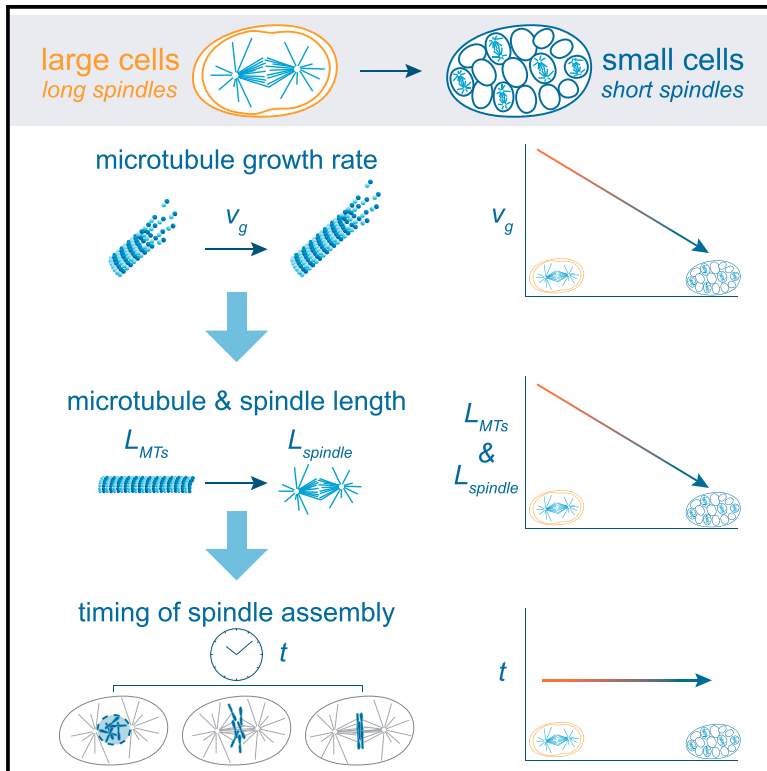


Developmental Cell

Microtubule Dynamics Scale with Cell Size to Set Spindle Length and Assembly Timing

Graphical Abstract



Authors

Benjamin Lacroix, Gaëlle Letort,
Laras Pitay, ..., Nicolas Minc,
François Nédélec, Julien Dumont

Correspondence

benjamin.lacroix@ijm.fr (B.L.),
nedelec@embl.de (F.N.),
julien.dumont@ijm.fr (J.D.)

In Brief

During early embryonic development, the mitotic spindle scales with decreasing cell size across successive reductive divisions. Lacroix et al. uncover, using *in vivo* and *in silico* analyses, a common scaling mechanism whereby spindle microtubule growth rate is coupled to cell volume for size scaling while maintaining constant spindle assembly timing.

Highlights

- Microtubule dynamics scales with cell size during embryonic development
- Microtubule growth rate controls spindle length adaptation to cell size
- Timing of spindle assembly is constant and independent of spindle and cell size
- Microtubule growth rate regulates spindle length and assembly timing



Microtubule Dynamics Scale with Cell Size to Set Spindle Length and Assembly Timing

Benjamin Lacroix,^{1,*} Gaëlle Letort,² Laras Pitayu,¹ Jérémy Sallé,¹ Marine Stefanutti,¹ Gilliane Maton,¹ Anne-Marie Ladouceur,³ Julie C. Canman,⁴ Paul S. Maddox,³ Amy S. Maddox,³ Nicolas Minc,¹ François Nédélec,^{5,*} and Julien Dumont^{1,6,*}

¹Institut Jacques Monod, CNRS, UMR 7592, University Paris Diderot, Sorbonne Paris Cité, 75205 Paris, France

²Institut Curie, Mines Paris Tech, Inserm, U900, PSL Research University, 75005 Paris, France

³Department of Biology, University of North Carolina, Chapel Hill, NC 27599, USA

⁴Columbia University Medical Center, Department of Pathology and Cell Biology, New York, NY 10032, USA

⁵Cell Biology and Biophysics Unit, European Molecular Biology Laboratory, 69117 Heidelberg, Germany

⁶Lead Contact

*Correspondence: benjamin.lacroix@ijm.fr (B.L.), nedelec@embl.de (F.N.), julien.dumont@ijm.fr (J.D.)

<https://doi.org/10.1016/j.devcel.2018.04.022>

SUMMARY

Successive cell divisions during embryonic cleavage create increasingly smaller cells, so intracellular structures must adapt accordingly. Mitotic spindle size correlates with cell size, but the mechanisms for this scaling remain unclear. Using live cell imaging, we analyzed spindle scaling during embryo cleavage in the nematode *Caenorhabditis elegans* and sea urchin *Paracentrotus lividus*. We reveal a common scaling mechanism, where the growth rate of spindle microtubules scales with cell volume, which explains spindle shortening. Spindle assembly timing is, however, constant throughout successive divisions. Analyses *in silico* suggest that controlling the microtubule growth rate is sufficient to scale spindle length and maintain a constant assembly timing. We tested our *in silico* predictions to demonstrate that modulating cell volume or microtubule growth rate *in vivo* induces a proportional spindle size change. Our results suggest that scalability of the microtubule growth rate when cell size varies adapts spindle length to cell volume.

INTRODUCTION

Eukaryotic cells range in size over six orders of magnitude. Regardless of size from the smallest unicellular eukaryote *Ostreococcus tauri* (<1 μm) to long motor neurons (>1 m long), all cells contain a common set of organelles and subcellular structures. This requirement mandates a strict scaling between these intracellular components and cell size. One striking example of this scaling is the progressive decrease in cell volume that occurs during cleavage of early embryos. Early embryonic development usually occurs without an increase in the overall embryo volume. Each round of cell division halves the size of blastomeres, so blastomere volume can decrease by three orders of magnitude from single-celled zygotes to multicellular

gastrulae (O'Farrell et al., 2004). Thus, intracellular structures and organelles must adapt to this wide range of cell dimensions by adjusting their spatial distribution and/or size to remain functional (West and Brown, 2005). Organelles known to exhibit size adaptation to cell volume variations include nuclei, cilia, endoplasmic reticulum, and cytoskeletal assemblies such as the metaphase spindle (reviewed in Chan and Marshall, 2010, 2012; Levy and Heald, 2012; Marshall, 2015b; Reber and Goehring, 2015).

The metaphase spindle is a bipolar structure composed of highly dynamic microtubules. Adapting spindle length to cell volume enables accurate chromosome segregation and spindle orientation to accommodate different scales (Dumont and Mitchison, 2009a; Holmfeldt et al., 2006; Lancaster et al., 2013). Spindle length scaling among different organisms can occur through biochemical variations in cytoplasmic content. For example, a single amino acid change in the microtubule-severing protein katanin primarily accounts for the spindle length difference observed between oocytes from *Xenopus laevis* and the smaller closely related frog *Xenopus tropicalis* (Brown et al., 2007; Loughlin et al., 2011). In contrast, the biochemical composition of different sized blastomeres from a given species is assumed to be constant (Mitchison et al., 2015). During cleavage of the large *X. laevis* embryo, spindle length remains constant for the first five divisions and then decreases linearly with blastomere radius for the next five to seven divisions (Wuhr et al., 2008). In contrast, the smaller *Caenorhabditis elegans* embryo shows spindle length proportional to cell length from the first division throughout cleavage (Decker et al., 2011; Hara and Kimura, 2009, 2013). Seminal experiments using artificially encapsulated extracts from *X. laevis* oocytes or embryos demonstrated that spindle length directly corresponds to the size of the encapsulating droplet (Good et al., 2013; Hazel et al., 2013). These experiments accurately recapitulated the spindle scaling observed in intact embryos with a linear relationship between spindle length and droplet radius in small droplets and an upper limit to spindle length in large droplets. Intrinsic spindle mechanisms, such as balancing force between opposed motors, may account for the upper limit of spindle length scaling (Dumont and Mitchison, 2009a; b; Reber and Goehring, 2015). In contrast, spindle extrinsic mechanisms, such as component



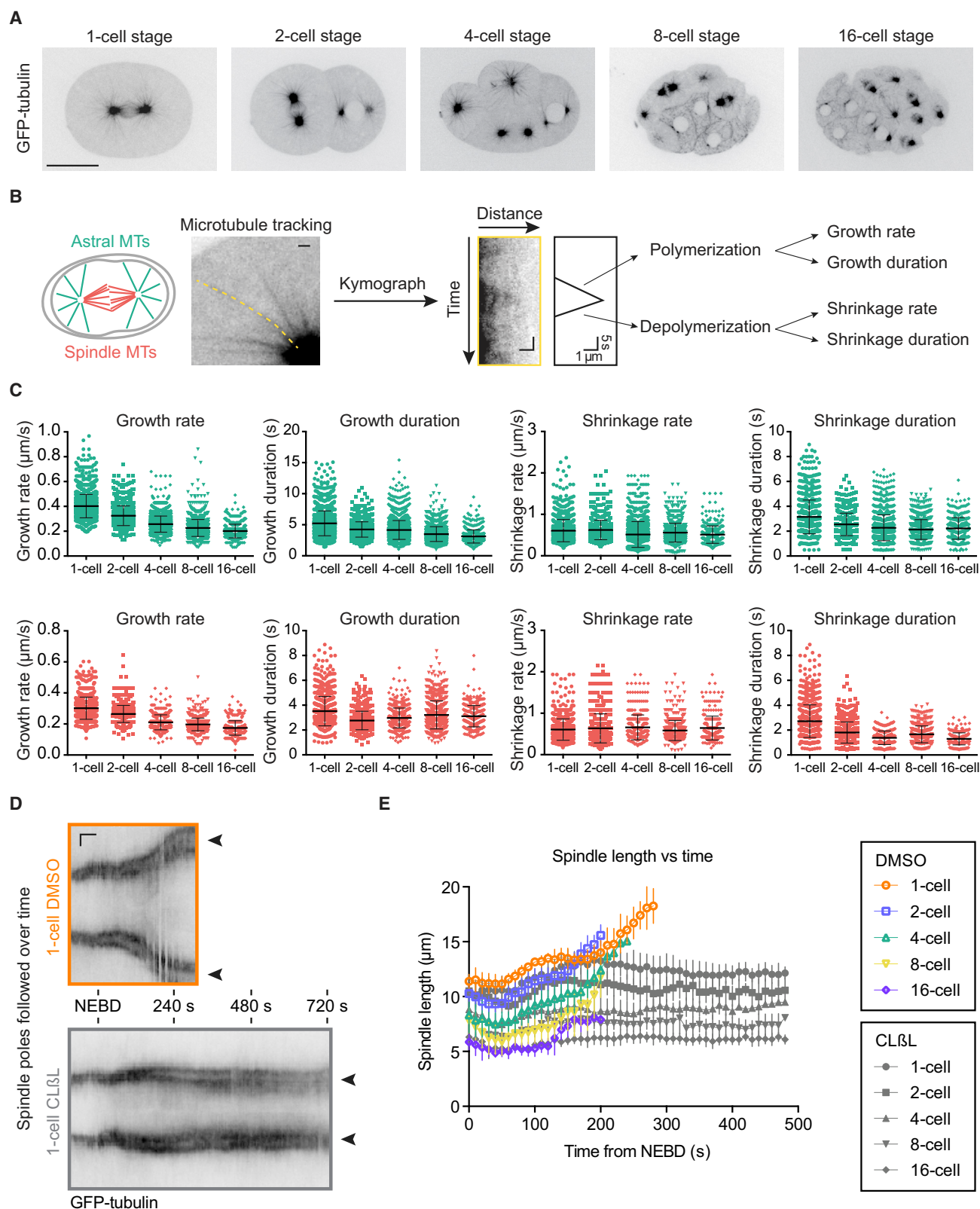


Figure 1. Astral and Spindle Microtubule Dynamics Vary during *C. elegans* Embryo Cleavage

(A) Still frames from confocal live imaging of *C. elegans* embryos expressing GFP-tagged β -tubulin during the first five embryonic divisions (1- to 16-cell stage). Images correspond to a single focal plane. Scale bar, 20 μ m.

(legend continued on next page)

limitation, have been proposed to explain how different cytoplasm volumes with a given composition may produce different spindle lengths (Goehring and Hyman, 2012; Marshall, 2015a; Mitchison et al., 2015; Reber and Goehring, 2015; Reber and Hyman, 2015). In *C. elegans* early embryos, decreasing spindle length correlates with a progressive reduction in the amount of centrosomal components and with a decaying gradient of the microtubule-associated protein TPXL-1 (ortholog of TPX2) along spindle microtubules (Greenan et al., 2010). Experiments performed in *Xenopus* egg or embryo extracts suggest that titration of tubulin heterodimers, limited amount/activity of the microtubule polymerase XMAP215, or cortical sequestration of Importin α , the negative regulator of the microtubule depolymerase KIF2A, could participate in spindle length scaling (Reber et al., 2013; Wilbur and Heald, 2013). However, it remains unclear how the limited supply of these factors controls spindle size.

The limited supply or local inactivation of key factor(s) could directly regulate spindle microtubule dynamics to efficiently control spindle length (Andersen, 2000; Andersen et al., 1997; Desai and Mitchison, 1997; Goshima et al., 2005b; Picone et al., 2010; Tournebise et al., 2000; Verde et al., 1992). Both *in vitro* and *in vivo*, microtubules alternate between phases of growth and shrinkage in a process called dynamic instability (Mitchison and Kirschner, 1984). Four parameters define these dynamic properties of microtubules: the velocities of growth and shrinkage and the frequencies of transitions between these two states, called catastrophe and rescue (Kirschner and Mitchison, 1986; Walker et al., 1988). Typically, long interphasic microtubules display low catastrophe and high rescue frequencies (Belmont et al., 1990; Verde et al., 1990, 1992). Microtubules in this state are “unbounded” and continuously elongate over time. In contrast, microtubules shorten upon mitotic entry, due to a sharp increase in catastrophe frequency and a significant decrease in rescue events. In this “bounded” regime, microtubules tend to disassemble, and their average growth velocity, termed J , is negative. A steady population of microtubules can only be maintained because a finite fraction is continuously nucleated *de novo* (Mitchison et al., 2015; Verde et al., 1992). This regime establishes a distribution of microtubule lengths to dictate a steady state spindle size. Therefore, precise control of microtubule dynamics during mitosis in cleaving embryos becomes an attractive candidate to adjust spindle length for blastomere size. However, the functional link between microtubule dynamics and spindle length scaling

as a function of cell volume during embryo cleavage remains unknown.

RESULTS

Microtubule Dynamics Are Modulated during *C. elegans* Embryo Cleavage

We first determined the potential relationship among metaphase spindle length, cell volume, and microtubule dynamics from the 1- to the 16-cell stage in cleaving *C. elegans* embryos. We combined high-temporal single-plane confocal microscopy and two-photon three-dimensional (3D)-volumetric reconstructions of live embryos expressing GFP-tagged microtubules or a plasma membrane marker respectively (Figures 1A, S1A, and S1B). In line with previous studies, we found that spindle length and cell volume progressively decreased in a sub-proportional manner across early embryogenesis in *C. elegans* (Figures S1C–S1F) (Decker et al., 2011; Greenan et al., 2010; Hara and Kimura, 2009, 2013). To determine if microtubule dynamics vary concomitantly with spindle length and cell volume, we generated kymographs of individual microtubules from our high-frame-rate, single-plane confocal series of embryos expressing GFP-tagged β -tubulin (Figure 1B). This approach allowed us to identify phases of elongation and shortening and to measure the rate and duration of individual phases for all analyzed microtubules. We observed that microtubule growth rates and durations were significantly higher for astral microtubules than spindle microtubules in all blastomeres from the 1- to the 16-cell stage, in agreement with published results for the one-cell stage (Figure 1C) (Srayko et al., 2005). In addition, we found that microtubule dynamics’ parameters for both types of microtubules varied throughout development. While we found a notable but mild decrease in shrinkage duration between the 1- and the 16-cell stage, the most striking variation across divisions was the continuous and significant decrease in microtubule growth rate for both astral and spindle microtubules (Figure 1C). Importantly, we obtained similar rates and frequencies using a different promoter to drive expression of our GFP-tagged β -tubulin reporter or mCherry-tagged β -tubulin (Figure S2 and Table S1). These results suggest that microtubule dynamics vary throughout early embryonic divisions, with a distinct decrease in the microtubule growth rate associated with decreased blastomere volume.

