastic timescale measured from experiments. The resulting simulations accounted for both flow fields organization and speed magnitude at various steps of the pulling and relaxation phases observed in experiments (Fig. 3 C–G and Movie S3). We validated the simulations by computing the consistency between input and output values of material properties, which we measured from the simulated time-displacement curves following a 1D Jeffreys model, as in experiments. We found that the quantitative creep and recovery curves of the experiments were consistent with the simulation output, asserting that the 1D Jeffreys model was sufficient to describe the 3D viscoelastic response of the cytoplasm (SI Appendix, Figs. S5 A–E and S6 B and C). Finally, visualizing 3D simulated flow streamlines along planes orthogonal to the pulling direction showed that flows exhibit a rotational symmetry with

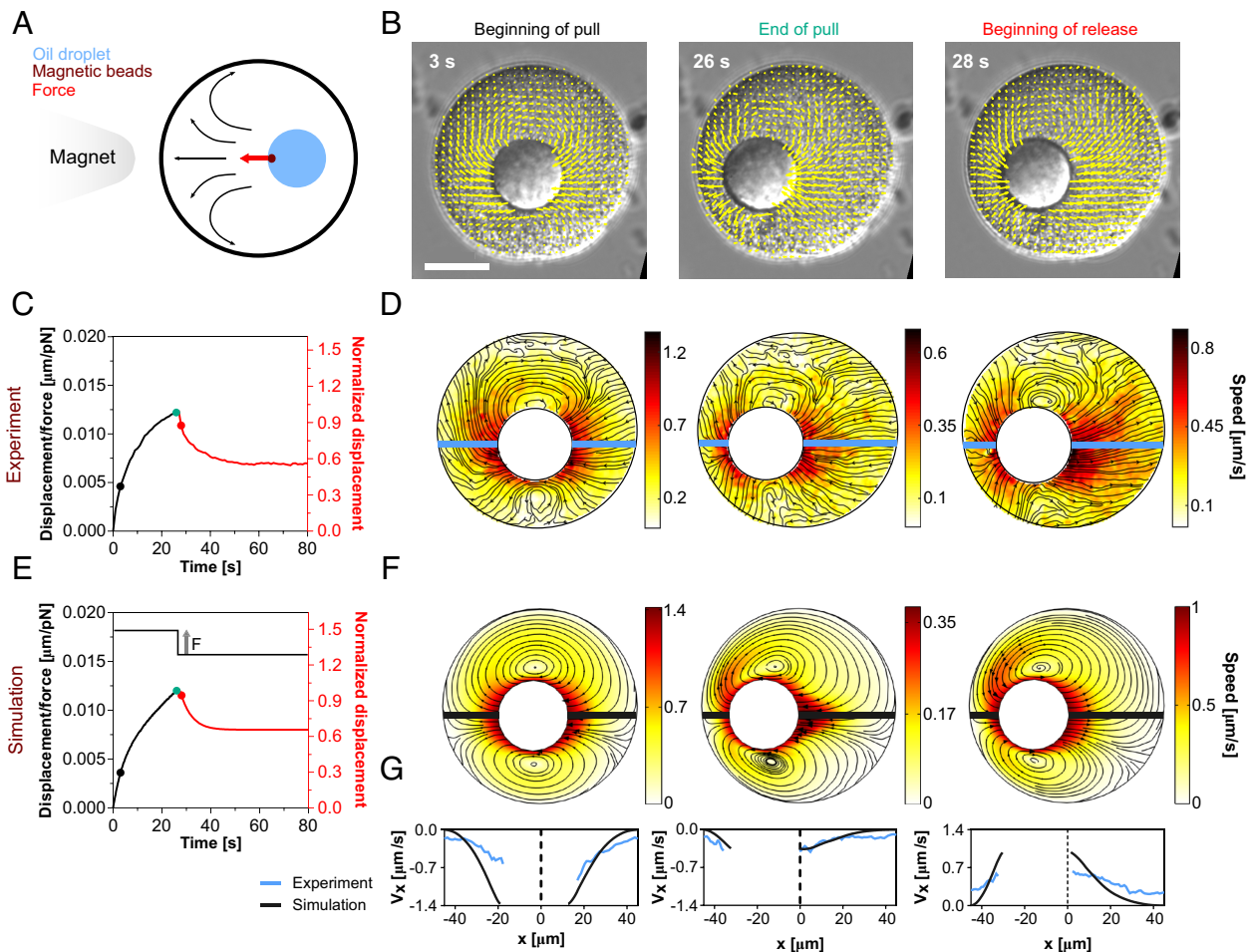


Fig. 3. Experimental and theoretical mapping of cytoplasmic flows created by the translation of large objects inside cells. (A) Schematic of a moving oil droplet and consequent viscoelastic flows. (B) Vector fields of cytoplasmic flows obtained by PIV around a moving oil droplet at the beginning of the pulling phase, end of pulling, and beginning of the release phase overlaid on DIC images. (C) Scaled displacement curve of the pulling phase and normalized curve of the release phase for the same experiment as in B. Time points of temporal snapshots of the vector fields are indicated by color-coded circular markers on the curves. (D) Experimental streamlines and speed heat maps of cytoplasmic flow for the same snapshots as in B. (E) Scaled displacement curve of the pulling phase and normalized release phase obtained from 3D finite-element simulations with input parameters taken from experimental measurements. (F) Numerical streamlines and speed heat maps of the same time points as in D in the mid-plane parallel to the pulling direction. Arrowheads in the simulations are proportional to the speed. (G) Profile of the cytoplasm velocity along the force x-axis for the experiment and simulation averaged along stripes passing through the oil droplet center as indicated in the flow maps in D and F. (Scale bar, 30 μm .)

respect to the force axis, justifying a direct comparison with 2D experimental streamlines (SI Appendix, Fig. S5F).

Viscoelastic Drag and Restoring Stiffness Depend on Confinement. Flow analysis suggested that the displacement of large objects generates shear flows from hydrodynamic interactions between the object and cell boundaries. We sought to test if these interactions could affect object mobility and notably enhance its drag and/or restoring stiffness. For a sphere located at the exact center of a compartment filled with a Newtonian fluid, the viscous drag of the object is predicted to follow a modified Stokes' law $\gamma_I(\lambda) = 6\pi\eta r C(\lambda)$ where η is the fluid viscosity, r , the object radius, and C a wall correction factor: $C(\lambda) = \frac{4(1-\lambda^5)}{4-9\lambda + 10\lambda^3 - 9\lambda^5 + 4\lambda^6}$ with $\lambda = r/R$ the ratio of the sphere radius to that of the container (24). Therefore, such correction amounts to an increase in the effective viscosity felt by the object: $\eta^*(\lambda) = \eta C(\lambda)$. The correction factor asymptotically approaches 1 for a small and weakly bounded object, is ~ 2.5 for objects $\sim 30\%$ of container size, reaches up to ~ 7 when objects are $\sim 50\%$ of container size, and diverges to infinity when object size approaches that of the container (Fig. 4A). By running 3D simulations, we confirmed the validity of this formula in the

context of our particular pulling assay and also predicted that confinement should have a similar impact on both viscous and elastic responses of the cytoplasm.