(B) Schematic representation of parameter extraction for microtubule dynamics from individual astral (green) or spindle (red) microtubule kymographs. One representative example of a kymograph shown of an individual astral microtubule tracked over time. Horizontal scale bars, 1 μ m, vertical scale bar (kymograph), 5 s. MT, microtubule

(C) Microtubule dynamics parameters for astral (green) and spindle (red) microtubules plotted at each cleavage stage (1- to 16-cell stage). Each dot corresponds to an individual microtubule. For both microtubule populations, each parameter significantly varies between stages (one-way ANOVA: $p < 0.01$). Only microtubule growth rates of both microtubule populations exhibit significant and continuous decrease at each stage (one-way ANOVA with Tukey’s multiple comparison tests: $p < 0.01$). All parameters, including sample size, mean, and SD for the four astral and spindle microtubule dynamics parameters at the different stages, are listed in Table S1 (horizontal bars, mean; error bars, SD; n (microtubules) ≥ 288 per cleavage stage; n (embryos) ≥ 12).

(D) Kymographs extracted from confocal live imaging of *C. elegans* embryos expressing GFP-tagged β -tubulin during the first embryonic division (one-cell stage) treated with DMSO (control, top) or with 20 μ M proteasome inhibitor, clasto-Lactacystin β -lactone (CL β L diluted in DMSO, bottom) to inhibit the metaphase-to-anaphase transition. Spindles poles (black arrowheads) are visible as two dark stripes that separate during anaphase in controls and stay at the same distance over time in CL β L-treated embryos. Timings relative to NEBD monitored by diffusion of free GFP-tagged β -tubulin in the nuclear area. Horizontal scale bar, 50 s; vertical scale bar, 5 μ m.

(E) Spindle length (aster-to-aster distance) plotted over time in DMSO (colors) and CL β L (gray) treated embryos at each cleavage stage (1- to 16-cell stage). Timings relative to NEBD ($n \geq 5$ spindles per stage in each condition). Error bars, SD.

To investigate a potential link between these variations in microtubule dynamics and spindle length, we first determined if the length of metaphase spindles reached a steady state or if they were limited by the duration of the cell cycle and the time available before anaphase onset. Indeed, cell divisions in cleaving embryos of most species are particularly rapid, and spindle length increases continuously from nuclear envelope breakdown (NEBD) to anaphase onset (Mitchison et al., 2015). However, delaying anaphase onset in *C. elegans* embryos using a proteasome inhibitor did not induce spindle elongation above the normal metaphase spindle length at any analyzed stage (Figures 1D and 1E) (Labbe et al., 2004). Moreover, the measured microtubule dynamics parameters indicate that all microtubules are in the bounded regime ($J < 0$) at every stage of embryo cleavage, which is compatible with a steady state (Figure S2B and Tables S1A and S1C) (Verde et al., 1992). These results suggest that mitotic spindles in early *C. elegans* embryos reach a steady state length before anaphase onset that is independent of the duration of mitosis. Overall, our results demonstrate that microtubule dynamic instability evolves during embryo cleavage with the microtubule growth rate continuously decreasing in parallel with the progressive reduction of steady state spindle length.

Spindle Microtubule Growth Rate Adapts to Cell Volume in *C. elegans*

We next asked if variations in microtubule dynamics parameters during early embryogenesis were either a direct consequence of cell size changes or under the control of a developmental program. Therefore, we analyzed the direct correlation between cell volume and microtubule dynamics parameters (Figures 2A and 2B). This analysis revealed that the growth rate of spindle microtubules most significantly correlated with cell volume (Figure 2B). So, we tested if the decrease in cell volume of dividing blastomeres solely accounted for this relationship or if cell fate patterning and developmental timing also contributed. Since *C. elegans* zygotes divide asymmetrically, patterning is already established at the two-cell stage by asymmetric distribution of cell fate determinants (Nance, 2005; Rose and Kemphues, 1998). The first division of the *C. elegans* zygote produces a large anterior AB blastomere from which most somatic tissues emerge and a small posterior P1 blastomere from which the germline originates (Figure 2A) (Sulston et al., 1983). We used a fast-acting temperature-sensitive (ts) mutant of formin CYK-1 to induce cytokinesis failure in the zygote (Figure 2C) (Canman et al., 2008; Davies et al., 2014). In control two-cell-stage embryos, AB and P1 blastomeres display shorter spindles than the one-celled zygote, which correlates with slower microtubule growth in both blastomeres (Figure 2D). At the restrictive temperature (25°C), *cyk-1(ts)* mutant zygotes exhibit cytokinesis failure and form abnormal one-cell embryos that kinetically correspond to two-cell-stage embryos but possess the cytoplasmic content and cell fate determinants of both AB and P1 blastomeres. These abnormal embryos assembled tetrapolar spindles with microtubules that grew at a rate indistinguishable from normal one-cell zygotes (Figures 2C and 2D). Thus cell fate determinants and developmental timing do not make a major contribution to set the spindle microtubule growth rate in cleaving *C. elegans* embryos. To further demonstrate the effect of cell volume on spindle microtubule growth rate, we generated abnormally large

zygotes. We generated embryos depleted of the fucosyltransferase C27D9.1, which does not have any known direct effect on microtubules and leads to the formation of abnormally large embryos (Hara and Kimura, 2009; Sonnichsen et al., 2005). In these extra-large zygotes, we found longer spindles and a significantly higher growth rate of spindle microtubules than in control normal-sized zygotes (Figures 2C and 2D). Altogether, these results show that the observed progressive reduction in the growth rate of spindle microtubules is directly linked to cell volume during embryonic cleavage and independent of developmental timing or cell fate.

Spindle Length Scales with Microtubule Growth Rate in *C. elegans*

We then asked if variations between dynamics parameters of astral and spindle microtubules and cell volume could underlie spindle length scaling during early embryogenesis. Strikingly, we found that the growth rate of both astral and spindle microtubules was the only parameter exhibiting a distinct, continuous, and linear relationship with spindle length throughout cleavage (Figures 3A–3C). This observation suggests that modulating the growth rate of one or both microtubule populations could be a key determinant for spindle length adaptation in cleaving embryos. However, analysis of this scaling in C27D9.1-depleted extra-large zygotes revealed that only spindle microtubule growth rate increased with spindle length (Figure 3B), while astral microtubule growth rate remained similar to controls (Figures 3C, S1G, and S1H) ($0.41 \pm 0.08 \mu\text{m/s}$ versus $0.40 \pm 0.09 \mu\text{m/s}$, $p = 0.087$ unpaired t test). These results suggest that spindle, but not astral, microtubule dynamics determine spindle length in cleaving embryos.

As the growth rate of spindle microtubules decreased progressively with cell volume during embryo cleavage and concomitant with spindle length, we hypothesized that modulating this parameter is sufficient to scale spindle length to cell volume during embryo cleavage. We calculated the average length $\langle L \rangle$ predicted from microtubule dynamics parameters (Figures 3D, S2B, S2C and Table S1) (Verde et al., 1992). In control embryos, $\langle L \rangle$ scaled linearly with our experimentally measured spindle lengths from the 1- to the 16-cell stage. This scaling implies that spindle length is a multiple of $\langle L \rangle$ and that the multiplicative factor remains relatively constant as cell size evolves. Interestingly, the predicted average length $\langle L \rangle$ of spindle microtubules in C27D9.1-depleted embryos fitted well with the abnormally long spindles in these extra-large zygotes. Thus, spindle length varies proportionally to the overall microtubule dynamics in cleaving embryos. Since rescue frequency is low but catastrophe frequency and shrinkage rate are almost constant in cleaving *C. elegans* embryos, our results demonstrate that $\langle L \rangle$ is primarily determined by the microtubule growth rate (Figures 3B, 3D, and Table S1). Our results support the idea that spindle microtubule growth rate is a key regulator to scale spindle length to cell volume.

To directly test this hypothesis, we experimentally reduced spindle microtubule growth rate in zygotes and measured spindle length. We analyzed zygotes partially depleted of the microtubule-associated protein (MAP) CLS-2 (ortholog of CLASP, Figures 3A–3C) (Cheeseman et al., 2005; Espiritu et al., 2012), since CLS-2 promotes microtubule assembly *in vitro* and *in vivo* (Maton et al., 2015). Consistent with this, in partial

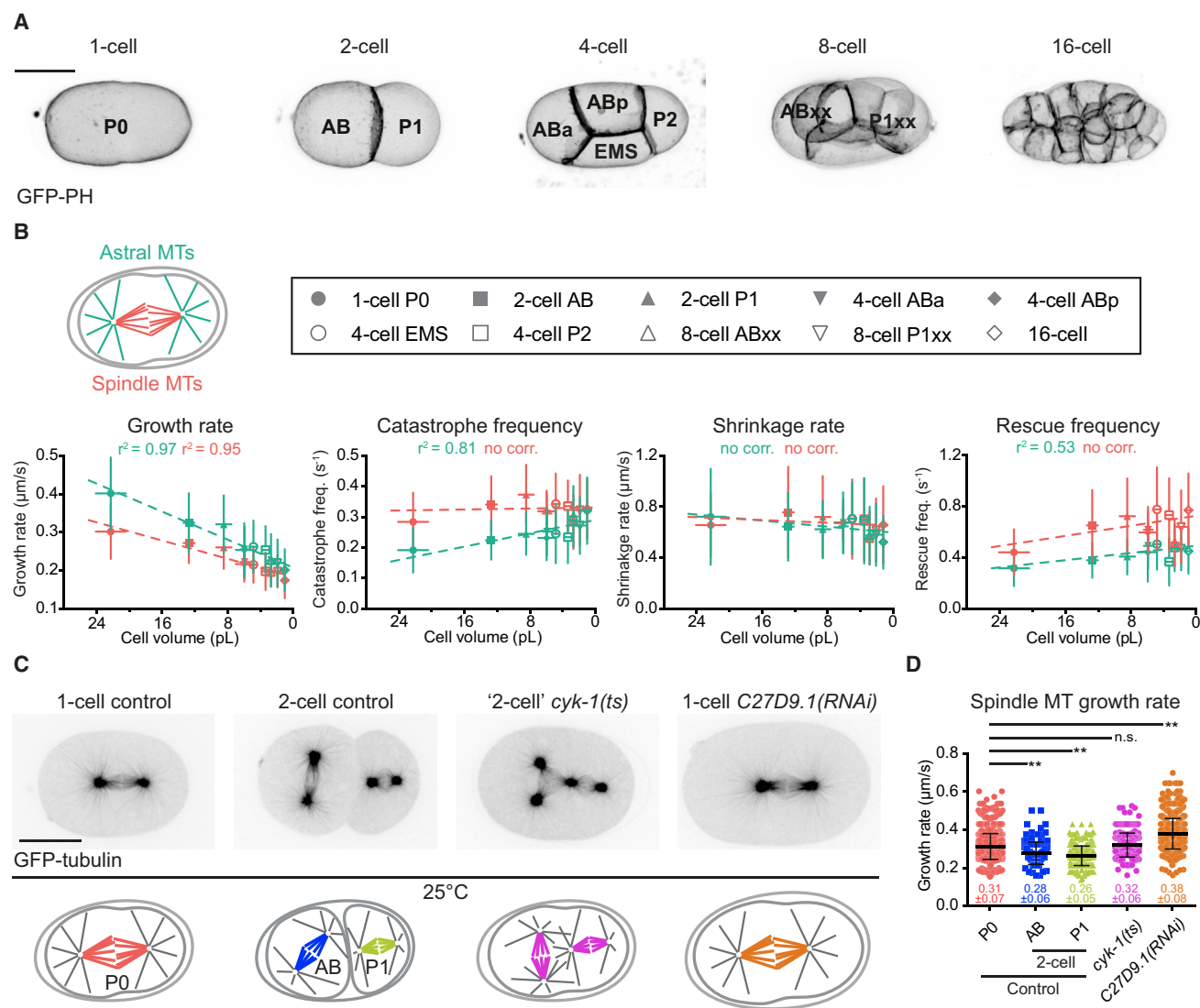


Figure 2. Astral and Spindle Microtubule Dynamics Vary with Cell Volume during *C. elegans* Embryo Cleavage

(A) Still frames from live two-photon imaging of *C. elegans* embryos expressing a GFP-tagged plasma membrane probe (Pleckstrin Homology [PH] domain) during the first five embryonic divisions (1- to 16-cell stage). Images correspond to maximal projections of z-stacks covering the entire thickness of the embryo. Scale bar, 20 μm . Blastomere names are indicated except for the 16-cell stage. At the eight-cell stage, progeny of AB and P1 were grouped together as ABxx and P1xx respectively.

(B) Mean astral (green) and spindle (red) microtubule dynamics parameters: mean microtubule growth rate, catastrophe frequency, shrinkage rate, and rescue frequency (from Figure 1C) for each type of blastomere plotted over the corresponding average cell volumes (from Figure S1). Key for different blastomeres shown in the top box. Dotted lines correspond to the linear regression curves. Error bars, SD. Pearson correlation coefficient (r^2) is indicated at the top of each graph if $p \leq 0.01$ (no corr. is indicated otherwise).

(C) From left to right, still images from confocal live imaging of *C. elegans* control one-cell embryo, control two-cell embryo, thermosensitive (*ts*) mutant embryo of the formin *cyk-1* at the two-cell stage after P0 cytokinesis failure and abnormally large *C27D9.1(RNAi)*-treated embryo. All express GFP-tagged β -tubulin. Corresponding schematics with color coding for spindle microtubules in different conditions shown at the bottom. Scale bar, 20 μm .

(D) Spindle microtubule growth rates measured at 25°C (restrictive temperature for the *cyk-1(ts)* mutant) for the indicated conditions. Color coding for the different conditions corresponds to the schematics in (C). Error bars, SD; one-way ANOVA with Dunnett's multiple comparisons test, ** $p \leq 0.01$; n.s., $p > 0.05$.

cls-2(RNAi) conditions, spindle microtubules displayed a significantly reduced growth rate compared with control zygotes (0.25 ± 0.06 versus 0.3 ± 0.07 $\mu\text{m/s}$, $p < 0.001$ unpaired t test) (Figure 3B and Table S1). Rescue frequency also slightly increased, while catastrophe frequency and shrinkage rate remained unaltered. As we predicted, abnormally short but functional spindles assembled under this condition. Strikingly, both the average

theoretical length of microtubules $\langle L \rangle$ and spindle length in these depleted zygotes were concomitantly reduced to levels corresponding to that of four-cell-stage control blastomeres (Figures 3B–3D). Taken together, our results show that microtubule dynamics parameters, specifically the growth rate of spindle microtubules, vary proportionally to cell volume and are key factors that control spindle length during *C. elegans* embryo cleavage.

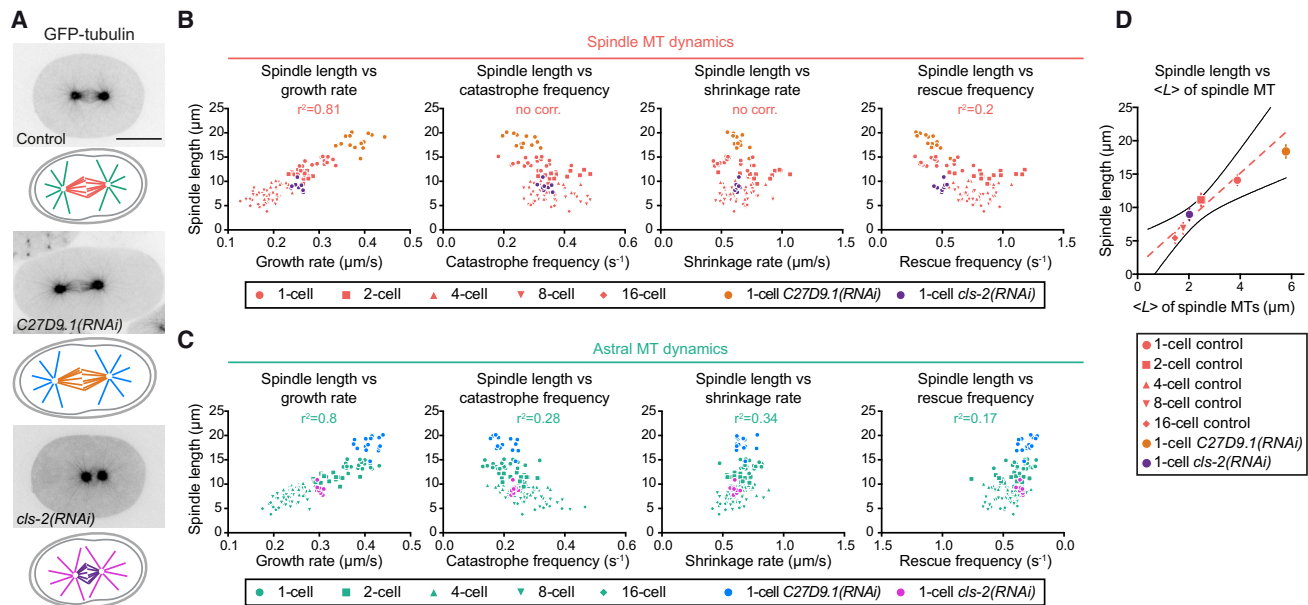


Figure 3. Spindle Length Scales with Spindle, but Not Astral, Microtubule Growth Rate

(A) From top to bottom, still images from confocal live imaging of *C. elegans* control one-cell embryo, abnormally large C27D9.1(RNAi)-treated embryo and *cls-2(RNAi)*-treated embryo. All expressing GFP-tagged β -tubulin. Corresponding schematics with color coding for astral and spindle microtubules in the different conditions shown underneath each image. Scale bar, 20 μ m.