To test the relevance of confinement to experimental results, we plotted measured viscous drags as a function of λ for the different-sized objects (Fig. 4A). Individual values for each typical object size exhibited a large variability, which we primarily attributed to cell to cell heterogeneities, and to plausible residual motions of probes along the Z-axis that may affect viscoelastic parameter estimations. In spite of this noise, average experimental drags were in correct agreement with the results of both analytical formula and 3D hydrodynamic simulations in the large intervals of confinement ratio. Importantly, for large oil droplets, the deviation from linear Stokes' relationship became pronounced as the confinement ratio λ exceeded -0.1 to 0.2 , with correction factors that ranged from ~ 1 to ~ 9 . In addition, as predicted by simulations, we found that the effect was similar for restoring stiffness, directly demonstrating that the proximity of boundaries can enhance both viscous and elastic cytoplasm resistance (Fig. 4A).

To better establish the relevance of this effect in dose-dependence, we next performed 3D simulations in the size range of spherical oil

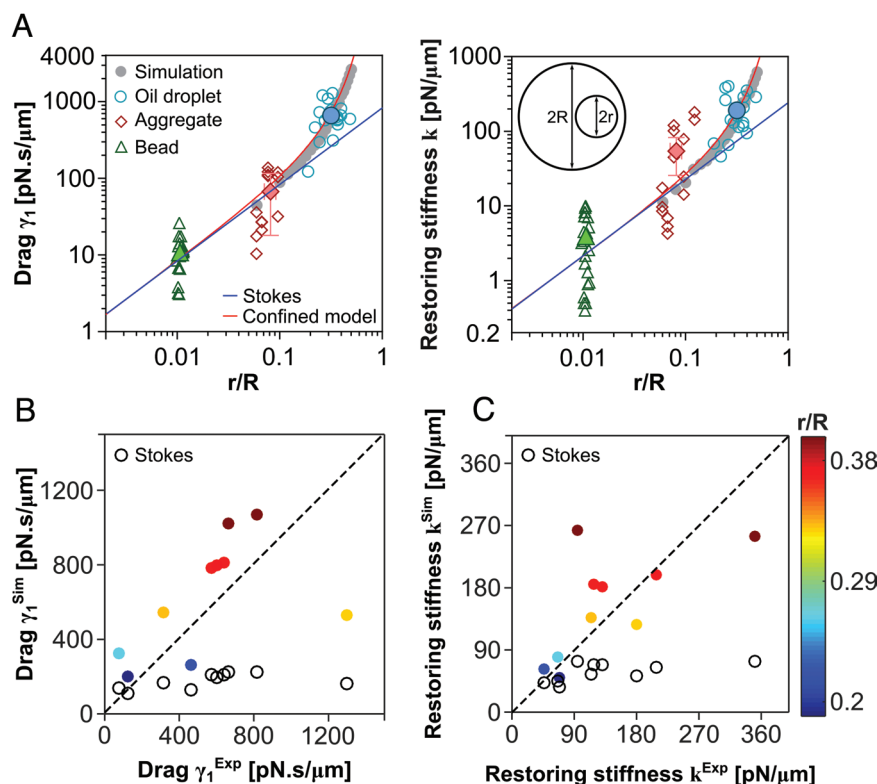


Fig. 4. Cell confinement enhances cytoplasm viscoelastic resistance in a nonlinear manner. (A) Viscous drag and restoring stiffness increase with the object size in a nonlinear manner, and deviate from linear Stokes' law for confinement ratios larger than ~ 0.1 . The red curve represents the analytical prediction for a confined Newtonian fluid, the blue line is the Stokes' law with no confinement, gray solid circles are 3D simulations, and solid colored symbols are average values for beads ($n = 21$), aggregates ($n = 15$), and oil droplets ($n = 18$). Deviations from experimental data to the linear Stokes' model are significantly larger ($R^2 = -1.86$ and $RAE = 1.018$) than deviations to the nonlinear model including the confinement correction ($R^2 = 0.37$ and $RAE = 0.53$). (B and C) Individual viscous drags (B) and restoring stiffness (C) computed from experiments and simulations for individual droplets of various sizes in the cytoplasm. Hollow circles indicate the linear Stokes' model predictions for the oil droplets of various sizes in the experiments. Dashed lines in B and C guide the eyes for a perfect match between experiment and models.

droplets, and compared predicted drags and restoring stiffness with individual experimental results. For this, we inputted average experimental values of cytoplasm viscosities and second viscoelastic timescale, and varied droplet and egg size and initial position (see below) according to experiments. The agreement between experiments and simulations was in general very good, suggesting that experiments are close to the theoretical limit. In comparison, the agreement between measured drags and restoring stiffness to those predicted by a linear Stokes model was generally poor (Fig. 4 B and C). Together, these results strongly suggest that hydrodynamic interactions between a large moving object and the cell surface, effectively enhance cytoplasm viscoelasticity at this scale.

Slippage on Boundaries Reduces the Effect of Confinement on Organelle Mobility. Organelles and cell surfaces may come with different properties like rugosity or hydrophobicity that may influence how the cytoplasm fluid interacts with these surfaces. In addition, our assays build in part on comparisons between large oil droplets and smaller bead aggregates, which not only differ in size but also in surface properties. We thus sought to evaluate the impact of stick or slip conditions on the confinement effects. In experiments, it was technically challenging to modulate slippage. Therefore, we performed a series of simulations to test how boundary conditions impact flow fields and size dependency. We considered three different scenarios: a no-slip boundary condition over the oil droplet and cortex surface, slippage only over the oil surface, and finally slippage over both oil and cortex surfaces. Interestingly, the general flow patterns were independent of boundary conditions chosen (Fig. 5 A–C). However, the impact

of dissipation for a sphere of a given size was reduced when the fluid slips on surfaces, yielding to a net increase in average fluid speed (Fig. 5 D). Under the same applied force, the fluid speed drops as object size increases, but boundary conditions affect the speed in the same manner for spheres of different sizes (Fig. 5 D). Accordingly, both viscous drag and restoring stiffness increased in a nonlinear manner as a function of the confinement ratio λ under all boundary conditions, but the effect was more pronounced when the fluid could adhere to all surfaces (Fig. 5 E and F). We conclude that the impact of confinement on large organelle mobility may still be significant independently of the type of boundary conditions, but more pronounced for nonslip conditions.

Heterogeneity and Anisotropy of Drags and Restoring Stiffness.