(B) Spindle length plotted over spindle microtubule dynamics parameters in the indicated cleavage stage or condition. Key for different stages and conditions indicated at the bottom of the graphs (control, red; C27D9.1(RNAi), orange; *cls-2(RNAi)*, purple). Each dot represents the spindle length represented over mean microtubule dynamics parameters measured in an individual blastomere. n (cells) ≥ 10 with n (events/cell) ≥ 60 . Pearson correlation coefficient (r^2) for the control condition indicated at the top of each graph if $p \leq 0.01$ (no corr. is indicated otherwise).

(C) Same as (B) for astral microtubules (control, green; C27D9.1(RNAi), blue; *cls-2(RNAi)*, magenta).

(D) Average theoretical microtubule length $\langle L \rangle$ plotted over experimentally measured average spindle length in the indicated conditions (control, red; C27D9.1(RNAi), orange; *cls-2(RNAi)*, purple). Error bars, SD. $\langle L \rangle = \frac{V_g \times V_s}{V_s \times f_c - V_g \times f_r}$ with V_g , growth rate; V_s , shrinkage rate; f_c , catastrophe frequency; f_r , rescue frequency. Dotted red line and black lines represent the linear regression and 95% confidence interval respectively.

Spindle Length and Microtubule Growth Rate Scale with Cell Volume in the Sea Urchin *Paracentrotus lividus*

We next wondered whether the scaling relationship among cell volume, spindle length, and microtubule growth rate identified in *C. elegans* also takes place in other species. Sea urchin (*Paracentrotus lividus*) embryos are approximately 20 times larger in volume than *C. elegans* embryos. *P. lividus* zygotes are spherical and divide symmetrically and synchronously until the eight-cell stage (Figure 4A) (Agrell, 1956; Parisi et al., 1978). First, we microinjected *P. lividus* eggs with fluorescently labeled tubulin (ATTO 565-tubulin, Figures S3A–S3F), which then underwent fertilization. We examined the first six rounds of embryonic cleavages by live confocal microscopy (Videos S1 and S2). Consistent with previous reports for other echinoderms (Crowder et al., 2015), spindle length and cell volume progressively decreased across early embryogenesis in *P. lividus* (Figures S3G, S3H, and Table S2). Spindle lengths measured in ATTO 565-tubulin injected live embryos were indistinguishable from those in control non-injected fixed embryos (Figures S3B and S3D). To determine if microtubule dynamics also varied concomitantly with spindle length and cell volume, we generated kymographs of individual microtubules to measure spindle microtubule dynamics parameters. In line with our results from *C. elegans* embryos, microtubule dynamics parameters varied

during *P. lividus* cleavage, but the overall microtubule dynamics remained in the bounded regime at every stage (Figure 4B and Table S2). We observed a continuous and significant decrease in the growth rate of spindle microtubules across *P. lividus* embryo cleavage (Figure 4B). This decrease correlated with the progressive reduction in blastomere volume and spindle length (Figures 4C and 4D). We observed similar spindle lengths and growth rates using another fluorescent microtubule probe (the 3XmCherry-tagged ensconsin microtubule-binding domain, 3XmCherry-EMTB; Faire et al., 1999; Figures S3A–S3F). These results suggest that microtubule growth rate is a key determinant of spindle length in cleaving sea urchin embryos. Importantly, both spindle length and spindle microtubule growth rate were comparable in vegetal micromeres (which result from strong asymmetric division at the eight-cell stage and inherit a fate determining polar domain; Angerer and Angerer, 2000; Davidson et al., 1998) and in 32-cell-stage blastomeres at the animal pole ($p = 0.85$ unpaired t test, Figures 4A and 4B). Thus, cell volume, but not cell fate or developmental timing, appears to dictate spindle microtubule growth rate and consequent spindle size in cleaving *P. lividus* embryos, as we found for *C. elegans*. We conclude that this scaling principle operates across a 500-fold change in cell volume and could potentially represent an evolutionarily conserved feature of cleaving embryos.

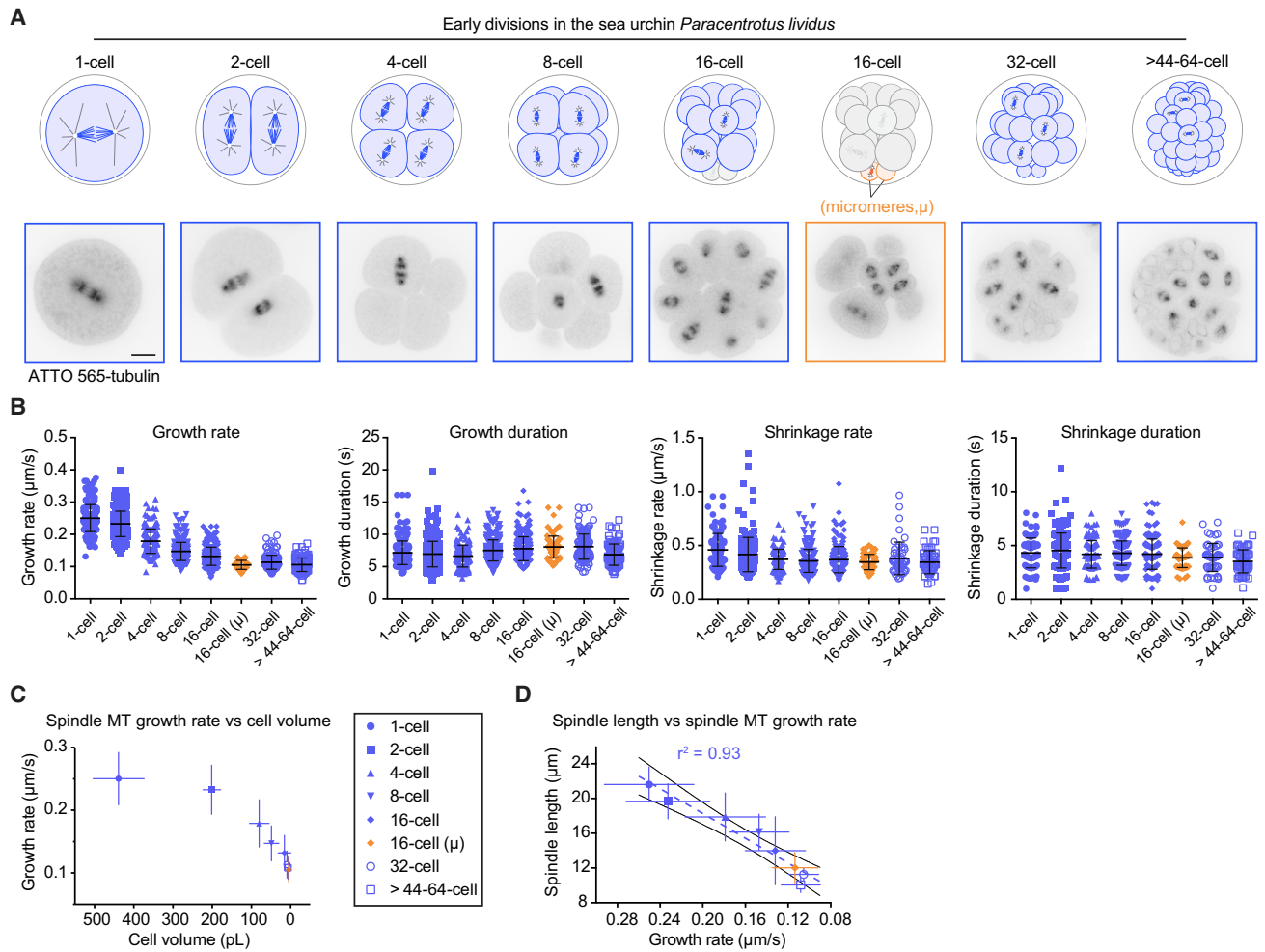


Figure 4. Spindle Length Scales with Cell Volume and Microtubule Growth Rate during Embryo Cleavage in the Sea Urchin *P. lividus*

(A) (Top) Schematic representations of early embryonic divisions of the sea urchin *P. lividus*. Top views schematized for the two- and four-cell stages. All other schemes represent side views with the animal pole at the bottom. At the 16-cell stage, micromeres highlighted in orange. (Bottom) Still frames from confocal live imaging of *P. lividus* embryos microinjected with ATTO 565-labelled pig brain tubulin during the first six embryonic divisions (1- to >44-64-cell stage). Scale bar, 20 μm .

(B) Microtubule dynamics parameters for spindle microtubules plotted at each cleavage stage (1- to >44-64-cell stage). Each dot corresponds to an individual microtubule. Microtubule growth rate significantly varies between stages (one-way ANOVA with Tukey's multiple comparison tests: $p < 0.0001$), except between the 16-cell micromeres, the 32-cell and the >44-64-cell macromeres ($p > 0.5$ in all cases). However, the 16-cell micromeres and the 32-cell macromeres, as well as the 32-cell and the >44-64-cell macromeres differ significantly using a Student's *t*-test ($p = 0.0004$ and 0.0039 respectively), but the 16-cell micromeres do not when compared with the >44-64-cell macromeres ($p = 0.85$). All parameters, including sample size, mean and SD, are listed in Table S2. Horizontal bars, means; error bars, SD; n (cells/stage) ≥ 5 ; n (microtubules/stage) ≥ 55 .

(C) Mean growth rate for spindle microtubules plotted at each cleavage stage (1- to >44-64-cell stage) over the average corresponding cell volume. Error bars, SD.

(D) Mean spindle length plotted at each stage (1- to >44-64-cell stage) over the corresponding average spindle microtubule growth rate. Dotted blue line and black lines represent the linear regression and 95% confidence interval respectively. Pearson correlation coefficient (r^2) is indicated at the top of the graph because $p \leq 0.01$. Error bars, SD.

3D Simulations Reproduce Spindle Length Scaling with Microtubule Growth Rate

To directly test if modulating only microtubule growth rate is sufficient to explain the observed spindle length scaling, we utilized computer simulations. Using the cytoskeletal simulator Cytosim to develop a 3D spindle model, we examined the contribution of the microtubule growth rate on spindle size in a dose-dependent manner *in silico* (www.cytosim.org; Nedelec and Foethke, 2007). We modeled each spindle pole as an aster composed of

a preset number of microtubules that can grow, shrink, and stochastically undergo catastrophe and rescue (Figures 5A and S4, see detailed parameters in Table S3 and STAR Methods). We constructed two asters by distributing a subset of these microtubules evenly and then confining the remaining microtubules within a cone to account for the higher microtubule density directed toward the metaphase plate in *C. elegans* spindles. We represented the metaphase plate itself using a fixed discoid volume in the center of the cell that microtubules cannot enter.

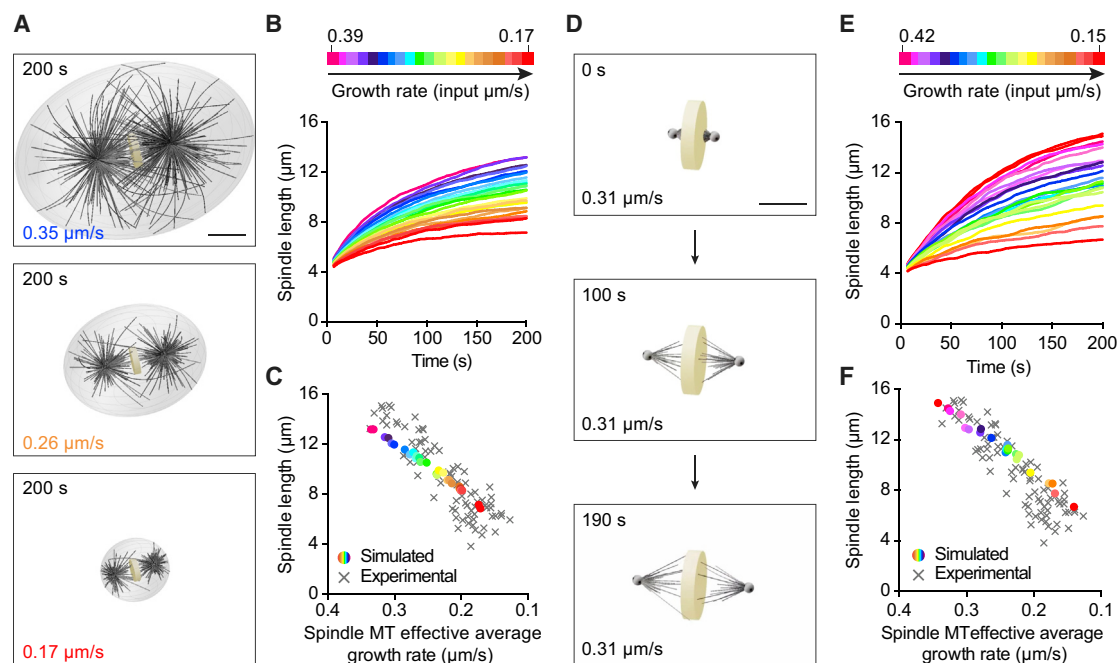


Figure 5. Microtubule Growth Rate Scales Spindle Length in Computational 3D Spindle Models

(A) Spindle length scaling with microtubule growth rate and cell volume. Astral and spindle microtubules and a cell boundary are included in these simulations. Images correspond to steady state spindles obtained after running the simulations for 200 s. The input growth rate indicated at the bottom left of each image. Scale bar, 5 μm .

(B) Simulated spindle length plotted over time at various microtubule growth rates. Color coding of the growth rate indicated at the top, from magenta (0.39 $\mu\text{m/s}$) to red (0.17 $\mu\text{m/s}$).

(C) Simulated steady state (200 s) spindle length plotted over the effective average spindle microtubule growth rate. Growth rate color coded as in (B). Experimental data in gray.

(D) Spindle length scaling with microtubule growth rate. Only spindle microtubules are included in these simulations. Images correspond to a spindle obtained with a microtubule growth rate of 0.31 $\mu\text{m/s}$ at the beginning of the simulation (0 s, top) and after running the simulation for 100 s (middle) and 190 s (bottom). Scale bar, 5 μm .

(E) Simulated spindle length plotted over time at various effective average spindle microtubule growth rates. Color coding of growth rate indicated at the top, from magenta (0.42 $\mu\text{m/s}$) to red (0.15 $\mu\text{m/s}$).

(F) Simulated steady state (200 s) spindle length plotted over spindle microtubule growth rate. Growth rate color coded as in (E). Experimental data in gray.

Using our experimental measurements, we scaled cell volume, metaphase plate thickness, and spindle width linearly with respect to the input growth rate (Table S2B). Microtubules are confined inside the cell volume, and growing plus-ends contacting the cell boundaries can create pushing forces leading to aster centration. Similarly, growing microtubules emanating from the two centrosomes, and contacting the metaphase plate, can generate forces that would push spindle poles apart leading to spindle elongation. To ensure that spindle pole movements would strictly occur through growing microtubules pushing on the cell cortex or on the metaphase plate, we omitted microtubule motors from this model. We analyzed the effects of modulating the microtubule growth rate as a function of cell volume, while keeping the three other microtubule dynamics parameters constant. We tested the physiological range of microtubule growth rates that we measured *in vivo* in *C. elegans* (Table S1). In this first set of simulations, the spindle length (pole-to-pole distance) trended toward a plateau over time for every tested microtubule growth rate (Figure 5B and Video S3). Consistent with our hypothesis, the steady state spindle length decreased concomitantly with the microtubule growth rate (Figure 5C). Overall, the spindle

lengths calculated *in silico* were in good agreement with our experimental measurements (Figure 5C), which confirms that this simple model accurately recapitulated the *in vivo* relationship between microtubule growth rate and spindle length.

Since our experimental data suggested that spindle length correlates with spindle but not astral microtubule dynamics, we tested if a simulation devoid of cell boundary and astral microtubules could reproduce the relationship between spindle length and microtubule growth rate (Figure 5D). With this modified model, we tested a range of microtubule growth rates, while keeping all other parameters constant (Figure 5E and Video S4). We did find that spindle length plateaued over time at a length that increased with microtubule growth rate that yielded similar values and scaling slopes as in our experiments (Figure 5F). This model exhibited the correct multiplicative factor between $\langle L \rangle$ and spindle length, which suggests that this scaling factor only depends on the geometrical dimensions of the system (i.e., cell size and/or dimensions of the metaphase plate) included in the simulation. Together, these findings suggest that modulating spindle microtubule growth rate is sufficient to scale spindle size with cell volume in cleaving embryos.

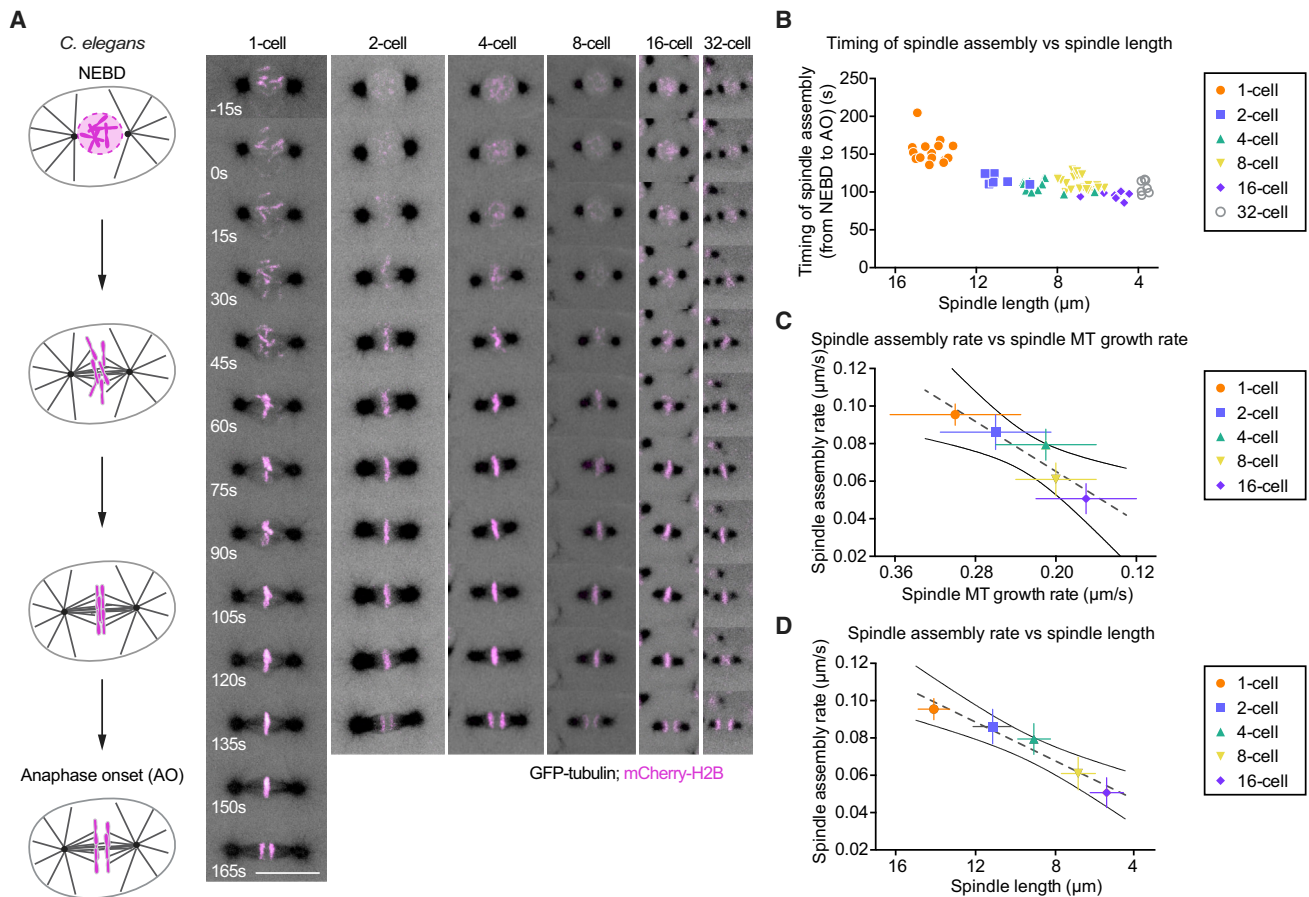


Figure 6. Spindle Assembly Rate Scales with Spindle Microtubule Growth Rate during *C. elegans* Embryo Cleavage

(A) Left: schematics of the spindle assembly process in the *C. elegans* embryo from NEBD (top) to anaphase onset (bottom). Right: still frames from live confocal imaging of *C. elegans* embryos co-expressing mCherry-tagged histone H2B (magenta) and GFP-tagged β -tubulin (gray) during spindle assembly in the first six embryonic divisions (1- to 32-cell stage from left to right). Timings are relative to NEBD. Images correspond to maximum projections of z-stacks. Scale bar, 10 μm . (B) Spindle assembly timing measured from the 1- to the 32-cell stage in *C. elegans* embryos and plotted over the corresponding spindle length at anaphase onset. Each dot corresponds to an individual spindle ($n \geq 9$ per stage).

(C) Mean spindle assembly rate (spindle length/spindle assembly timing) measured at each cleavage stage from the 1- to the 16-cell stage plotted over the corresponding average spindle microtubule growth rate. Dotted and solid gray lines represent the linear regression and 95% confidence interval respectively. Error bars, SD.

(D) Mean spindle assembly rate (spindle length/spindle assembly timing) measured at each cleavage stage from the 1- to the 16-cell stage plotted over the corresponding average spindle length. Dotted and solid gray lines represent the linear regression and 95% confidence interval respectively. Error bars, SD.

Spindle Assembly and Microtubule Growth Rates Proportionally Correlate with Constant Spindle Assembly Timing during Embryo Cleavage

An interesting finding from our 3D simulations was that spindle length reached steady state within a time frame that was independent of microtubule growth rate or final spindle size (Figures 5B, 5E, and S4D). So, our simulations predict that shorter spindles would not assemble faster than longer ones. To test if this occurred *in vivo*, we compared spindle lengths at various stages of *C. elegans* cleavage with the timing of spindle assembly (Figure 6A and Video S5). Since spindle length continuously increases from NEBD to anaphase onset in *C. elegans* embryos, we approximated spindle assembly timing as the duration between NEBD and anaphase onset. We found that the timing of spindle assembly was independent of the initial distance between centrosomes or final spindle length (Figure 6B). Although spindle assembly took

slightly longer in the one-celled zygote than in subsequent stages, spindle assembly durations stayed relatively constant over the first five rounds of embryonic division, despite the progressive decrease in spindle length at each division. We also observed a progressive decrease of the spindle assembly rate, which strongly correlated with the decreasing spindle length and microtubule growth rate across early embryonic divisions (including in the zygote, Figures 6C and 6D). These results agree with the predictions from our simulations. Therefore, the progressive decrease of the microtubule growth rate is sufficient to regulate the constant timing of spindle assembly in cleaving embryos.

DISCUSSION

In summary, we have explored the dynamic properties of microtubules as cell size decreases in early cleaving embryos. Using

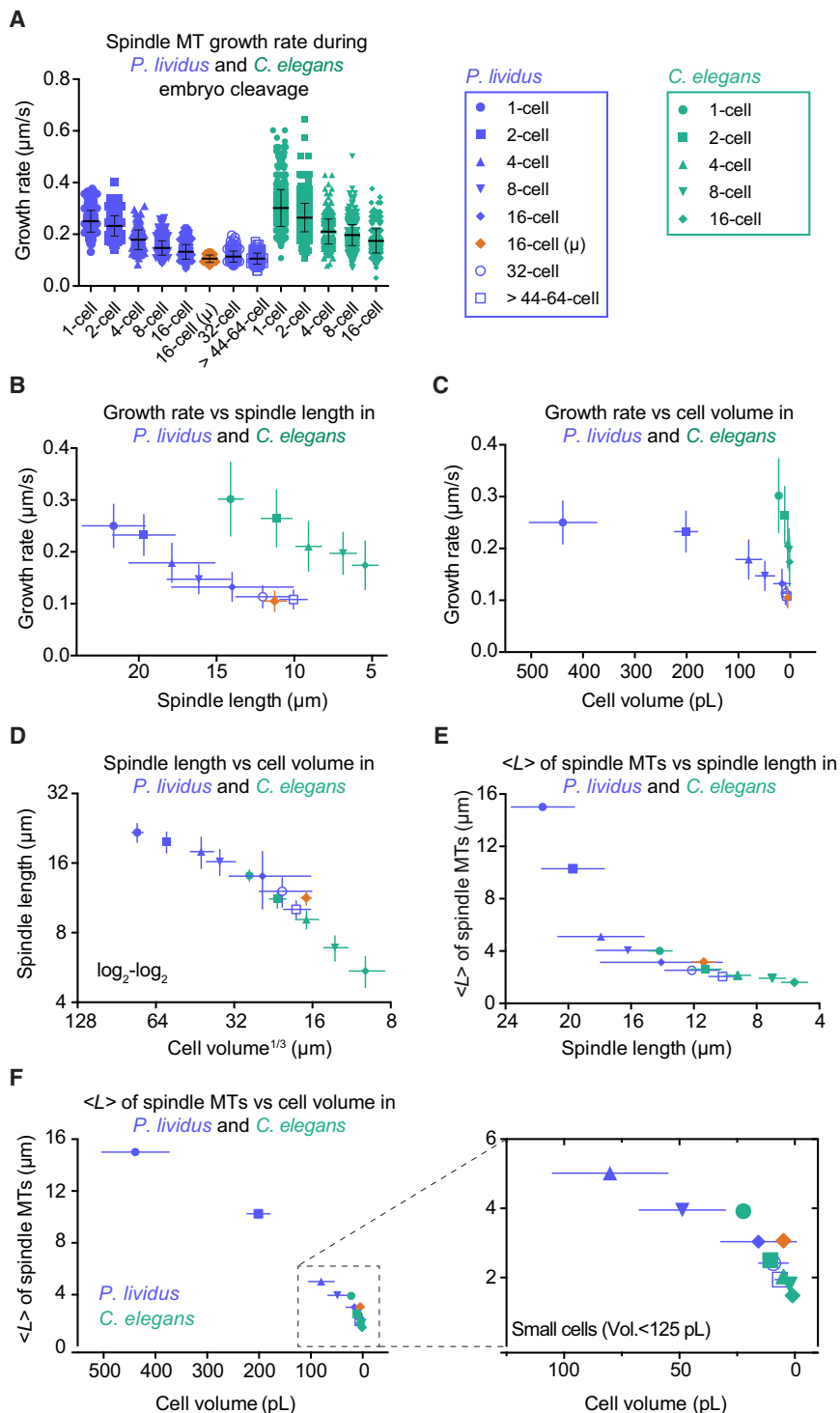


Figure 7. Microtubules and Spindle Length Adaptation to Cell Volume in *P. lividus* and *C. elegans* Embryos

(A) Growth rate for spindle microtubules in *P. lividus* and *C. elegans* (same as Figures 1C and 4B) plotted at each cleavage stage (1- to >44-64-cell stage in *P. lividus* and 1- to 16-cell stage in *C. elegans*). Each dot corresponds to an individual microtubule. Color coding and symbols shown in the right-hand boxes. Horizontal bars, means; error bars, SD; n (cells/stage) ≥ 5; n (microtubules/stage) ≥ 55 in *P. lividus*; n (cells/stage) ≥ 12; n (microtubules/stage) ≥ 288 in *C. elegans*. All parameters, including sample size, mean, and SD, listed in Table S2.

(B) Mean growth rate for spindle microtubules plotted at each cleavage stage over the corresponding average spindle length (bars, SD).

(C) Mean growth rate for spindle microtubules plotted at each cleavage stage over the average corresponding cell volume (bars, SD).

(D) Mean spindle length plotted over the cube root of the average cell volume on a log₂-log₂ scale. Error bars, SD.

(E) Average theoretical microtubule length <L> plotted over the experimentally measured spindle length. Error bars, SD.

(F) (Left) Average theoretical microtubule length <L> plotted over the average cell volume. (Right) Magnification of the graph for the smaller cells (volume < 125 pL). Error bars, SD.

lates the principal features of spindle scaling observed *in vivo*. Our results suggest a simple mechanism to adjust spindle length with varying cell volume, as typically found in early embryonic development. Importantly, our results elucidate how spindle assembly timing is constant among different blastomere sizes in early embryos. This mechanism may be crucial to prevent chromosome segregation defects (Holmfeldt et al., 2006; Lancaster et al., 2013; Mitchison et al., 2015).

Microtubule Dynamics and Cell Volume

Parameters of microtubule dynamics scaled similarly across cleavages in *C. elegans* and *P. lividus* but had different absolute values in the two species. *C. elegans* embryos are ~20 times smaller in volume than sea urchin embryos, but their microtubules grow significantly faster at every stage of cleavage (Figure 7A). These results indicate that microtubule growth rate is not an absolute predictor of spindle length (Figures 7B–7D). In contrast, the average theoretical microtubule length <L>, calculated from the four parameters of dynamic instability, followed a linear and similar trend in both species when plotted against cell volume (Figure 7F). Strikingly, blastomeres of comparable volumes

the nematode *C. elegans* and the sea urchin *P. lividus*, our results establish that the growth rate of spindle microtubules in both species is the primary parameter of dynamic instability that decreases proportionally to cell volume and concomitantly with spindle length. Using an *in silico* 3D spindle model, we demonstrate that decreasing the microtubule growth rate proportionally to cell volume is sufficient to control spindle size and recapitu-

lating the principal features of spindle scaling observed *in vivo*. Our results suggest a simple mechanism to adjust spindle length with varying cell volume, as typically found in early embryonic development. Importantly, our results elucidate how spindle assembly timing is constant among different blastomere sizes in early embryos. This mechanism may be crucial to prevent chromosome segregation defects (Holmfeldt et al., 2006; Lancaster et al., 2013; Mitchison et al., 2015).

displayed very similar values of $\langle L \rangle$ regardless of their species of origin (*C. elegans* two-cell-stage blastomeres and *P. lividus* 32-cell-stage blastomeres display volumes of 10.6 and 9.28 pL respectively and $\langle L \rangle$ of 2.48 and 2.42 μm respectively). $\langle L \rangle$ is a readout of the overall microtubule dynamics, which suggests that microtubule dynamics vary to set an average microtubule length that scales with cell volume. Furthermore, since spindle length is roughly proportional to $\langle L \rangle$, microtubule dynamics are modulated to scale spindle length with cell volume.

However, we note that $\langle L \rangle$ is not equal to the spindle half-length nor do we suggest that spindle length is solely determined by microtubule length. Spindle assembly requires other factors (Dumont and Mitchison, 2009b; Mitchison et al., 2015; Reber and Hyman, 2015; Walczak and Heald, 2008; Waters and Salmon, 1997). We also provide evidence for this premise, as $\langle L \rangle$ did not always scale linearly with spindle length in *P. lividus* (Figure 7E). Specifically, one- and two-cell-stage sea urchin blastomeres deviated from the linear scaling trend followed by other cells, and assembled spindles that were shorter than predicted by values of $\langle L \rangle$. Several non-exclusive causes could account for the discrepancy between $\langle L \rangle$ and spindle length: microtubules may bend, detach from the centrosomes, or be severed (Brangwynne et al., 2006; Crowder et al., 2015; Dumont and Mitchison, 2009a; Gadde and Heald, 2004; Goshima et al., 2005a; Maiato et al., 2004; McBeath and Fujiwara, 1990; Reber and Hyman, 2015; Redemann et al., 2017; Wuhr et al., 2008). We also note that, theoretically, the microtubule growth rate should regulate microtubule mass within the spindle rather than the spindle length itself (Mitchison et al., 2015; Reber et al., 2013). So, when microtubule length and spindle length scale linearly together, total microtubule mass in the spindle may also scale. But in larger blastomeres, an excess in microtubule mass, due to the increased growth rate, could be compensated either by an increase in density or by a change in spindle width rather than length. Consistent with the later possibility and previous observations done in other species (Crowder et al., 2015; Hara and Kimura, 2013), we observed a significant change in the spindle length to width ratio and in the centrosome radius in *P. lividus* among cleavages, which correlated with proportionally wider spindle poles at earlier stages (Figure S3H and Table S2).