As organelles may adopt different locations within the cytoplasm, being e.g., initially closer to the cell surface, we sought to test if hydrodynamic interactions affect mechanical resistance of the cytoplasm depending on object's initial position. We first performed a range of simulations. We considered a sphere with a confinement ratio of $\lambda = 0.2$ in a cell filled with Jeffreys fluid, and placed it at different positions along the force axis. We found that both drags and restoring stiffness increased as the object was closer to the cell surface, reaching an enhancement of $\sim 2.5\times$ at an offset distance of $\sim 30\%$ of cell size closer to the surface. Simulating a much smaller sphere of $\lambda = 0.04$ as control, showed that this local effect is only relevant to relatively large objects (Fig. 6 A and B). Interestingly, because of the linearity of the viscoelastic-model used, this position-dependent

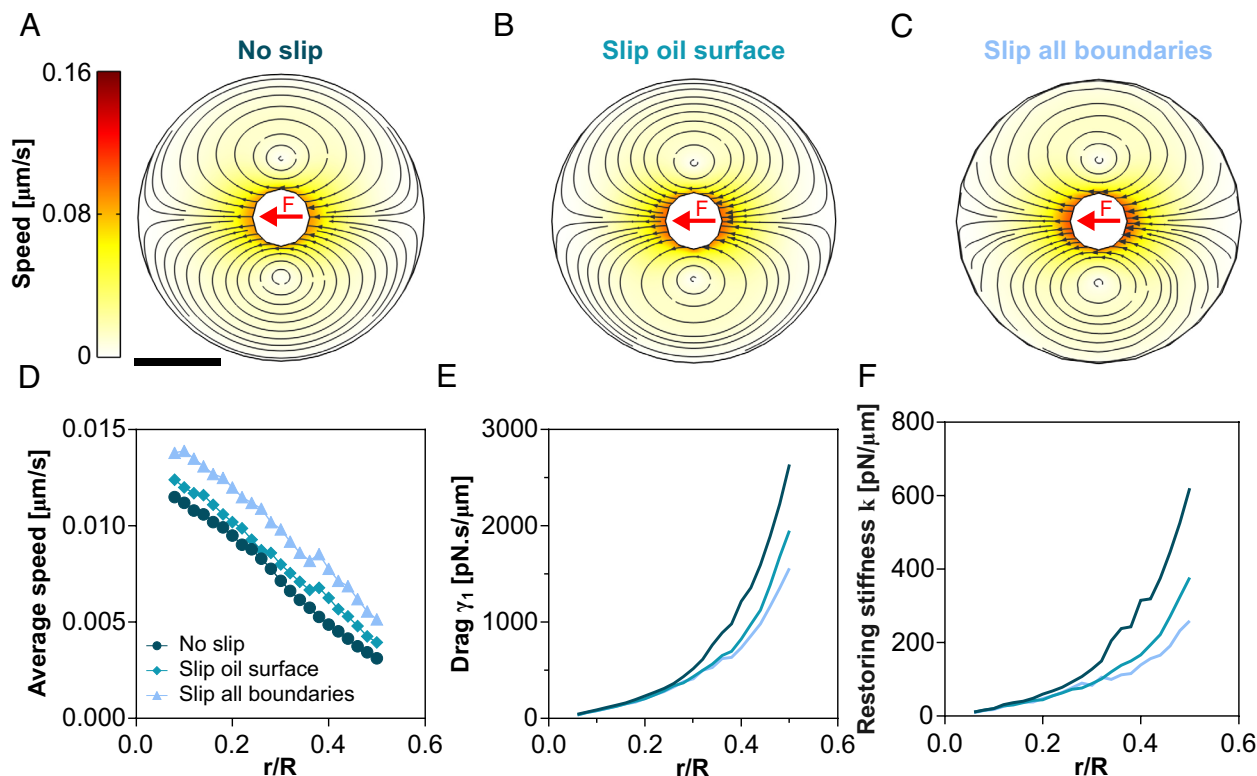


Fig. 5. Impact of slip or stick boundary conditions for the influence of cell confinement on large object mobility. (A–C) Simulated streamlines and flow patterns of the cytoplasm for various boundary conditions on the oil droplet and cell surfaces. (D) Slippage over the boundaries increases the flow speed for all confinement ratios. The magnitude and direction of the pulling force are set to be the same for all spheres of different sizes. (E and F) Viscous drag and restoring stiffness grow in a nonlinear manner for all types of boundary conditions, but the values of viscoelastic parameters are smaller when the fluid can slip over surfaces. Arrowheads in the simulations are proportional to the speed. (Scale bar, 30 μm .)

enhancement was perfectly symmetric, whether the object was pushed against or pulled away from the surface. Accordingly, analysis of fluid flows revealed symmetric flow maps with respect to the boundary, indicating a similar interaction of the fluid with the container surface in both cases (Fig. 6C). Finally, these symmetric enhanced effects were also observed for restoring stiffnesses (Fig. 6D). In the second sets of simulations, we changed object initial position along an axis orthogonal to the force axis. In this situation, boundary conditions also enhanced cytoplasm resistance, but the effect was less pronounced than when objects moved toward or away from the cell surface (Fig. 6A). Therefore, hydrodynamic interactions with cell boundaries may yield to anisotropic cytoplasm resistance facilitating the motion of large objects parallel as compared with orthogonal to the cell surface.

To test these predictions in real cells, we pulled oil droplets with different initial positions. To minimize variability arising from different droplets sizes or different cells, we performed successive pulls of the same droplets, spaced by sufficient time for the material to relax, and varied their initial position with magnetic tweezers. The average experimental values for drags and restoring stiffness exhibited a minimum at the cell center, and increased symmetrically as the droplet was placed closer to the cell surface, with a good alignment on simulations data (Fig. 6D). Interestingly, the position-dependent enhancement, for both drag and restoring stiffness was symmetric, as predicted from the linear model, suggesting that both cytoplasm compression and extension can result in viscous and elastic stresses. Together, these simulations and experiments demonstrate that cytoplasm viscoelasticity felt by relatively large objects in a cell may be position-dependent and anisotropic.

Discussion

Here, we used magnetic tweezers to displace large passive components of different sizes in the cytoplasm of living cells with unidirectional calibrated forces. Our results suggest that objects floating in bulk cytoplasm can be coupled to the cell surface through the fluid, with no need for any direct cytoskeletal connections. This hydrodynamic coupling can occur over distances of up to tens of microns and enhance the viscoelastic resistance of the cytoplasm, thereby reducing organelle mobility. The strength of the coupling increases as the distance between the object and the surface reduces, so that larger components or components closer to the cell surface, become disproportionately harder to displace. Size and position dependency had previously been reported for the diffusion of smaller components in different cells. They were attributed to effects including a hierarchy of cytoplasm pore sizes (41), glass-like transitions of bulk material (16), or to heterogeneities across cells (17). Our data for large objects, support a different physical origin, in which both size and position dependency can emerge solely from hydrodynamic interactions with the surface. As such, previously proposed alterations in bulk material properties or gradients in these properties, although not required here, could add up to the impact of hydrodynamic interactions in different cell types.

Our data suggest that the impact of hydrodynamic coupling becomes pronounced for objects over ~ 20 to 30% of cell size, which is the typical size ratio for organelles such as nuclei, mitotic spindles or microtubule asters. Accordingly, in vivo force measurements reported spindle and aster drags that largely exceeded Stokes drags calculated from the size of these organelles and cytoplasm viscosity (21, 25, 26). However, the active force generating nature of cytoskeletal structures coupled

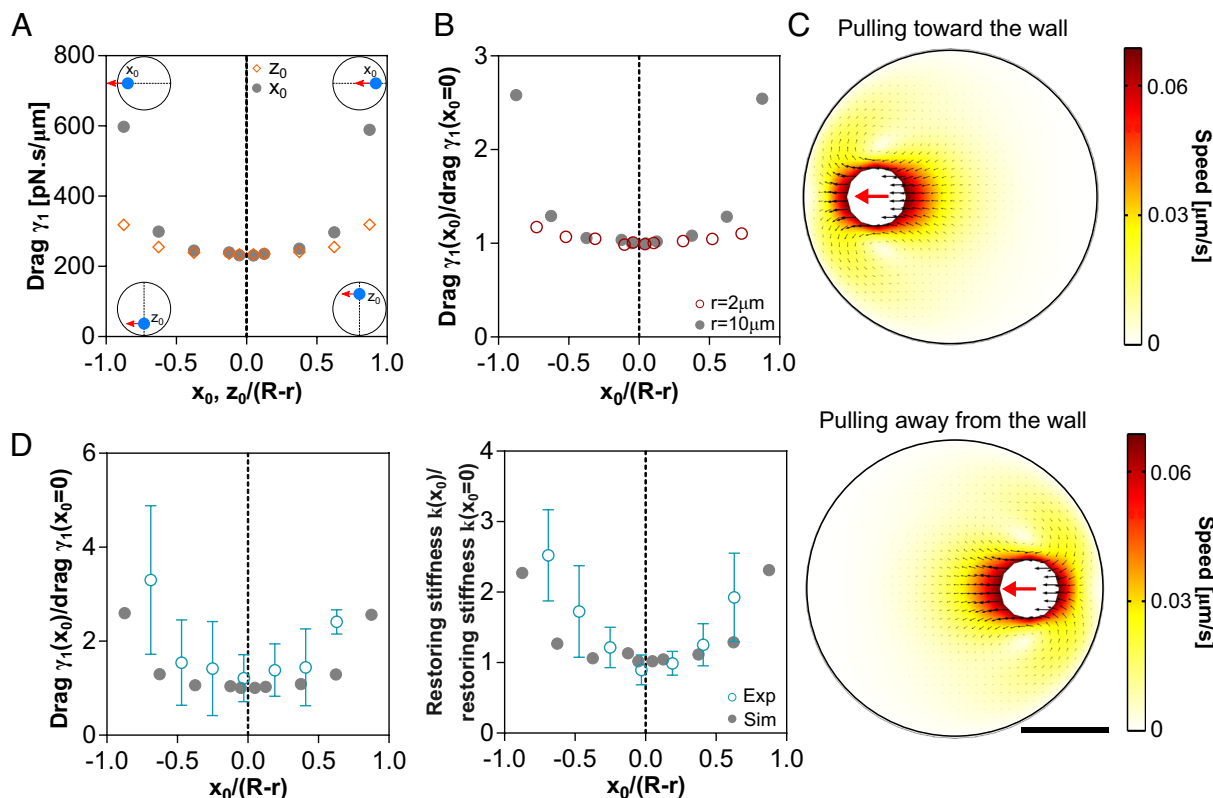


Fig. 6. Cytoplasm viscoelastic properties are heterogeneous and anisotropic depending on object position. (A) Simulation of viscous drags experienced along the pulling force axis (x -axis) for objects positioned with offsets along the force axis or orthogonal to this axis (Z -axis). (B) Simulations of viscous drags experienced by objects of bigger or smaller sizes. (C) Simulation of fluid hydrodynamics interaction with the cell surface as the sphere is pulled toward or away from the surface. (D) Measured viscous drags and restoring stiffness for oil droplets pulled along the x -axis starting from different initial positions ($n = 47$ pulls, from four cells). The values of viscoelastic parameters have been renormalized to the values in the cell center, and experimental results are binned and overlaid with simulation results. Error bars correspond to the SD of data. (Scale bar, $30\ \mu\text{m}$.)

to these organelles precluded from univocally associating these enhanced drags to cytoplasm properties and size occupancy in the cell. Therefore, the advent of the passive oil droplet model we introduce here, is to directly establish the role of cytoplasm mechanics and boundaries set by the cell surface to the mobility of large components within cells. Other relevant parameters that could impact cytoplasm resistance include organelle shapes and porosity especially when considering fibrous-like structures such as asters and spindles (22, 42). Furthermore, as demonstrated here, the relative proximity of organelles to boundaries, may also greatly impact their mobility. As a consequence, we expect cell shape to also influence organelle mobility. For instance, a nucleus moving in a tube-like cell such as fission yeast or a columnar epithelial cell (43, 44), is predicted to face very large resistance from the cytoplasm, given the little space left for the fluid to move around the moving organelle (24). Although the role of the cytoplasm has been generally omitted in standard models of organelle positioning (7, 45), we anticipate they could impact our current appreciation of the mechanics of nuclear or spindle positioning, as well as that of shape changes.

Finally, our study also highlights large shear flows that form as a direct result of object motion under force, and cause the cytoplasm to recirculate over the scale of the whole cell (21). Cytoplasm flows can organize processes ranging from cortical polarity (14), and RNA localization (46), to nuclear positioning and internal organization (47, 48). They may emerge from cortical contractile acto-myosin flows that generate surface stresses that propagate through the cytoplasm (18, 19, 48, 49), or from the activity of

the cytoskeleton and associated motors directly in bulk (50, 51). Based on our observations, we propose that the natural motion or rotation of large organelles during e.g., asymmetric division or nuclear translocation could therefore create shear cytoplasm flows that may impact the polarization of both cytoplasmic and cortical elements. Accordingly, recent assays suggest that both intracellular and extracellular shear flows can cause the rotation of cell membranes and cortical polarity proteins (14, 52). Further work on how cytoplasm and cortical material properties and forces are integrated to control organelle mobility, will enlarge our understanding of cellular organization.

Material and Methods

Sea Urchin Gametes. Purple sea urchins (*Paracentrotus lividus*) were obtained from Roscoff Marine station (France) and maintained at 16°C in aquariums of ASW (Reef Crystals, Instant Ocean). Gametes were collected by intracoelomic injection of $0.5\ \text{M}$ KCl. Eggs were rinsed twice with ASW, kept at 16°C , and used on the day of collection.

Injection. Unfertilized eggs were placed on protamine-coated 50-mm glass-bottom dishes (MatTek Corporation) after removing the jelly coat through a $80\text{-}\mu\text{m}$ Nitex mesh (Genesee Scientific). The bead suspensions were injected using a micro-injection system (FemtoJet 4; Eppendorf) and a micro-manipulator (Injectman 4; Eppendorf). Injection pipettes were prepared from silicized (Sigmacote) borosilicate glass capillaries ($1\ \text{mm}$ diameter). Glass capillaries were pulled using a needle puller (P-1000; Sutter Instrument) and ground with a 40° angle on a diamond grinder (EG-40; Narishige) to obtain a $10\text{-}\mu\text{m}$ aperture. Injection pipettes were back-loaded with $\sim 2\ \mu\text{L}$ bead suspension before each experiment, and were not reused.