Microtubule Dynamics and Spindle Length

Our analysis revealed that the microtubule growth rate and spindle length decrease concomitantly and sub-proportionally to cell volume across reductive divisions in early *C. elegans* and *P. lividus* embryos. This contrasts with previous work comparing stage 3 and 8 *Xenopus* embryo extracts. These studies found no major variation in the microtubule growth rate, but a 3-fold increase in the microtubule catastrophe frequency correlated with smaller spindles (Wilbur and Heald, 2013). It is possible that different mechanisms may exist across phylogeny that would produce similar effects on spindle length, thus reflecting evolutionary diversity. However, we note that *Xenopus* blastomeres (at both stages 3 and 8) are significantly larger than *C. elegans* or *P. lividus* embryos, which could favor one spindle scaling mechanism over the other. Moreover, stage 8 blastomeres utilize a linear scaling regime, where spindle length scales linearly with cell size, while stage 3 blastomeres remain in the

“large-cell” regime, in which spindle length reaches an upper limit that is independent of cell size (Wilbur and Heald, 2013; Wuhr et al., 2008). The difference in the catastrophe frequency between stage 3 and 8 could thus be related to the transitioning from large-cell to linear scaling regime rather than reflecting a cell size-dependent spindle scaling mechanism. Finally, results obtained with *Xenopus* egg extracts could also reflect the removal of membrane confinements. In the large-cell regime, spindle length is controlled through spindle intrinsic mechanisms such as autocatalytic microtubule nucleation (Decker et al., 2018; Ishihara et al., 2016; Mitchison et al., 2015). It is therefore possible that in the “small-cell” regime, modulation of the microtubule nucleation rate similarly contributes to spindle length scaling. However, our results demonstrate that regulation of the microtubule growth rate is sufficient to account for spindle length adaptation to cell volume in small cells.

We still must determine the specific factors that control microtubule growth rate with respect to cell volume. The limiting component hypothesis proposes that one or several factors critical for spindle assembly have a limited supply, so their absolute quantity per cell diminishes upon embryo cleavage (Mitchison et al., 2015; Reber and Goehring, 2015). Tubulin is the most obvious candidate, as its concentration does determine the rate of microtubule elongation *in vitro* (Walker et al., 1988). However, several *in vitro* and *in vivo* studies argue against tubulin being the sole limiting component. In *Xenopus* egg extracts or in the presence of crowding agents *in vitro*, the growth rate of microtubules is not linearly dependent on the available tubulin concentration (Parsons and Salmon, 1997; Wicczorek et al., 2013), as robust spindle length scaling occurred in lipid droplets even after artificially increasing the amount of tubulin (Good et al., 2013). In sea urchin embryos, a 5-fold excess of tubulin is present in a soluble non-polymerized form and can be artificially mobilized into the spindle upon treatment with crowding agents, indicating that tubulin itself is not limiting in this system (Inoue and Sato, 1967; Raff et al., 1975; Raff and Kaumeyer, 1973; Rebhun et al., 1975). Quantitative western blotting allowed us to estimate the tubulin concentration to approximately 22 μM in *C. elegans* embryos, which is similar to *Xenopus* embryos (Figure S5 and STAR Methods) (Belmont et al., 1990). Based on a recent study providing the first complete electron tomographic reconstruction of the mitotic spindle in the *C. elegans* zygote (Redemann et al., 2017), we estimated that the total amount of tubulin heterodimers should be sufficient to assemble two to three zygotic mitotic spindles (see STAR Methods). Thus, tubulin seems unlikely to be the only limiting factor for spindle length scaling. Another possibility is that specific MAPs that regulate microtubule growth rate are also limiting. Consistent with this, we found that reducing levels of the CLS-2 protein in *C. elegans* zygotes modulated microtubule growth rate and spindle length proportionally. Furthermore, by performing a temporal dilution experiment through progressive RNAi depletion of CLS-2 in the *C. elegans* one-cell embryo, we found that spindle length was proportional to CLS-2 protein level (Figures 8A–8E). Together, these results are in agreement with the limiting amount of one or several MAPs restricting microtubule dynamics and spindle length in early embryos (Figures 8F and 8G). To explain how the absolute amount of MAPs could become limiting and thus control spindle length scaling, we favor a model where a

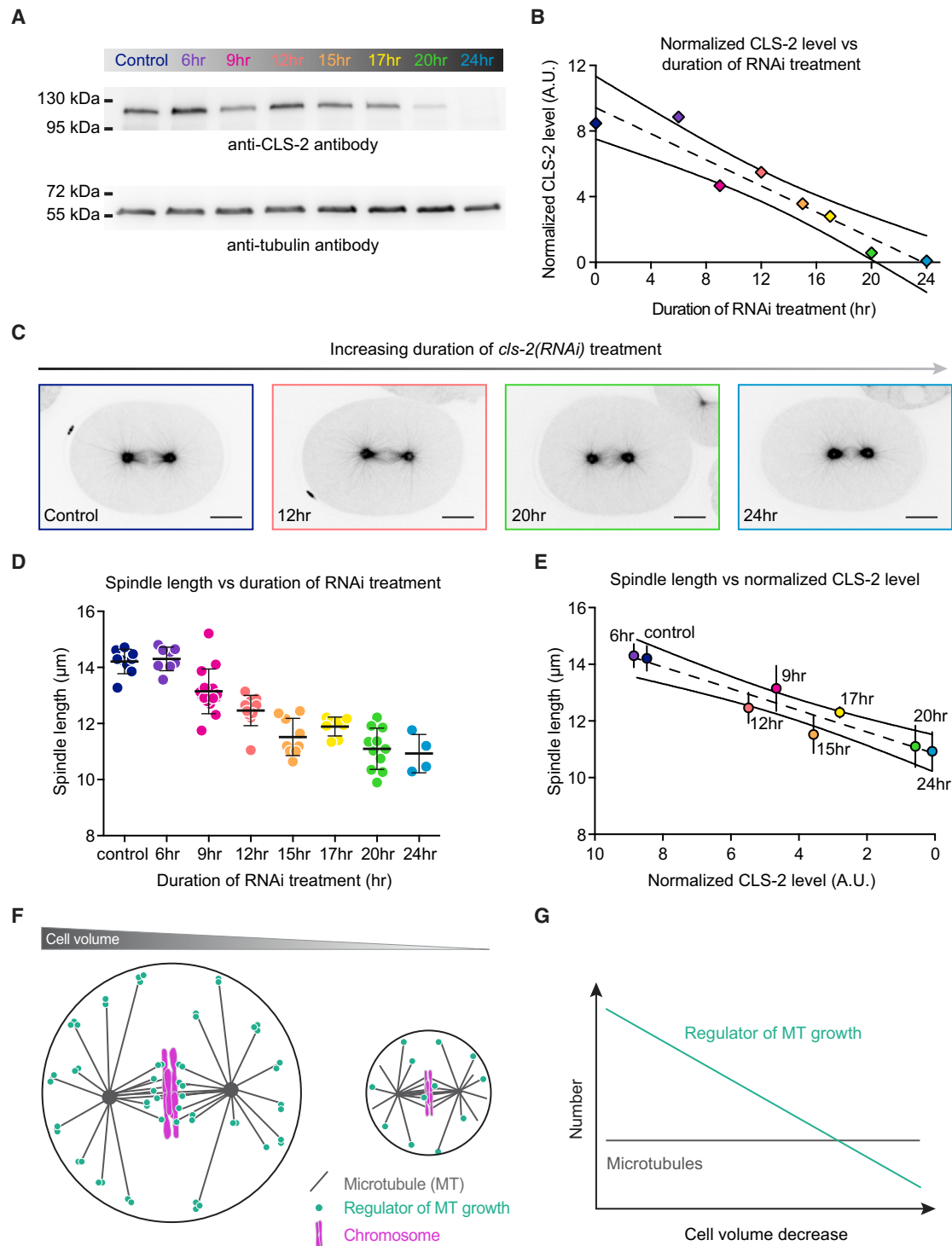


Figure 8. A Limiting Component(s) Model for Microtubule Growth Rate and Spindle Length Scaling

(A) (Top) Western blot using an anti-CLS-2 antibody (C2a14) on whole control worm extract or extracts treated with *cls-2*(RNAi) for increasing times (from 6 to 24 hr). Duration of the RNAi treatment is indicated above each lane. (Bottom) Western blot using an anti- α -tubulin antibody (DM1 α) was used as a loading control. (B) Normalized CLS-2 level plotted over the corresponding duration of RNAi treatment. Dotted and solid black lines represent the linear regression and 95% confidence interval respectively. The color code corresponds to (A).

(C) Still images of one-cell *C. elegans* embryos in metaphase expressing GFP-tagged β -tubulin after progressive depletion of the CLS-2 protein. The duration of the RNAi treatment is color coded as in (A) and is indicated at the bottom right corner of each image. Scale bar, 10 μ m.

(legend continued on next page)

progressive mismatch is established across successive divisions between the number of available MAPs and the number of spindle microtubules (Figure 8G). The CLS-2 and TPXL-1 proteins are good candidate factors for acting as limiting components (Greenan et al., 2010). However, MAPs influence several microtubule dynamics parameters, which complicates the identification of the key factor(s) that coordinate spindle length with cell size in early embryos *in vivo* (Bowne-Anderson et al., 2015). We must also point out that the limiting component model cannot account for the spindle scaling mismatch observed between oocytes and zygotes of most species, and that cell volume is not an absolute predictor of spindle length. Indeed, although they assemble in an identical volume of the same cytoplasm, oocyte spindles are usually smaller than their zygotic counterparts. Meiotic-specific and volume-independent mechanisms can usually account for the discrepancy between cell volume and spindle length in oocytes (Clandinin and Mains, 1993; Clark-Maguire and Mains, 1994; Lu et al., 2004; Srayko et al., 2000).

Microtubule Dynamics and Spindle Assembly Rate

In addition to spindle size, we also found that the rate of spindle assembly (spindle length/time of assembly) scaled with cell size in *C. elegans* embryos. Our simulations combined with our *in vivo* measurements suggest that this scalability occurs through the proportional relationship between microtubule growth rate and steady state spindle length. This property could be key in early embryos that undergo rapid cell divisions with a weak spindle assembly checkpoint (Encalada et al., 2005). Indeed, *C. elegans* embryos respond to unattached kinetochores by inducing a small delay in mitosis but do not arrest their cell cycle progression. In this context, adapting the microtubule growth rate to the final spindle length would ensure efficient chromosome biorientation and avoid sister chromatid mis-segregation. Fast-assembling microtubules in large blastomeres reach further and search more space to ensure timely chromosome capture during the short mitotic time window. As cleavage progresses and spindle length decreases, slowing down microtubule assembly may negate the simultaneous connection of individual kinetochores to both spindle poles, which would promote merotelic and gross chromosome mis-segregation if not corrected. From these observations, we envision that decreasing the microtubule growth rate permits the embryo to not only scale down its spindles but also globally optimize chromosome segregation during embryogenesis. Previous work in *C. elegans*

embryos demonstrated that the rate of spindle elongation during anaphase (Hara and Kimura, 2009) and the rate of cortical ring constriction during cytokinesis (Carvalho et al., 2009) also decreased as cell volume decreased, which makes the time needed for anaphase spindle elongation and for cytokinetic ring constriction independent of cell size. Future studies should examine whether the rates of other cell division processes also exhibit intrinsic scalability and whether this is a general principle that dictates how cell biological processes scale with cell size.

STAR★METHODS

Detailed methods are provided in the online version of this paper and include the following:

- KEY RESOURCES TABLE
- CONTACT FOR REAGENT AND RESOURCE SHARING
- EXPERIMENTAL MODEL AND SUBJECT DETAILS
 - *Caenorhabditis elegans*
 - *Paracentrotus lividus*
- METHOD DETAILS
 - RNA-mediated Interference (RNAi) and Drug Treatment in *C. elegans*
 - Estimation of the Tubulin Heterodimer Concentration in the *C. elegans* Embryo by Quantitative Western Blot
 - Estimation of CLS-2 Protein Level Following RNAi-mediated Depletion in the *C. elegans* Embryo by Quantitative Western Blot
 - Tubulin Preparation and Fluorescent Labeling
 - Two-photon Live Microscopy of *C. elegans* Embryos
 - Spinning-disc Live Microscopy of *C. elegans* Embryos
 - Injection and Imaging of Sea Urchin Embryos
 - Immunostaining of Sea Urchin Embryos
 - Image Analysis
 - Analysis of Microtubule Dynamics
 - Cytosim Simulations
- QUANTIFICATION AND STATISTICAL ANALYSIS
- DATA AND SOFTWARE AVAILABILITY
 - Data Availability

SUPPLEMENTAL INFORMATION

Supplemental Information includes five figures, three tables, and five videos and can be found with this article online at <https://doi.org/10.1016/j.devcel.2018.04.022>.

(D) Spindle length in one-cell *C. elegans* embryos in metaphase after progressive depletion of the CLS-2 protein plotted over the corresponding duration of RNAi treatment. The color code corresponds to (A). Error bars, SD.

(E) Mean spindle length plotted over the corresponding level of CLS-2 protein. Dotted and solid black lines represent the linear regression and 95% confidence interval, respectively. Error bars, SD.

(F) A limiting component model explains microtubule growth rate and spindle length scaling with respect to cell volume (Decker et al., 2011; Goehring and Hyman, 2012; Good et al., 2013; Hazel et al., 2013; Mitchison et al., 2015; Schmoller and Skotheim, 2015). In this model, one or several positive regulators of spindle microtubule growth (such as CLS-2) bind to microtubule (+) ends. The microtubule growth rate depends on the number of (+)-end-bound regulators. Across successive divisions, the concentration of regulators remains constant but the absolute number of regulator molecules decreases with cell volume. If in parallel, the number of spindle microtubules remains constant or decreases in a sub-proportional manner across divisions, the number of regulators becomes progressively limiting relative to the number of microtubule (+) ends. The limited number of regulators in turn restricts spindle microtubule growth rate.

(G) Schematic evolution of spindle microtubule and regulator number as cell size decreases. As cells get smaller, microtubules are shorter but their number remains constant (or decreases slower than the number of regulators). In contrast, the absolute number of regulator molecules is directly proportional to cell volume. If the regulator stimulates microtubule growth (such as CLS-2), microtubule growth rate will progressively decrease as cell volume decreases across successive divisions.

ACKNOWLEDGMENTS

We thank all members of the Dumont lab for support and advice, and Kimberley Laband for critical reading of the manuscript. We are grateful to Patricia Moussounda for providing technical support. We thank Life Science Editors for editing assistance. We acknowledge the ImagoSeine core facility of the Institut Jacques Monod, member of IBISA and France-BioImaging (ANR-10-INBS-04) infrastructures. We thank Nicolas Tissot (ImagoSeine) for his help with the two-photon microscopy. We thank Julie Ahringer (The Gurdon Institute, University of Cambridge, UK) for the generous gift of the JA1559 *C. elegans* strain and George Von Dassow (University of Oregon) for providing recombinant 3xmCherry-EMTB. Some strains were provided by the CGC, which is funded by NIH Office of Research Infrastructure Programs (P40 OD010440). EMBRC-France is supported by the Investments of the Future program under reference ANR-10-INBS-02. We thank Pascal Romans (UPMC, Banyuls-sur-Mer, France) and Anaëlle Pierre (IJM, Paris, France) for technical assistance with sea urchins. We thank Dmitry Ershov (IJM, Paris, France) for his help with MATLAB. We are grateful to Jean-Claude Labbe (IRIC) for initial technical support and discussions. B.L. was originally supported by a post-doctoral fellowship from the Fondation pour la Recherche Médicale (FRM ARF20140129055). J.S. and N.M. are supported by the European Research Council (CoG Forcaster N° 647073). This work was supported by CNRS and University Paris Diderot and by grants from the Agence Nationale pour la Recherche (ANR-16-CE13-0020-01), the Mairie de Paris (Emergence), and the Fondation pour la Recherche Médicale (FRM DEQ20160334869) to J.D.