Immunostaining. Immunostaining was performed using procedures described previously (53). Samples were fixed for 70 min in 100 mM Hepes, pH 6.9, 50 mM EGTA, 10 mM MgSO₄, 2% formaldehyde, 0.2% glutaraldehyde, 0.2% Triton X-100, and 400 mM glucose. To reduce autofluorescence, eggs were then rinsed in Phosphate-Buffered Saline (PBS) and placed in 0.1% NaBH₄ in PBS freshly prepared, for 30 min. Eggs were rinsed with PBS and PBT (PBS + 0.1% TritonX) and blocked in PBT supplemented with 5% goat serum and 0.1% bovine serum albumin (BSA) for 30 min. Samples were rinsed with PBT before adding primary antibodies. For microtubule staining, cells were incubated for 48 h at 4 °C with a mouse anti- α -tubulin (DM1A; Sigma-Aldrich) primary antibody at 1:5,000 in PBT, rinsed 3 times in PBT and incubated for 4 h at room temperature with anti-mouse secondary antibody coupled to Dylight 488 (Thermo Fisher Scientific) at 1:1,000 in PBT for 4 to 5 h. To stain F-actin, samples were also incubated together with secondary antibodies in a solution of Rhodamine Phalloidin at 4 U/mL in PBT. Eggs were washed three times in PBT then twice in PBS, transferred in 50% glycerol in PBS, and finally transferred into a mounting medium (90% glycerol and 0.5% N-propyl gallate in PBS).

Hypoosmotic and Hyperosmotic Shocks. To elevate cytoplasm crowding with hyperosmotic shocks, ASW was prepared to 120% of its normal content by adjusting the amount of Deionized (DI) water to salts mixtures. The eggs were laid down on protamine-coated dishes in the hyperosmotic water and then injected. Higher concentrations of 150% were tested, but droplets could not be pulled in such cytoplasm. To reduce cytoplasm crowding with hypoosmotic shocks, the eggs were first injected, and then ASW was diluted by the same volume of DI water equal to ASW inside the dishes, to reach an ASW at 50% of its normal content.

Osmolality Measurements. The osmolality of the ASWs at different concentrations was estimated with the osmometer (VAPRO Vapor Pressure Osmometer 5600; ELITechGroup). The measurements were done at least twice for each salt concentration and the average values for the 50% ASW, ASW, and 120% ASW were, respectively, 452, 866, and 1,076 mOsm/kg, corresponding to osmotic pressure drops of -1.02 MPa and +0.52 MPa respectively.

Chemical Inhibitors. Cytoskeletal inhibitors were prepared in 100 \times stock aliquots in dimethyl sulfoxide. Nocodazole (Sigma-Aldrich) was applied ~5 min before pulling the oil droplet at a final concentration of 20 μ M. Latrunculin B (Sigma-Aldrich) was first diluted in 2 mL ASW and then added ~5 min before pulling to reach the final concentration of 20 μ M.

Magnetic Force Application. In vivo magnetic tweezers were implemented as described previously (21, 26, 31, 54, 55). The magnet probe used for force applications in vivo was built from three rod-shaped strong neodymium magnets (diameter 4 mm; height 10 mm; S-04-10-AN; Supermagnet) prolonged by a sharpened steel piece with a tip diameter of ~60 μ m to create a magnetic gradient. The surface of the steel tip was electro-coated with gold to prevent oxidation. The probe was controlled with a micromanipulator (Injectman 4; Eppendorf) and mounted on an inverted epifluorescent microscope.

Super-paramagnetic 1- μ m Dynabeads (MyOne Streptavidin C1; Thermofisher) were pulled inside the cytoplasm as single beads. To prepare beads for injection, a 1- μ L bead suspension was diluted in 100- μ L washing solution (1 M NaCl with 1% Tween-20) and sonicated for 20 min. Beads were then separated by a magnet, rinsed in 100- μ L PBS BSA 1%, and sonicated for 20 min after 5 min of incubation. The beads were then resuspended in 20 μ L 2 μ g/mL Atto565-biotin (Sigma-Aldrich), incubated for 5 min, and finally resuspended in 20 μ L PBS.

Hydrophilic super-paramagnetic 800 nm particles (NanoLink; Solulink) were used for their propensity to form large and compact aggregates inside the eggs (26). A solution of 10- μ L undiluted streptavidin beads was first washed in 100- μ L washing solution and sonicated for 1 h. The beads were then incubated for 15 min in 100 μ L 2 μ g/mL Atto565-biotin (Sigma-Aldrich), rinsed in 100- μ L (PBS), and finally resuspended in 20 μ L PBS. To form aggregates in cells, beads were first pulled by the magnet to one side of the egg to form an aggregate close to the cortex gathering all the beads inside the cytoplasm. Then, the dish was rotated, and the aggregate was pulled from the other side of the egg. The aggregates often stretched along the pulling direction, which could potentially reduce their viscous drag.

To pull oil droplets in the cytoplasm, a suspension of 10 μ L 1.2 μ m hydrophobic superparamagnetic beads (magtivio; MagSi-proteomics C18) was washed in 100 μ L 30, 50, and 70% ethanol solution. It was then dried in vacuum for ~20 min and resuspended in ~10 μ L soybean oil (Naissance; Huile de soja). All the

bead suspensions were kept at 4 °C until use. All oil-injected eggs in each sample were surveyed to identify oil droplets with a sufficient amount of beads needed for pulling. After approaching the magnet, beads inside the oil progressively formed a compact aggregate and slowly moved toward the magnet while the oil droplet was stationary until the aggregate contacted the oil-cytoplasm interface on the side facing the magnet tip.

Large aggregates could not usually cross the interface due to the oil surface tension, aggregate size, and hydrophobic properties of the beads, and were used to pull oil droplets in the cytoplasm. Upon force application, the magnet was quickly retracted when the oil distance to the cell cortex was ~10 μ m, which usually caused aggregate detachment from the oil-cytoplasm interface and backward relaxation of the droplet along the initial pulling force axis. The initial position-dependent experiments with the oil droplets were done similarly as for aggregates. Oil droplets were first pulled toward the cortex on one side of the egg. However, the droplets could not stay very close to the cortex because of the viscoelastic response of the cytoplasm. Then, the dish was rotated and the oil droplet was pulled from the opposite side along the diagonal direction. Droplets were displaced slowly to change the offset and suppress the oil droplet from recoiling toward its initial position (21). The droplet was pulled again in the same direction after at least a 5-min delay to ensure a complete relaxation of the droplet.

Magnet Force Calibration. Magnetic forces were calibrated in vitro following procedures described previously (21, 26, 54). The magnetic force field created by the magnet tip was first characterized by pulling super-paramagnetic 1 μ m Dynabeads (MyOne Streptavidin C1; Thermofisher) in a viscous test fluid (80% glycerol; viscosity 8.0×10^{-2} Pa.s at 22 °C) along the principal axis of the magnet tip. Small motion of the fluid was subtracted by tracking 0.5- μ m nonmagnetic fluorescent tracers (Molecular probes; Invitrogen) in the same suspension. The speed of magnetic beads was computed as a function of the distance to the magnet, to obtain and trace the decay function of the magnetic force, which was fitted using a double exponential function (SI Appendix, Fig. S2A).

To calculate the dependence of the force on aggregate size, bead aggregates from the same types of beads (hydrophilic or hydrophobic) as those used within the cytoplasm or within oil droplets in sizes ranging from 2 to 7 μ m, similar to that used in vivo, were pulled in the same fluid as above. The speed V_a was measured and transformed into a force using Stokes' law $F = 6\pi\eta R V_a$, where η is the viscosity of the test fluid, R the aggregate effective radius defined as the geometric mean of the longest and shortest axes of the aggregate $R = \frac{1}{2}\sqrt{L_1 L_2}$. The force-size relationship at a fixed distance from the magnet was well represented and fitted by a cubic function (SI Appendix, Fig. S2B). The cubic fit error in the 95% CI is ~10% which introduces some uncertainty in the force estimation and viscoelastic parameters, significantly smaller than the SD in the results emerging from cell to cell variability.

In each live cell experiment, the size of the aggregates inside the cytoplasm (for hydrophilic beads) or within each oil droplet (for hydrophobic beads) was measured at three different positions in the fluorescence or bright field images and averaged (SI Appendix, Fig. S2C). Importantly, larger oil droplets did not necessarily contain larger aggregates. These speed-distance and force-size relationships were combined to compute the magnetic forces applied to the hydrophilic or hydrophobic bead aggregates as a function of time, from the size of aggregates and their distance to the magnet tip.

Imaging. Time-lapses of oil droplets, aggregates, and beads moving under magnetic force were recorded on two inverted microscope set-ups equipped with a micromanipulator for magnetic tweezers, at a stabilized room temperature (18 to 20 °C). The first set-up was an inverted epifluorescence microscope (TI-Eclipse; Nikon) combined with a complementary metal-oxide-semiconductor camera (Hamamatsu), using a 20 \times DIC dry objective (Apo; NA 0.75; Nikon) and a 1.5 \times magnifier, yielding a pixel size of 0.216 μ m. The second one was a Leica DMI6000 B microscope equipped with an A-Plan 40 \times /0.65 PH2 objective yielding a pixel size of 0.229 μ m, and an ORCA-Flash4.0LT Hamamatsu camera. Both microscopes were operated with Micro-Manager (Open Imaging). Imaging was done in DIC/fluorescence/bright field at a rate of 1 frame per s. Immuno-stained eggs presented in SI Appendix, Fig. S1 A and B were imaged on a spinning-disk confocal microscope (TI-Eclipse; Nikon) equipped with a Yokogawa CSU-X1FW spinning head, and a Prime BSI camera (Photometrics), using a 60 \times water-immersion objective (Apo; NA 1.2; Nikon).

Tracking Bead and Droplet Positions. Magnet tip position was recorded in the bright field or fluorescent images through the fluorescent beads attracted onto the magnet. Oil droplets and aggregates time-lapse images were rotated to align their displacement vector antiparallel to the horizontal x-axis meaning that they all move from the right to the left. The position of beads and aggregates was tracked from their fluorescence signal using the TrackMate plugin in Fiji. The trajectories of the beads were rotated to align their displacement from the right to the left. Bright-field images of oil droplets were segmented in Fiji from the contrast at the periphery of the droplet and tracked using the TrackMate plugin. Displacement of the oil droplet was corrected when the egg had moved during the pulling.

Viscoelastic Parameter Calculation. Oil droplet and bead displacements were fitted with a Jeffreys model using a custom written code in Matlab (Mathwork) to compute viscoelastic parameters (Fig. 1 B and C). For the rising phase, the position was fitted using:

$$\frac{dx(t)}{f(t)} = \frac{1}{\kappa} (1 - e^{-\frac{\kappa}{\gamma_1} t}) + \frac{t}{\gamma_2}, \quad [1]$$

where dx is the displacement along the x-axis and f is the magnetic force. This rescaling of the displacement by force allows to compensate for variations in force amplitude during each pull, and implicates that we assume that viscoelastic responses are mostly linear. These fits allowed to compute the restoring stiffness, κ , and the viscoelastic drags γ_1 and γ_2 of oil droplets and beads, and thus the viscoelastic timescales as $\tau_{1,2} = \gamma_{1,2}/\kappa$.

Trajectories of beads during the relaxation phase were influenced by the intrinsic cytoplasm fluctuations and beads started random motions after moving a few steps backward (Fig. 1A). It was assumed the viscoelastic response of beads was ended and that the Brownian motion started when the angle between two successive steps exceeded 90 degrees. Relaxation phases of beads, aggregates, and oil droplets were fitted using:

$$\frac{dx(t)}{dx(0)} = (1 - a)e^{-\frac{t}{\tau_r}} + a, \quad [2]$$

where $t = 0$ corresponds to the time of the end of force application, to compute the decay timescale τ_r .

Fit to the data was obtained for every single experiment using the optimization method in Matlab in which the results are less sensitive than the nonlinear least squares method to the initial values.

Statistical Error Analysis. The statistical metrics r-squared (R^2) and relative absolute error (RAE) were used to test which models best explain the experimental data. The following equation was used for the R^2 measurement:

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2}, \quad [3]$$

where y_i are experimental drag values for the bead, aggregate, and oil droplets and \hat{y}_i and \bar{y} represent predicted values by the model and average experimental data, respectively. We obtained $R^2 = -1.86$ for the linear Stokes' model and $R^2 = 0.37$ for the nonlinear model including the confinement correction. The negative R^2 value indicates that the average of the data can describe the points better than linear model, and therefore, Stokes' model does not fit properly the data. RAE of the models was also considered, and computed as:

$$RAE = \frac{\sum_{i=1}^n |y_i - \hat{y}_i|}{\sum_{i=1}^n |y_i - \bar{y}|}. \quad [4]$$

RAE is smaller when the model fits better to the experimental data points. The calculated RAE for the linear Stokes' model was 1.018, twice the corresponding value of the nonlinear model, 0.53.

Flow Analysis. The recorded oil droplet images in DIC/bright field were analyzed using the particle image velocimetry PIVlab tool in Matlab. The exterior of the egg and oil droplet surface at each frame were masked to be excluded from the analysis. Contrast limited adaptive histogram equalization and two-dimensional Wiener filter with accordingly windows of 20 and 3 pixels widths were applied on the images in the pre-processing steps for noise reduction. Image sequences were investigated in the Fourier space by four interrogation windows with 64, 32, 16, and 8 pixels widths and 50% overlapped area. The spline method was used for the window deformation and subpixel resolution obtained by two-dimensional Gaussian fits. The distribution of velocity components of vectors for each set was visually inspected and restricted to remove outliers in the post-processing stage. Moreover, two other filters based on the SD and local median of velocity vectors were applied to validate the vector fields. The output vector fields after smoothing were used for further analysis and for plotting flow maps and streamlines in MATLAB.

Finite Element Hydrodynamic Simulations Using COMSOL. Pulling of the object in the cytoplasm was modeled as a time-dependent problem using the finite element software COMSOL, using an Oldroyd-B viscoelastic model. Oldroyd-B is a three element viscoelastic fluid model consisting of a Maxwell element in parallel with a viscous element represented by the constitutive equation $\dot{\sigma} + \kappa^o \frac{\sigma}{\eta_2^o} = \eta_1^o \ddot{\epsilon} + \frac{\kappa(\eta_1^o + \eta_2^o)}{\eta_2^o} \dot{\epsilon}$, where σ and ϵ denote stress and strain,

and dots represent temporal derivative (34). The parameters κ^o , η_2^o , and η_1^o , respectively, indicate stiffness, viscosity of the dashpot in series with the spring, and viscosity of the dashpot parallel to the spring. This viscoelastic model is equivalent to Jeffreys model as one can write the Oldroyd-B model parameters as a function of Jeffreys parameters measured experimentally:

$$\kappa^o = \kappa \left(\frac{\gamma_2}{\gamma_1 + \gamma_2} \right)^2, \quad [5]$$