AUTHOR CONTRIBUTIONS

B.L. and J.D. conceived the project with input from all authors. B.L. performed all of the experiments, except those specifically attributed to other authors. L.P. performed the clasto-Lactacystin β -lactone experiments and analysis. J.S. performed the sea urchin microinjection experiments with input from N.M. G.M. performed the *C. elegans* microinjection experiments. M.S. and J.C.C. generated some strains used in this study. A.-M.L. performed some image analyses. J.C.C., P.S.M., and A.S.M. provided input on conceptualization and initial resources. B.L., J.D., G.L., and F.N. conceived the *in silico* model, and G.L. and F.N. extended Cytosim to implement it. G.L. performed the computer simulations under F.N.'s supervision. B.L. and J.D. made the figures and wrote the manuscript with input from all authors.

DECLARATION OF INTERESTS

The authors declare no competing interests.

Received: December 14, 2017

Revised: March 22, 2018

Accepted: April 24, 2018

Published: May 21, 2018

REFERENCES

- Agrell, I. (1956). A mitotic gradient as the cause of the early differentiation in the sea urchin embryo. In *Zoological Papers in Honour of B. Hanström*, K.G. Wingstrand, ed. (Berlingska Boktryckeriet), pp. 27–34.
- Andersen, S.S. (2000). Spindle assembly and the art of regulating microtubule dynamics by MAPs and Stathmin/Op18. *Trends Cell Biol.* 10, 261–267.
- Andersen, S.S., Ashford, A.J., Tournébeise, R., Gavet, O., Sobel, A., Hyman, A.A., and Karsenti, E. (1997). Mitotic chromatin regulates phosphorylation of Stathmin/Op18. *Nature* 389, 640–643.
- Angerer, L.M., and Angerer, R.C. (2000). Animal-vegetal axis patterning mechanisms in the early sea urchin embryo. *Dev. Biol.* 218, 1–12.
- Belmont, L.D., Hyman, A.A., Sawin, K.E., and Mitchison, T.J. (1990). Real-time visualization of cell cycle-dependent changes in microtubule dynamics in cytoplasmic extracts. *Cell* 62, 579–589.
- Bowne-Anderson, H., Hibbel, A., and Howard, J. (2015). Regulation of microtubule growth and catastrophe: unifying theory and experiment. *Trends Cell Biol.* 25, 769–779.
- Brangwynne, C.P., MacKintosh, F.C., Kumar, S., Geisse, N.A., Talbot, J., Mahadevan, L., Parker, K.K., Ingber, D.E., and Weitz, D.A. (2006). Microtubules can bear enhanced compressive loads in living cells because of lateral reinforcement. *J. Cell Biol.* 173, 733–741.
- Brenner, S. (1974). The genetics of *Caenorhabditis elegans*. *Genetics* 77, 71–94.
- Brown, K.S., Blower, M.D., Maresca, T.J., Grammer, T.C., Harland, R.M., and Heald, R. (2007). *Xenopus tropicalis* egg extracts provide insight into scaling of the mitotic spindle. *J. Cell Biol.* 176, 765–770.
- Canman, J.C., Lewellyn, L., Laband, K., Smerdon, S.J., Desai, A., Bowerman, B., and Oegema, K. (2008). Inhibition of Rac by the GAP activity of centralspindlin is essential for cytokinesis. *Science* 322, 1543–1546.
- Carvalho, A., Desai, A., and Oegema, K. (2009). Structural memory in the contractile ring makes the duration of cytokinesis independent of cell size. *Cell* 137, 926–937.
- Castoldi, M., and Popov, A.V. (2003). Purification of brain tubulin through two cycles of polymerization-depolymerization in a high-molarity buffer. *Protein Expr. Purif.* 32, 83–88.
- Chalfie, M., and Thomson, J.N. (1982). Structural and functional diversity in the neuronal microtubules of *Caenorhabditis elegans*. *J. Cell Biol.* 93, 15–23.
- Chan, Y.H., and Marshall, W.F. (2010). Scaling properties of cell and organelle size. *Organogenesis* 6, 88–96.
- Chan, Y.H., and Marshall, W.F. (2012). How cells know the size of their organelles. *Science* 337, 1186–1189.
- Cheeseman, I.M., MacLeod, I., Yates, J.R., 3rd, Oegema, K., and Desai, A. (2005). The CENP-F-like proteins HCP-1 and HCP-2 target CLASP to kinetochores to mediate chromosome segregation. *Curr. Biol.* 15, 771–777.
- Clandinin, T.R., and Mains, P.E. (1993). Genetic studies of mei-1 gene activity during the transition from meiosis to mitosis in *Caenorhabditis elegans*. *Genetics* 134, 199–210.
- Clark-Maguire, S., and Mains, P.E. (1994). Localization of the mei-1 gene product of *Caenorhabditis elegans*, a meiotic-specific spindle component. *J. Cell Biol.* 126, 199–209.
- Crowder, M.E., Strzelecka, M., Wilbur, J.D., Good, M.C., von Dassow, G., and Heald, R. (2015). A comparative analysis of spindle morphometrics across metazoans. *Curr. Biol.* 25, 1542–1550.
- Davidson, E.H., Cameron, R.A., and Ransick, A. (1998). Specification of cell fate in the sea urchin embryo: summary and some proposed mechanisms. *Development* 125, 3269–3290.
- Davies, T., Jordan, S.N., Chand, V., Sees, J.A., Laband, K., Carvalho, A.X., Shirasu-Hiza, M., Kovar, D.R., Dumont, J., and Canman, J.C. (2014). High-resolution temporal analysis reveals a functional timeline for the molecular regulation of cytokinesis. *Dev. Cell* 30, 209–223.
- Decker, F., Oriola, D., Dalton, B., and Brugués, J. (2018). Autocatalytic microtubule nucleation determines the size and mass of *Xenopus laevis* egg extract spindles. *Elife* 7, <https://doi.org/10.7554/eLife.31149>.
- Decker, M., Jaensch, S., Pozniakovskiy, A., Zinke, A., O'Connell, K.F., Zachariae, W., Myers, E., and Hyman, A.A. (2011). Limiting amounts of centrosome material set centrosome size in *C. elegans* embryos. *Curr. Biol.* 21, 1259–1267.
- Desai, A., and Mitchison, T.J. (1997). Microtubule polymerization dynamics. *Annu. Rev. Cell Dev. Biol.* 13, 83–117.
- Dogterom, M., and Yurke, B. (1997). Measurement of the force-velocity relation for growing microtubules. *Science* 278, 856–860.
- Dumont, S., and Mitchison, T.J. (2009a). Compression regulates mitotic spindle length by a mechanochemical switch at the poles. *Curr. Biol.* 19, 1086–1095.
- Dumont, S., and Mitchison, T.J. (2009b). Force and length in the mitotic spindle. *Curr. Biol.* 19, R749–R761.

- Encalada, S.E., Willis, J., Lyczak, R., and Bowerman, B. (2005). A spindle checkpoint functions during mitosis in the early *Caenorhabditis elegans* embryo. *Mol. Biol. Cell* 16, 1056–1070.
- Espiritu, E.B., Krueger, L.E., Ye, A., and Rose, L.S. (2012). CLASPs function redundantly to regulate astral microtubules in the *C. elegans* embryo. *Dev. Biol.* 368, 242–254.
- Faire, K., Waterman-Storer, C.M., Gruber, D., Masson, D., Salmon, E.D., and Bulinski, J.C. (1999). E-MAP-115 (ensconsin) associates dynamically with microtubules in vivo and is not a physiological modulator of microtubule dynamics. *J. Cell Sci.* 112 (Pt 23), 4243–4255.
- Fire, A., Xu, S., Montgomery, M.K., Kostas, S.A., Driver, S.E., and Mello, C.C. (1998). Potent and specific genetic interference by double-stranded RNA in *Caenorhabditis elegans*. *Nature* 391, 806–811.
- Foe, V.E., and von Dassow, G. (2008). Stable and dynamic microtubules coordinately shape the myosin activation zone during cytokinetic furrow formation. *J. Cell Biol.* 183, 457–470.
- Frokjaer-Jensen, C., Davis, M.W., Hopkins, C.E., Newman, B.J., Thummel, J.M., Olesen, S.P., Grunnet, M., and Jorgensen, E.M. (2008). Single-copy insertion of transgenes in *Caenorhabditis elegans*. *Nat. Genet.* 40, 1375–1383.
- Gadde, S., and Heald, R. (2004). Mechanisms and molecules of the mitotic spindle. *Curr. Biol.* 14, R797–R805.
- Goehring, N.W., and Hyman, A.A. (2012). Organelle growth control through limiting pools of cytoplasmic components. *Curr. Biol.* 22, R330–R339.
- Good, M.C., Vahey, M.D., Skandarajah, A., Fletcher, D.A., and Heald, R. (2013). Cytoplasmic volume modulates spindle size during embryogenesis. *Science* 342, 856–860.
- Goshima, G., Nedelec, F., and Vale, R.D. (2005a). Mechanisms for focusing mitotic spindle poles by minus end-directed motor proteins. *J. Cell Biol.* 171, 229–240.
- Goshima, G., Wollman, R., Stuurman, N., Scholey, J.M., and Vale, R.D. (2005b). Length control of the metaphase spindle. *Curr. Biol.* 15, 1979–1988.
- Greenan, G., Brangwynne, C.P., Jaensch, S., Gharakhani, J., Julicher, F., and Hyman, A.A. (2010). Centrosome size sets mitotic spindle length in *Caenorhabditis elegans* embryos. *Curr. Biol.* 20, 353–358.
- Hara, Y., and Kimura, A. (2009). Cell-size-dependent spindle elongation in the *Caenorhabditis elegans* early embryo. *Curr. Biol.* 19, 1549–1554.
- Hara, Y., and Kimura, A. (2013). An allometric relationship between mitotic spindle width, spindle length, and ploidy in *Caenorhabditis elegans* embryos. *Mol. Biol. Cell* 24, 1411–1419.
- Hazel, J., Krutkramelis, K., Mooney, P., Tomschik, M., Gerow, K., Oakey, J., and Gatlin, J.C. (2013). Changes in cytoplasmic volume are sufficient to drive spindle scaling. *Science* 342, 853–856.
- Holmfeldt, P., Brannstrom, K., Stenmark, S., and Gullberg, M. (2006). Aneugenic activity of Op18/stathmin is potentiated by the somatic Q18→E mutation in leukemic cells. *Mol. Biol. Cell* 17, 2921–2930.
- Hyman, A.A. (1991). Preparation of marked microtubules for the assay of the polarity of microtubule-based motors by fluorescence. *J. Cell Sci. Suppl.* 14, 125–127.
- Inoue, S., and Sato, H. (1967). Cell motility by labile association of molecules. The nature of mitotic spindle fibers and their role in chromosome movement. *J. Gen. Physiol.* 50 (Suppl.), 259–292.
- Ishihara, K., Korolev, K.S., and Mitchison, T.J. (2016). Physical basis of large microtubule aster growth. *Elife* 5, <https://doi.org/10.7554/eLife.19145>.
- Kamath, R.S., Martinez-Campos, M., Zipperlen, P., Fraser, A.G., and Ahringer, J. (2001). Effectiveness of specific RNA-mediated interference through ingested double-stranded RNA in *Caenorhabditis elegans*. *Genome Biol.* 2, 1–10, RESEARCH0002.
- Kirschner, M., and Mitchison, T. (1986). Beyond self-assembly: from microtubules to morphogenesis. *Cell* 45, 329–342.
- Komarova, Y.A., Vorobjev, I.A., and Borisy, G.G. (2002). Life cycle of MTs: persistent growth in the cell interior, asymmetric transition frequencies and effects of the cell boundary. *J. Cell Sci.* 115, 3527–3539.
- Labbe, J.C., McCarthy, E.K., and Goldstein, B. (2004). The forces that position a mitotic spindle asymmetrically are tethered until after the time of spindle assembly. *J. Cell Biol.* 167, 245–256.
- Lacroix, B., and Maddox, A.S. (2014). Microtubule dynamics followed through cell differentiation and tissue biogenesis in *C. elegans*. *Worm* 3, e967611.
- Lacroix, B., Ryan, J., Dumont, J., Maddox, P.S., and Maddox, A.S. (2016). Identification of microtubule growth deceleration and its regulation by conserved and novel proteins. *Mol. Biol. Cell* 27, 1479–1487.
- Lancaster, O.M., Le Berre, M., Dimitracopoulos, A., Bonazzi, D., Zlotek-Zlotkiewicz, E., Picone, R., Duke, T., Piel, M., and Baum, B. (2013). Mitotic rounding alters cell geometry to ensure efficient bipolar spindle formation. *Dev. Cell* 25, 270–283.
- Letort, G., Nedelec, F., Blanchoin, L., and Thery, M. (2016). Centrosome centering and decentering by microtubule network rearrangement. *Mol. Biol. Cell* 27, 2833–2843.
- Levy, D.L., and Heald, R. (2012). Mechanisms of intracellular scaling. *Annu. Rev. Cell Dev. Biol.* 28, 113–135.
- Loughlin, R., Wilbur, J.D., McNally, F.J., Nedelec, F.J., and Heald, R. (2011). Katanin contributes to interspecies spindle length scaling in *Xenopus*. *Cell* 147, 1397–1407.
- Lu, C., Srayko, M., and Mains, P.E. (2004). The *Caenorhabditis elegans* microtubule-severing complex MEI-1/MEI-2 katanin interacts differently with two superficially redundant beta-tubulin isoforms. *Mol. Biol. Cell* 15, 142–150.
- Maddox, P., Straight, A., Coughlin, P., Mitchison, T.J., and Salmon, E.D. (2003). Direct observation of microtubule dynamics at kinetochores in *Xenopus* extract spindles: implications for spindle mechanics. *J. Cell Biol.* 162, 377–382.
- Maiato, H., Rieder, C.L., and Khodjakov, A. (2004). Kinetochore-driven formation of kinetochore fibers contributes to spindle assembly during animal mitosis. *J. Cell Biol.* 167, 831–840.
- Marshall, W.F. (2015a). How cells measure length on subcellular scales. *Trends Cell Biol.* 25, 760–768.
- Marshall, W.F. (2015b). Subcellular size. *Cold Spring Harb. Perspect. Biol.* 7, <https://doi.org/10.1101/cshperspect.a019059>.
- Maton, G., Edwards, F., Lacroix, B., Stefanutti, M., Laband, K., Lieury, T., Kim, T., Espeut, J., Canman, J.C., and Dumont, J. (2015). Kinetochore components are required for central spindle assembly. *Nat. Cell Biol.* 17, 697–705.
- McBeath, E., and Fujiwara, K. (1990). Microtubule detachment from the microtubule-organizing center as a key event in the complete turnover of microtubules in cells. *Eur. J. Cell Biol.* 52, 1–16.
- Mitchison, T., and Kirschner, M. (1984). Dynamic instability of microtubule growth. *Nature* 312, 237–242.
- Mitchison, T.J., Ishihara, K., Nguyen, P., and Wuhr, M. (2015). Size scaling of microtubule assemblies in early *Xenopus* embryos. *Cold Spring Harb. Perspect. Biol.* 7, a019182.
- Muller-Reichert, T., Greenan, G., O'Toole, E., and Srayko, M. (2010). The elegans of spindle assembly. *Cell Mol. Life Sci.* 67, 2195–2213.
- Nance, J. (2005). PAR proteins and the establishment of cell polarity during *C. elegans* development. *Bioessays* 27, 126–135.
- Nedelec, F., and Foethke, D. (2007). Collective Langevin dynamics of flexible cytoskeletal fibers. *New J. Phys.* 9, 427.
- Nogales, E., Wolf, S.G., and Downing, K.H. (1998). Structure of the alpha beta tubulin dimer by electron crystallography. *Nature* 391, 199–203.
- O'Farrell, P.H., Stumpff, J., and Su, T.T. (2004). Embryonic cleavage cycles: how is a mouse like a fly? *Curr. Biol.* 14, R35–R45.
- Parisi, E., Filosa, S., De Petrocellis, B., and Monroy, A. (1978). The pattern of cell division in the early development of the sea urchin. *Paracentrotus lividus*. *Dev. Biol.* 65, 38–49.
- Parsons, S.F., and Salmon, E.D. (1997). Microtubule assembly in clarified *Xenopus* egg extracts. *Cell Motil. Cytoskeleton* 36, 1–11.
- Picone, R., Ren, X., Ivanovitch, K.D., Clarke, J.D., McKendry, R.A., and Baum, B. (2010). A polarised population of dynamic microtubules mediates homeostatic length control in animal cells. *PLoS Biol.* 8, e1000542.

- Raff, R.A., Brandis, J.W., Green, L.H., Kaumeyer, J.F., and Raff, E.C. (1975). Microtubule protein pools in early development. *Ann. N. Y. Acad. Sci.* 253, 304–317.
- Raff, R.A., and Kaumeyer, J.F. (1973). Soluble microtubule proteins of the sea urchin embryo: partial characterization of the proteins and behavior of the pool in early development. *Dev. Biol.* 32, 309–320.
- Reber, S., and Goehring, N.W. (2015). Intracellular scaling mechanisms. *Cold Spring Harb. Perspect. Biol.* 7, <https://doi.org/10.1101/cshperspect.a019067>.
- Reber, S., and Hyman, A.A. (2015). Emergent properties of the metaphase spindle. *Cold Spring Harb. Perspect. Biol.* 7, a015784.
- Reber, S.B., Baumgart, J., Widlund, P.O., Pozniakovsky, A., Howard, J., Hyman, A.A., and Julicher, F. (2013). XMAP215 activity sets spindle length by controlling the total mass of spindle microtubules. *Nat. Cell Biol.* 15, 1116–1122.
- Rebhun, L.I., Jemioło, D., Ivy, N., Mellon, M., and Nath, J. (1975). Regulation of the in vivo mitotic apparatus by glycols and metabolic inhibitors. *Ann. N. Y. Acad. Sci.* 253, 362–377.
- Redemann, S., Baumgart, J., Lindow, N., Shelley, M., Nazockdast, E., Kratz, A., Prohaska, S., Bragues, J., Furthauer, S., and Müller-Reichert, T. (2017). *C. elegans* chromosomes connect to centrosomes by anchoring into the spindle network. *Nat. Commun.* 8, 15288.
- Rose, L.S., and Kemphues, K.J. (1998). Early patterning of the *C. elegans* embryo. *Annu. Rev. Genet.* 32, 521–545.
- Schmoller, K.M., and Skotheim, J.M. (2015). The biosynthetic basis of cell size control. *Trends Cell Biol.* 25, 793–802.
- Sonnichsen, B., Koski, L.B., Walsh, A., Marschall, P., Neumann, B., Brehm, M., Alleaume, A.M., Artelt, J., Bettencourt, P., Cassin, E., et al. (2005). Full-genome RNAi profiling of early embryogenesis in *Caenorhabditis elegans*. *Nature* 434, 462–469.
- Srayko, M., Buster, D.W., Bazirgan, O.A., McNally, F.J., and Mains, P.E. (2000). MEI-1/MEI-2 katanin-like microtubule severing activity is required for *Caenorhabditis elegans* meiosis. *Genes Dev.* 14, 1072–1084.
- Srayko, M., Kaya, A., Stamford, J., and Hyman, A.A. (2005). Identification and characterization of factors required for microtubule growth and nucleation in the early *C. elegans* embryo. *Dev. Cell* 9, 223–236.
- Stiernagle, T. (2006). Maintenance of *C. elegans*. *WormBook*, 1–11.
- Sulston, J.E., and Horvitz, H.R. (1977). Post-embryonic cell lineages of the nematode, *Caenorhabditis elegans*. *Dev. Biol.* 56, 110–156.
- Sulston, J.E., Schierenberg, E., White, J.G., and Thomson, J.N. (1983). The embryonic cell lineage of the nematode *Caenorhabditis elegans*. *Dev. Biol.* 100, 64–119.
- Tanimoto, H., Kimura, A., and Minc, N. (2016). Shape-motion relationships of centering microtubule asters. *J. Cell Biol.* 212, 777–787.
- Tirnauer, J.S., Canman, J.C., Salmon, E.D., and Mitchison, T.J. (2002). EB1 targets to kinetochores with attached, polymerizing microtubules. *Mol. Biol. Cell* 13, 4308–4316.
- Tournebise, R., Popov, A., Kinoshita, K., Ashford, A.J., Rybina, S., Pozniakovsky, A., Mayer, T.U., Walczak, C.E., Karsenti, E., and Hyman, A.A. (2000). Control of microtubule dynamics by the antagonistic activities of XMAP215 and XKCM1 in *Xenopus* egg extracts. *Nat. Cell Biol.* 2, 13–19.
- Verde, F., Dogterom, M., Stelzer, E., Karsenti, E., and Leibler, S. (1992). Control of microtubule dynamics and length by cyclin A- and cyclin B-dependent kinases in *Xenopus* egg extracts. *J. Cell Biol.* 118, 1097–1108.
- Verde, F., Labbe, J.C., Doree, M., and Karsenti, E. (1990). Regulation of microtubule dynamics by cdc2 protein kinase in cell-free extracts of *Xenopus* eggs. *Nature* 343, 233–238.
- Walczak, C.E., and Heald, R. (2008). Mechanisms of mitotic spindle assembly and function. *Int. Rev. Cytol.* 265, 111–158.
- Walker, R.A., O'Brien, E.T., Pryer, N.K., Soboeiro, M.F., Voter, W.A., Erickson, H.P., and Salmon, E.D. (1988). Dynamic instability of individual microtubules analyzed by video light microscopy: rate constants and transition frequencies. *J. Cell Biol.* 107, 1437–1448.
- Waters, J.C., and Salmon, E. (1997). Pathways of spindle assembly. *Curr. Opin. Cell Biol.* 9, 37–43.
- West, G.B., and Brown, J.H. (2005). The origin of allometric scaling laws in biology from genomes to ecosystems: towards a quantitative unifying theory of biological structure and organization. *J. Exp. Biol.* 208, 1575–1592.
- Wieczorek, M., Chaaban, S., and Brouhard, G.J. (2013). Macromolecular crowding pushes catalyzed microtubule growth to near the theoretical limit. *Cell. Mol. Bioeng.* 6, 383–392.
- Wilbur, J.D., and Heald, R. (2013). Mitotic spindle scaling during *Xenopus* development by kif2a and importin alpha. *Elife* 2, e00290.
- Wuhr, M., Chen, Y., Dumont, S., Groen, A.C., Needleman, D.J., Salic, A., and Mitchison, T.J. (2008). Evidence for an upper limit to mitotic spindle length. *Curr. Biol.* 18, 1256–1261.

STAR★METHODS

KEY RESOURCES TABLE

REAGENT or RESOURCE	SOURCE	IDENTIFIER
Antibodies		
DM1 α anti-tubulin	Sigma-Aldrich	T9026; RRID: AB_477593
Rabbit anti-CLS-2 directed against N-term 14 amino acids of <i>C. elegans</i> CLS-2 (R107.6): MSRVISRSTPGGTC	Home made (purified from rabbit serum)	C2a14
Bacterial and Virus Strains		
OP50 <i>E. coli</i>	Caenorhabditis Genetics Center (CGC)	http://www.cgc.cbs.umn.edu/strain.php?id=11078
HT115(DE3) <i>E. coli</i>	Caenorhabditis Genetics Center (CGC)	http://www.cgc.cbs.umn.edu/strain.php?id=8854
Chemicals, Peptides, and Recombinant Proteins		
ATTO 565 NHS-ester	ATTO-TEC GmbH	AD 565-35
Protamine sulfate	Sigma-Aldrich	P4020
<i>Clasto-Lactacystin β-Lactone (CLβL</i> , proteasome inhibitor)	Merck Millipore	426102
3XmCherry-EMTB	Gift from George von Dassow, University of Oregon	N/A
Experimental Models: Organisms/Strains		
Nematode <i>Caenorhabditis elegans</i> , strain JDU19: [5'mex-5::GFP::tbb-2; mCherry::his-11; cb-unc-119(+)] I; unc-119(ed3) III	Julien Dumont lab, CNRS Institut Jacques Monod, Paris	N/A
Nematode <i>Caenorhabditis elegans</i> , strain JA1559: [pJA138; 5'pie-1::mCherry::tbb-2::3'pie-1]	Julie Ahringer lab	N/A
Nematode <i>Caenorhabditis elegans</i> , strain MDX20: unc-119(ed3). ojs1[unc-119(+) pie-1::GFP::tbb-2]	Maddox lab, University of North Carolina in Chapel Hill	N/A
Nematode <i>Caenorhabditis elegans</i> , strain JDU156: ijmSi7 [pJD348/pSW077; 5'mex-5::GFP::tbb-2; mCherry::his-11; cb-unc-119(+)] I; cyk-1(or596ts) III; unc-119(ed3) III	Julien Dumont lab	N/A
Nematode <i>Caenorhabditis elegans</i> , strain JCC49: cyk-1(or596ts) III; ItIs37[pAA64; pie-1::mCHERRY::his-58; unc-119 (+)] IV	Julie C. Canman lab	N/A
Nematode <i>Caenorhabditis elegans</i> , strain OD58: unc-119(ed3) III; ItIs38[pAA1; pie-1::GFP::PH(PLC1delta1); unc-119 (+)]	Oegema & Desai lab	N/A
Nematode <i>Caenorhabditis elegans</i> , wild-type isolate (Bristol)	Caenorhabditis Genetics Center (CGC)	N2
Sea urchin <i>Paracentrotus lividus</i>	Station Biologiques de Roscoff et Banyuls-sur-mer, France http://www.embrc-france.fr/fr	N/A
Oligonucleotides		
Forward primer for production of dsRNA targeting cls-2 R107.6: TAATACGACTCACTATAGGttcaaggaaaagttggacc (Uppercase: T3 sequence)	(Maton et al., 2015)	N/A
Reverse primer for production of dsRNA targeting cls-2 R107.6: AATTAACCCCTCACTAAAGGggtgcattctgattccacc (Uppercase: T7 sequence)	(Maton et al., 2015)	N/A
Forward primer for production of dsRNA targeting ptr-2 C32E8.8: TAATACGACTCACTATAGGtggtgccgatcatc (Uppercase: T3 sequence)	This study	N/A

(Continued on next page)

Continued

REAGENT or RESOURCE	SOURCE	IDENTIFIER
Reverse primer for production of dsRNA targeting ptr-2 C32E8.8: AATTAACCCTCACTAAAGGgtggccatcaaga gctgat (Uppercase: T7 sequence)	This study	N/A
Forward primer for production of dsRNA against C27D9.1 using L4440 feeding vector in HT115 bacteria: tcagcaaccagcacattctc	https://www.sourcebioscience.com/products/life-science-research/clones/rnai-resources/c-elegans-rnai-collection-ahringer/	SourceBioscience Location II-4A13
Reverse primer for production of dsRNA against C27D9.1 using L4440 feeding vector in HT115 bacteria: aaaatacgcttgacgttggc	https://www.sourcebioscience.com/products/life-science-research/clones/rnai-resources/c-elegans-rnai-collection-ahringer/	SourceBioscience Location II-4A13
Forward primer for production of dsRNA against cls-2 (R107.6) using L4440 feeding vector in HT115 bacteria: aaatcgctctcgaacattgg	https://www.sourcebioscience.com/products/life-science-research/clones/rnai-resources/c-elegans-rnai-collection-ahringer/	SourceBioscience Location III-4J10
Reverse primer for production of dsRNA against cls-2 (R107.6) using L4440 feeding vector in HT115 bacteria: tgatgggtttgacaaacga	https://www.sourcebioscience.com/products/life-science-research/clones/rnai-resources/c-elegans-rnai-collection-ahringer/	SourceBioscience Location III-4J10
Software and Algorithms		
ImageJ	NIH	https://imagej.nih.gov/ij/index.html
MATLAB	MathWorks	https://www.mathworks.com/products/matlab.html
GraphPad PRISM 6.0	GraphPad	https://www.graphpad.com/
Imaris	Bitplane	http://www.bitplane.com/imaris/imaris
Cytosim	Nédélec Laboratory	http://github.com/nedelec/cytosim

CONTACT FOR REAGENT AND RESOURCE SHARING

Further information and requests for resources and reagents should be directed to and will be fulfilled by the Lead Contact, Julien Dumont (julien.dumont@ijm.fr). Requests related to the simulations should also be addressed to Francois Nedelec (nedelec@embl.de).

EXPERIMENTAL MODEL AND SUBJECT DETAILS***Caenorhabditis elegans***

C. elegans are small, transparent hermaphroditic soil worms with rapid, invariant and fully characterized development (Sulston and Horvitz, 1977; Sulston et al., 1983). Spindle assembly has been extensively studied in *C. elegans* (Muller-Reichert et al., 2010), primarily because many key proteins and mechanisms are highly conserved with other metazoans. All *C. elegans* strains were maintained at 23°C or at 16°C for the *cyk-1(ts)* mutant strain (JCC49 and JDU156) and cultured using standard procedures (Brenner, 1974). Briefly, *C. elegans* worms were grown monoxenically on NGM plates seeded with the OP50 *E. coli* strain. Worm strains were propagated and maintained by transferring three L4 larvae on fresh seeded NGM plates every 3 to 6 days. Different strains were obtained either by stable single insertion by MosSCI (Frokjaer-Jensen et al., 2008) or by crossing with pre-existing strains. *C. elegans* worm strains and genotypes are listed in the Key Resources Table. Adult hermaphrodites were dissected for embryo collection and analysis.

Paracentrotus lividus

Paracentrotus lividus sea urchins were purchased from the Roscoff Marine Station (Station Biologique de Roscoff, CNRS-UPMC, France) or from the EMBRC-France (European Marine Biological Resource Center, Banyuls-sur-mer, France). Adult individuals were maintained in large Plexiglas tanks filled with artificial seawater at 16°C under constant oxygenation and recurrent filtering, siphoning and volume exchange. Sea urchins were exposed to photoperiods of 12h light and 12h darkness. Water constants: temperature (16°C), density (1.025 g/L), pH (8 to 8.3) and carbonate hardness (7-10 dKH) were controlled on a daily basis. Others constant such as phosphates and nitrogen were controlled on a weekly basis and maintained within range compatible with sea urchin physiology ($\text{PO}_4 < 0.05 \text{ mg/L}$; $\text{NH}_4 < 0.1 \text{ mg/L}$; $\text{NO}_3 \leq 1 \text{ mg/L}$; $\text{NO}_2 < 0.025 \text{ mg/L}$). Sea urchins were fed with a mix of frozen algae in agar. Adult males and females were induced to spawn. *P. lividus* have no sexual dimorphism and sex could only be determined during

spawning based on the color of the laid gametes (eggs are pink to red, sperm are white). Sex of imaged embryos was therefore not determined.

METHOD DETAILS

RNA-mediated Interference (RNAi) and Drug Treatment in *C. elegans*

Depletion of C27D9.1 and of CLS-2 (R107.6) in Figure 8 were done by feeding as described by Kamath et al., (Kamath et al., 2001). For L1 larvae synchronization, adult worms were bleach-treated (1.2% NaOCl, 250 mM KOH in water; (Stiernagle, 2006) to release embryos. Embryos were allowed to hatch and left to starve in M9 buffer (22 mM KH_2PO_4 , 42 mM Na_2HPO_4 , 86 mM NaCl). Synchronized L1 hermaphrodite larvae were grown on regular NGM plates seeded with the OP50 bacterial strain for 44 hours (until they reached the adult stage), and then adult worms were transferred on RNAi feeding plates for at least 24 hours for C27D9.1 and for an increasing time (from 6 to 24h) for CLS-2 respectively. RNAi feeding was performed on NGM plates containing 50 $\mu\text{g}/\text{ml}$ ampicillin (Euromedex) and 1 mM IPTG (Isopropyl β -D-thiogalactopyranoside, Euromedex) and seeded with the HT115(DE3) bacterial strain transformed with the empty L4440 vector (control) or containing the C27D9.1 target sequence (corresponding to nt179-1366 of the genomic sequence). Depletion of CLS-2 in Figure 3 was performed by microinjection of the corresponding dsRNA in L4 hermaphrodite larvae as previously described (Fire et al., 1998). The dsRNA targeting *cls-2* was synthesized from a purified PCR product (corresponding to nt164-1081 of the genomic sequence, QIAquick PCR purification, Qiagen) that contained the T3 and T7 phage RNA polymerase promoter sequences (T3: taatacgtactcactatagg ; T7 : aattaaccctcactaaagg) in 5' and 3', respectively, using the MEGAscript T3 and T7 transcription kits (ThermoFischer Scientific). Single stranded RNAs were purified using the MEGAClear Transcription Clean-Up kit (ThermoFischer Scientific). Sense and antisense single stranded RNAs were mixed in equimolar concentrations and annealed at 68°C for 10 min followed by 37°C for 30 min. DsRNAs were aliquoted, snap-frozen in liquid nitrogen and stored at -80°C until use. The dsRNA targeting *cls-2* was injected in L4 hermaphrodites at a concentration of 1.8 $\mu\text{g}/\mu\text{l}$. Partial depletion of CLS-2 as obtained 25 to 27 h post-injection at 23°C (Maton et al., 2015). PTR-2 (C32E8.8) depletion was performed in a humid chamber by soaking 25 to 30 L4 hermaphrodite larvae in a 5 μl drop of the corresponding dsRNAs (synthesized as previously and corresponding to nt1886-2904 of the genomic sequence) supplemented with 2.86 mM spermidine (Sigma) and 0.05 % gelatin (Sigma). L4 larvae were soaked at 20°C for 24 hours, then washed twice in M9 medium and transferred on NGM plates for another 24 hours at 20°C before observation. PTR-2-depleted embryos are defective in eggshell formation and are therefore permeable and amenable to drug treatments. To induce a metaphase arrest in zygotes, PTR-2-depleted adult worms were dissected in 20 μM clasto-lactacystine β -lactone (CL β L, Merck Millipore) in L-15 blastomere culture medium [0.5 mg/mL Inulin (Sigma); 25 mM HEPES pH 7.5; 3 mL Leibowitz L-15 Media and 20% (vol/vol) Heat-Inactivated FBS (Life Technologies)] with 1% DMSO (Euromedex) final concentration.