$$\gamma_2^o = \frac{\gamma_2^2}{\gamma_1 + \gamma_2}, \quad [6]$$

$$\gamma_1^o = \frac{\gamma_1 \gamma_2}{\gamma_1 + \gamma_2}. \quad [7]$$

The viscous drag γ_2^o is associated with the dashpot in series with the elastic element describing the reorganization of cytoplasm. The drag γ_1^o is connected to the dashpot parallel to the elastic element serving for the viscosity of cytoplasm, and κ^o is the cytoplasm stiffness. We could obtain the viscosity through the Stokes' law $\gamma = 6\pi\eta r$. However, we also had to take into account the correction factor from confinement $C(\lambda)$, yielding $\gamma(\lambda) = 6\pi\eta r C(\lambda)$, with:

$$C(\lambda) = \frac{4(1 - \lambda^5)}{4 - 9\lambda + 10\lambda^3 - 9\lambda^5 + 4\lambda^6}, \quad [8]$$

where $\lambda = r/R$ is the ratio of oil droplet radius to egg radius. Considering the simulation results (SI Appendix, Fig. S6B), we assumed the viscoelastic timescale $\tau_1 = \gamma_1/\kappa$ as a constant material property which allowed us to apply the same confinement correction factor $C(\lambda)$ to calculate stiffness inside the cell.

For simplicity, we modeled the oil droplet as a spherical elastic sphere with different radii r , and set its initial position in the center of the coordinate system except for the one-by-one and position-dependent simulations (Figs. 3 E and F and 4-6 and SI Appendix, Fig. S5). The egg was represented as a large non-deformable sphere of radius R . The cytoplasm was interacting with the pulled object by including viscoelastic flow and solid mechanics modules in COMSOL through stresses at the boundaries. A Heaviside step function was used to apply a constant force as a body load with an amplitude equals to the average magnetic force in the experiments and the same pulling time. A no-slip wall condition was

set as a default on the boundaries and changed to slip condition on the walls of droplet and cell to examine its impact on the results (Fig. 5).

We first verified the lack of impact of the elasticity of the pulled objects by varying this parameter over a very wide range. The elasticity had an overall little impact, lesser than 20%, on the viscosities. The viscoelastic timescale τ_2 was differing from the actual cytoplasm properties by less than ~44% (SI Appendix, Fig. S5A). As COMSOL is a finite-element simulation software in which elements are discretized by a mesh, we also tested several mesh sizes including fine, normal, coarse, and coarser and observed that the results from different mesh sizes were not significantly different (SI Appendix, Fig. S5B). The simulations were performed using a coarse mesh size, and the size of the pulled object was reduced to the extent that re-meshing was feasible for the combination of used parameters and simulation time was reasonable. We then needed to ensure that bulk viscosities and viscoelastic timescales, $\tau_2 = \gamma_2/\kappa$ could be correctly evaluated from the drags and spring constants by fitting the one-dimensional Jeffreys model to the simulated displacement curves. In the COMSOL model, we varied input cytoplasm properties η_1 , η_2 , and τ_2 around the average experimental values and measured the simulated displacements. We next fitted the one-dimensional Jeffreys model to the scaled pulling curves, extracted and converted the output bulk properties to the Oldroyd-B model, which were close to the input values

(SI Appendix, Fig. S5 C-E). The maximum deviation between the input and output viscosities in the range of values that were tried was less than ~20%. These results show that the one-dimensional model is sufficient to describe bulk cytoplasm properties in three dimensions.

Heat maps, flow fields, and streamlines of the simulations were plotted using COMSOL, and the rest of the analysis were done using custom written codes in MATLAB similar to the experimental data. The input parameters of the simulations for Figs. 4–6 are summarized in SI Appendix, Table S1.

Data, Materials, and Software Availability. All study data are included in the article and/or SI Appendix.

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1. K. Luby-Phelps, Cytoarchitecture and physical properties of cytoplasm: Volume, viscosity, diffusion, intracellular surface area. *Int. Rev. Cytol.* **192**, 189–221 (2000).
2. L. Stagg, A. Christiansen, P. Wittung-Stafshede, Macromolecular crowding tunes folding landscape of parallel α/β protein Apoflavodoxin. *J. Am. Chem. Soc.* **133**, 646–648 (2011).
3. A. T. Molines *et al.*, Physical properties of the cytoplasm modulate the rates of microtubule polymerization and depolymerization. *Dev. Cell* **57**, 466–479.e6 (2022).
4. B. M. Regner *et al.*, Anomalous diffusion of single particles in cytoplasm. *Biophys. J.* **104**, 1652–1660 (2013).
5. M. C. Konopka, I. A. Skhel, S. Cayley, M. T. Record, J. C. Weishaar, Crowding and confinement effects on protein diffusion in vivo. *J. Bacteriol.* **188**, 6115–6123 (2006).
6. H. Tanimoto, A. Kimura, N. Minc, Shape-motion relationships of centering microtubule asters. *J. Cell Biol.* **212**, 777–787 (2016).
7. S. Reinsch, P. Gonczy, Mechanisms of nuclear positioning. *J. Cell Sci.* **111**, 2283–2295 (1998).
8. J. Xie, N. Minc, Cytoskeleton force exertion in bulk cytoplasm. *Front. Cell Dev. Biol.* **8**, 69 (2020).
9. S. Hurst, B. E. Vos, M. Brandt, T. Betz, Intracellular softening and increased viscoelastic fluidity during division. *Nat. Phys.* **17**, 1270–1276 (2021).
10. E. Moenndarby *et al.*, The cytoplasm of living cells behaves as a poroelastic material. *Nat. Mater.* **12**, 253–261 (2013).
11. M. T. Valentine, Z. E. Perlman, T. J. Mitchison, D. A. Weitz, Mechanical properties of *Xenopus* egg cytoplasmic extracts. *Biophys. J.* **88**, 680–689 (2005).
12. Y. Hiramoto, Rheological properties of echinoderm eggs during cell division. *Biorheology* **19**, 71–78 (1982).
13. Y. Tseng, T. P. Kole, D. Wirtz, Micromechanical mapping of live cells by multiple-particle-tracking microrheology. *Biophys. J.* **83**, 3162–3176 (2002).
14. M. Mittasch *et al.*, Non-invasive perturbations of intracellular flow reveal physical principles of cell organization. *Nat. Cell Biol.* **20**, 344–351 (2018).
15. J. Hu *et al.*, Size- and speed-dependent mechanical behavior in living mammalian cytoplasm. *Proc. Natl. Acad. Sci. U.S.A.* **114**, 9529–9534 (2017).
16. B. R. Parry *et al.*, The bacterial cytoplasm has glass-like properties and is fluidized by metabolic activity. *Cell* **156**, 183–194 (2014).
17. W. M. Smigiel *et al.*, Protein diffusion in *Escherichia coli* cytoplasm scales with the mass of the complexes and is location dependent. *Sci. Adv.* **8**, eabo5387 (2022).
18. R. Niwayama, K. Shinohara, A. Kimura, Hydrodynamic property of the cytoplasm is sufficient to mediate cytoplasmic streaming in the *Caenorhabditis elegans* embryo. *Proc. Natl. Acad. Sci. U.S.A.* **108**, 11900–11905 (2011).
19. N. Klughammer *et al.*, Cytoplasmic flows in starfish oocytes are fully determined by cortical contractions. *PLoS Comput. Biol.* **14**, e1006588 (2018).
20. J.-F. Berret, Local viscoelasticity of living cells measured by rotational magnetic spectroscopy. *Nat. Commun.* **7**, 10134 (2016).
21. J. Xie *et al.*, Contribution of cytoplasm viscoelastic properties to mitotic spindle positioning. *Proc. Natl. Acad. Sci. U.S.A.* **119**, e2115593119 (2022).
22. E. Nazockdast, A. Rahimian, D. Needleman, M. Shelley, Cytoplasmic flows as signatures for the mechanics of mitotic positioning. *Mol. Cell Biol.* **28**, 3261–3270 (2017).
23. H.-Y. Wu, Laser ablation and fluid flows show a single force mechanism governs spindle positioning. *Biophysics [Preprint]* (2021). 10.1101/2021.11.21.469320 (Accessed 9 September 2022).
24. J. Happel, H. Brenner, *Low Reynolds Number Hydrodynamics: With Special Applications to Particulate Media* (Springer Science & Business Media, 2012).
25. A. De Simone, A. Spahr, C. Busso, P. Gonczy, Uncovering the balance of forces driving microtubule aster migration in *C. elegans* zygotes. *Nat. Commun.* **9**, 938 (2018).
26. H. Tanimoto, J. Salle, L. Dodin, N. Minc, Physical forces determining the persistency and centering precision of microtubule asters. *Nat. Phys.* **14**, 848–854 (2018).
27. S. L. Rogers, V. I. Gelfand, Membrane trafficking, organelle transport, and the cytoskeleton. *Curr. Opin. Cell Biol.* **12**, 57–62 (2000).
28. E. Voronina, W. F. Marzluff, G. M. Wessel, Cyclin B synthesis is required for sea urchin oocyte maturation. *Dev. Biol.* **256**, 258–275 (2003).
29. R. A. Heil-Chapdelaine, J. J. Otto, Relative changes in F-actin during the first cell cycle: Evidence for two distinct pools of F-actin in the sea urchin egg. *Cell Motility* **34**, 26–35 (1996).
30. Y. Hiramoto, Mechanical properties of the protoplasm of the sea urchin egg. I. Unfertilized egg. *Exp. Cell Res.* **56**, 201–208 (1969).
31. C. Garzon-Coral, H. A. Fantana, J. Howard, A force-generating machinery maintains the spindle at the cell center during mitosis. *Science* **352**, 1124–7 (2016).
32. F. H. C. Crick, A. F. W. Hughes, The physical properties of cytoplasm: A study by means of the magnetic particle method Part I. Experimental. *Exp. Cell Res.* **1**, 37–80 (1950).
33. H. A. Barnes, J. F. Hutton, K. Walters, *An Introduction to Rheology* (Elsevier, 1989).
34. D. R. Bland, *The Theory of Linear Viscoelasticity* (Courier Dover Publications, 2016).
35. A. C. Giese, A. Farmanfarmaian, Resistance of the purple sea urchin to osmotic stress. *Biol. Bull.* **124**, 182–192 (1963).
36. A. Miermont *et al.*, Severe osmotic compression triggers a slowdown of intracellular signaling, which can be explained by molecular crowding. *Proc. Natl. Acad. Sci. U.S.A.* **110**, 5725–5730 (2013).
37. G. Guigas, C. Kalla, M. Weiss, Probing the nanoscale viscoelasticity of intracellular fluids in living cells. *Biophys. J.* **93**, 316–323 (2007).
38. B. Alic, C. Formosa-Dague, E. Dague, L. J. Holt, M. Delarue, Macromolecular crowding limits growth under pressure. *Nat. Phys.* **18**, 411–416 (2022).
39. J. Lemièrre, P. Real-Calderon, L. J. Holt, T. G. Fai, F. Chang, Control of nuclear size by osmotic forces in *Schizosaccharomyces pombe*. *Elife* **11**, e76075 (2022).
40. L. Carlini, G. P. Brittingham, L. J. Holt, T. M. Kapoor, Microtubules enhance mesoscale effective diffusivity in the crowded metaphase cytoplasm. *Dev. Cell* **54**, 574–582.e4 (2020).
41. K. Luby-Phelps, D. L. Taylor, F. Lanni, Probing the structure of cytoplasm. *J. Cell Biol.* **102**, 2015–22 (1986).
42. E. Nazockdast, A. Rahimian, D. Zorin, M. Shelley, A fast platform for simulating semi-flexible fiber suspensions applied to cell mechanics. *J. Comput. Phys.* **329**, 173–209 (2017).
43. J. Saleh *et al.*, Length-limitation of astral microtubules orients cell divisions in intestinal crypts. *bioRxiv [Preprint]* (2022). <https://www.biorxiv.org/content/10.1101/2022.09.02.506333v1> (Accessed 2 September 2022).
44. P. T. Tran, L. Marsh, V. Doye, S. Inoue, F. Chang, A mechanism for nuclear positioning in fission yeast based on microtubule pushing. *J. Cell Biol.* **153**, 397–411 (2001).
45. T. P. Lele, R. B. Dickinson, G. G. Gundersen, Mechanical principles of nuclear shaping and positioning. *J. Cell Biol.* **217**, 3330–3342 (2018).
46. K. M. Forrest, E. R. Gavis, Live imaging of endogenous RNA Reveals a diffusion and entrapment mechanism for nanos mRNA localization in *Drosophila*. *Curr. Biol.* **13**, 1159–1168 (2003).
47. A. Al Jord *et al.*, Cytoplasmic forces functionally reorganize nuclear condensates in oocytes. *Nat. Commun.* **13**, 5070 (2022).
48. V. E. Deneke *et al.*, Self-organized nuclear positioning synchronizes the cell cycle in *Drosophila* embryos. *Cell* **177**, 925–941.e17 (2019).
49. K. Yi *et al.*, Dynamic maintenance of asymmetric meiotic spindle position through Arp2/3-complex-driven cytoplasmic streaming in mouse oocytes. *Nat. Cell Biol.* **13**, 1252–1258 (2011).
50. L. R. Serbus, B.-J. Cha, W. E. Theurkauf, W. M. Saxton, Dynein and the actin cytoskeleton control kinesin-driven cytoplasmic streaming in *Drosophila* oocytes. *Development* **132**, 3743–3752 (2005).
51. S. Shamipour *et al.*, Bulk actin dynamics drive phase segregation in zebrafish oocytes. *Cell* **177**, 1463–1479.e18 (2019).
52. R. Gerum *et al.*, Viscoelastic properties of suspended cells measured with shear flow deformation cytometry. *Elife* **11**, e78823 (2022).
53. V. E. Foe, G. von Dassow, Stable and dynamic microtubules coordinately shape the myosin activation zone during cytokinetic furrow formation. *J. Cell Biol.* **183**, 457–70 (2008).
54. J. Salle *et al.*, Asymmetric division through a reduction of microtubule centering forces. *J. Cell Biol.* **218**, 771–782 (2019).
55. N. Ierushalmi *et al.*, Centering and symmetry breaking in confined contracting actomyosin networks. *Elife* **9**, e55368 (2020).