Estimation of the Tubulin Heterodimer Concentration in the *C. elegans* Embryo by Quantitative Western Blot

C. elegans early embryos (1- to ~64-cell stage) were extracted from synchronized adult N2 worms by bleaching as described earlier in the “RNA-mediated interference (RNAi) and drug treatment in *C. elegans*” method section. Embryos were then resuspended in M9 buffer. The number of embryos per volume and their approximate number of blastomeres (stage) were estimated under a dissection scope (Nikon). Embryos were then lysed into 1x Laemmli sample buffer (80 mM Tris-HCl pH 6.8, 140 mM 2-Mercaptoethanol, 2.5% SDS, 10% glycerol) by vortexing in presence of 0.7 mm diameter Zirconia beads (BioSpec Products) 3 times 5 min at 4°C with pauses of 5 min. Lysis efficiency was assessed using a dissection scope. Samples were then incubated 5 min at 95°C before loading on a SDS-PAGE gel. The equivalent of ~1120 or ~2240 embryos were loaded on a SDS-PAGE gel (10%, 37.5:1 acrylamide:bisacrylamide) together with increasing amounts of porcine brain tubulin purified as described in “Tubulin preparation and fluorescent labeling” (Figure S5). *C. elegans* and porcine brain tubulin samples were treated similarly. Proteins were transferred onto a nitrocellulose blotting membrane Protran 0.45 μm (Amersham, GE Healthcare) by liquid transfer. Membrane was incubated with DM1 α antibody (Sigma) diluted 1/1000 in 5% fat-free milk in Tris-buffered saline (TBS: 50 mM Tris pH 7.5, 150 mM NaCl). Protein bands were revealed with an HRP-labeled goat anti-mouse IgG 1:10,000 (GE Healthcare) and chemoluminescence (ECL SuperSignal West Pico, Thermo-Scientific). Detection was performed on a luminescence image analyzer LAS-4000 (Fujifilm). Band intensities were analyzed using ImageJ. The amount of α -tubulin contained per embryo was estimated to be between 2.04 and 2.73×10^{-11} g. This amount corresponds to a concentration of 0.93 to 1.24 g/L (Embryo volume = 2.2×10^{-11} L, Figure S1 and Table S1) or 18.6 and 24.8 μM (molecular weight of α -tubulin = 50,000 g/mol). *C. elegans* microtubules are composed of 11 protofilaments on average (Chalfie and Thomson, 1982), and tubulin heterodimers are 8 nm long (Nogales et al., 1998). If we assume an average tubulin heterodimer concentration of 22 μM , a *C. elegans* embryo contains enough tubulin heterodimers to build 21.2 cm of microtubules in total. The metaphase spindle in the 1-celled zygote is composed of around ~20,000 microtubules, which are on average 4 μm long (Redemann et al., 2017). This average microtubule length also corresponds to the theoretical average microtubule length $\langle L \rangle$ calculated from the dynamics parameters in the 1-celled zygote (Table S1). Therefore, in the 1-celled zygote in metaphase, spindle microtubules reach a total length of about 8 cm ($20,000 \times 4 \mu\text{m}$). We thus concluded that the *C. elegans* zygote contains enough tubulin heterodimers to build between 2 and 3 mitotic spindles.

Estimation of CLS-2 Protein Level Following RNAi-mediated Depletion in the *C. elegans* Embryo by Quantitative Western Blot

Control or RNAi treated gravid *C. elegans* were collected and washed into M9 buffer containing 0.1% Triton X-100. Worms (100 worms per 100 μ l) were then lysed into 1x Laemmli sample buffer (80 mM Tris-HCl pH 6.8, 140 mM 2-Mercaptoethanol, 2.5% SDS, 10% glycerol) by vortexing in presence of 0.7 mm diameter Zirconia beads (BioSpec Products) 3X5 min at 4°C with pauses of 5 min. Lysis efficiency was assessed using a dissection scope. Samples were then incubated 5 min at 95°C before loading on a SDS-PAGE gel. The equivalent of 10 worms were loaded on a SDS-PAGE gel (8%, 37.5:1 acrylamide:bisacrylamide). Proteins were transferred onto a nitrocellulose blotting membrane Protran 0.45 μ m (Amersham, GE Healthcare) by liquid transfer. The membrane was incubated with a rabbit polyclonal custom-made anti-CLS-2 antibody (C2a14) diluted at 1 μ g/ml and then with a DM1 α antibody (Sigma) diluted 1/1000 in 5% fat-free milk in Tris-buffered saline (TBS: 50 mM Tris pH 7.5, 150 mM NaCl). Protein bands were revealed with an HRP-labeled goat anti-rabbit (CLS-2) or anti-mouse (DM1 α) IgG 1:10,000 (GE Healthcare) and chemoluminescence (ECL Prime, Amersham). Detection was performed on a luminescence image analyzer LAS-4000 (Fujifilm). Band intensities were analyzed using ImageJ.

Tubulin Preparation and Fluorescent Labeling

Tubulin was obtained from pig brains following cycles of polymerization and depolymerization (Castoldi and Popov, 2003). Tubulin was then labeled with NHS-ester-ATTO 565 (ATTO-TEC) and further purified through two polymerization/depolymerization cycles (Hyman, 1991). Briefly, unlabeled polymerized tubulin was incubated 40 min at 37°C in the presence of 5 mM of succinimidyl ester-coupled fluorophore in labeling buffer (0.1 M HEPES pH 8.6, 1 mM MgCl₂, 1 mM EGTA and 40% glycerol (volume/volume)). Microtubules were then spun down through a low pH cushion (60% glycerol BRB: 80 mM PIPES pH 6.8, 1 mM MgCl₂, 1 mM EGTA) and resuspended and depolymerized in 50 mM K-glutamate pH 7.0, 0.5 mM MgCl₂. Depolymerized labeled tubulin was recovered through 120,000xg centrifugation at 2°C and suspended in 4 mM MgCl₂, 1 mM GTP and 1X BRB from a 5X BRB stock. Tubulin was then allowed to repolymerized at 37°C for 40 min. Microtubules were pelleted at 120,000xg for 20 min at 37°C and depolymerized in ice-cold BRB buffer. The depolymerized tubulin was recovered from a 10 min centrifugation at 2°C and at 150,000xg diluted to 15-20 mg/ml in 1X BRB, aliquoted, frozen in liquid nitrogen and stored at -80°C.

Two-photon Live Microscopy of *C. elegans* Embryos

Embryo and blastomere volume measurements were made from Z-stacks of 1- to 16-cell stage embryos expressing a GFP-tagged membrane marker (OD58 strain that expresses the GFP-PH-domain under a *pie-1* germline promoter). Embryos were released from gravid adult hermaphrodites in a 5 μ l drop of egg salt buffer (ESB, 25 mM HEPES pH 7.3, 118 mM NaCl, 48 mM KCl, 2 mM CaCl₂, 2 mM MgCl₂) by cutting each worm open using a scalpel (blade N°15). Embryos were then transferred between two 3% agarose pads to prevent compression and to minimize refractive index mismatch. The montage was then placed on a glass slide, sealed with paraffin. A well of Valap (petroleum jelly:lanolin:paraffin, 1:1:1) was made around it and filled with water for imaging in immersive conditions. An upright two-photon microscope with a Zeiss Plan APO 20x/NA1.0 water objective was used (Lavisision Biotec). GFP was excited with a pulsed laser at 920 nm. Emission at 535 nm was collected with a GaAsP detector (Lavisision Biotec). The entire embryo was imaged with 1 μ m Z-sectioning and 190 nm lateral sampling.

Spinning-disc Live Microscopy of *C. elegans* Embryos

Gravid worms were dissected as described in the previous paragraph in egg salt buffer (ESB, see above). Embryos were transferred on a 3% agarose pad between a glass slide and a coverslip. The montage was then sealed with Valap. Live imaging was done using a spinning-disk (CSU-X1, Yokogawa) confocal microscope (Roper Scientific) coupled to a CoolSnap HQ2 CCD camera (Photometrics) and all acquisition parameters were controlled by MetaMorph 7 software (Molecular Devices). For microtubule dynamics parameter extraction, images were acquired on a single channel (491 nm excitation) every 0.5 sec with a single z-plan using a Nikon CFI APO LBDA S 60x/NA1.4 oil objective with no binning. To measure spindle assembly timings, images were acquired on two channels sequentially (491 and 561 nm excitations) every 5 sec with 11 z-plan at 1 μ m intervals using a Nikon CFI APO LBDA S 40x/NA1.25 water objective with no binning. Maximal projections are presented.

Injection and Imaging of Sea Urchin Embryos

Gametes were collected by intracoelomic injection of 0.5M KCl. Eggs were washed several times in fresh seawater, kept at 12-14°C and used within 24h. Sperm were kept concentrated for several days at 4°C. Upon use, the sperm suspension was diluted 1000 times in fresh seawater and activated by vigorous aeration. Freshly collected *P. lividus* eggs were dejellied by pouring through a 80 μ m pore Nitex mesh (Sefar). Dejellied eggs were immobilized on a protamine (Sigma) treated 60 mm diameter glass-bottom dish for both microinjection and imaging. Eggs were fertilized 20 min after ATTO 565-tubulin microinjection (2 mg/ml) by adding a few drops of activated sperm. Live imaging was done using a spinning disk (CSU-W1, Yokogawa) confocal microscope (Leica Microsystems) coupled to an ORCA-Flash4.0 V2 CMOS camera (Hamamatsu). Embryos were maintained and imaged between 18°C and 20°C during and in between acquisitions. All acquisition parameters were controlled by MetaMorph 7 software (Molecular Devices). Images were acquired on a single channel (561 nm excitation) every 1 sec with a single z-plan using a Leica Plan APO 63x/NA1.2 water objective.

Immunostaining of Sea Urchin Embryos

Freshly collected eggs were fertilized in a 140 mm diameter glass container and allowed to develop at 18°C (same as for live imaging). Embryo cleavage and NEBD were monitored by transmitted light on a dissection scope. At NEBD, embryos were fixed following previously described procedures (Foe and von Dassow, 2008; Tanimoto et al., 2016). Fixation was performed in bulk in 15 ml polypropylene conical tubes. Embryos were first fixed for 70 min in 100 mM Hepes, pH 6.9, 50 mM EGTA, 10 mM MgSO₄, 2% formaldehyde, 0.2% glutaraldehyde, 0.2% Triton X-100, and 400 mM dextrose. They were then rinsed three times for 10 min in PBS and placed in freshly made 0.1% NaBH₄ in PBS for 45 min. Embryos were rinsed again with PBS and PBS 0.1% Triton X-100 (PBT). For microtubule immunostaining, embryos were incubated overnight at 4°C with a primary anti- α -tubulin antibody (DM1 α , Sigma-Aldrich) at a 1:5000 dilution, and washed 3 times for 30 min in PBT. Embryos were then incubated overnight in secondary antibody (goat anti-mouse DyLight 550, Jackson ImmunoResearch) at a 1:1000 dilution in PBT. Chromatin was stained using DAPI at a 1:5000 dilution in PBS. Embryos were then mounted in 0.5% n-propyl gallate in a 9:1 solution of glycerol/1M TRIS pH 8.0.

Image Analysis

Two-photon acquisitions of GFP-PH (membrane marker) during *C. elegans* embryonic development were analyzed using Imaris software (Bitplane). *C. elegans* blastomere volumes were extracted after semi-automated surface reconstruction. *P. lividus* blastomere volumes were estimated from experimentally measured blastomere diameters. Spinning-disk confocal images were analyzed using the Fiji package (<http://fiji.sc/>; <https://imagej.nih.gov/ij/>). Spindle length was estimated as the aster-to-aster distance (Crowder et al., 2015) on GFP-tubulin images. Metaphase plate thickness and centrosome radius were measured on segmented mCherry-histone and GFP- β -tubulin images in *C. elegans* embryos or ATTO 565-tubulin images in *P. lividus* embryos. At each cleavage stage in *C. elegans* embryos, a 10% or 40% grey level threshold were applied on mCherry-histone or GFP- β -tubulin images respectively. In *P. lividus* embryos, a 30% grey level threshold was applied on ATTO 565-tubulin images for centrosome radius measurements. These thresholds were selected to obtain the sharpest limit between the metaphase plate histone signal or the centrosome and the cytoplasmic background with minimal erosion of the signal. Measured values were used in Cytosim simulations to build *in silico* spindle 3D models.

Analysis of Microtubule Dynamics

Individual embryos were imaged at a single stage of cleavage and for less than 10 min to avoid phototoxicity-induced bias (Lacroix and Maddox, 2014; Lacroix et al., 2016). Kymographs were traced from time-lapse sequences using the 'Multi kymograph' plugin (http://imagej.net/Multi_Kymograph) in Fiji. Polymerization and depolymerization rates, as well as catastrophe and rescue frequencies, were extracted from these kymographs by manual tracking and semi-automated parameter extraction using homemade macros in Fiji and Excel (Microsoft) software. Catastrophe and rescue frequencies were defined as the inverse of the average growth time or shrinkage time, respectively (Desai and Mitchison, 1997; Komarova et al., 2002; Walker et al., 1988). Although this method could potentially overestimate catastrophe and rescue occurrences (which would be identical in all tested experimental conditions), it allows estimating both parameters independent of microtubule pausing, moving out-of-focus during live imaging or entering in the fluorescence-saturated centrosome area.

Cytosim Simulations

All simulations were performed in 3D using Cytosim (www.cytosim.org; Nedelec and Foethke, 2007). Cytosim simulations have already been used to show how polymerization forces and thus microtubules dynamics could affect centrosome positioning (Letort et al., 2016). Following this approach, we aimed for a minimal model in which spindle length, corresponding to the distance between two asters, would be influenced by microtubules dynamic behavior. A detailed list of Cytosim parameters for each object in the simulations is presented in Table S3. Spindle poles were modeled using microtubules radiating radially from a sphere (asters). The surface of the sphere contains a preset number of nucleation sites, at which microtubules are anchored at their minus-ends constraining their position and orientation. The minus-ends are static, while the plus-ends may grow or shrink, stochastically switching between these states following the usual phenomenological model of dynamic instability. The metaphase plate was represented as a fixed and rigid disc positioned orthogonally at the center of the "cell". Although microtubules were excluded from inside this plate, microtubule-associated molecules (called "singles", each made of one "hand") anchored on this disc and capable of tracking growing microtubule ends were used to mimic the chromokinesins present on chromosomes, as well as the capture of microtubules by pro-metaphase kinetochores. The primary function of these microtubule-associated molecules is to prevent microtubules from sliding on the surface of the "metaphase plate". At the start of every simulation, the two asters were positioned symmetrically 2 μ m away from the "metaphase plate" on each side.

The input growth rate (v_0) varied within the range of experimental measurements made in *C. elegans* embryos from 1- to 16-cell stage. The effective microtubule growth rate was set to decrease exponentially under an opposing force as $v_g = v_0 e^{-\frac{F}{F_s}}$, where v_0 is the input growth rate and F_s is the force at which microtubule polymerization stalls (Dogterom and Yurke, 1997). Consequently, microtubules encountering the metaphase plate grew dramatically slower, in agreement with *in vivo* measurements at the

kinetochore (Maddox et al., 2003; Tirnauer et al., 2002). Further, in the first simulation that contained both astral and spindle microtubules, a force-dependent increase in the catastrophe rate $k_{cat} = \frac{k_{cat}^{stall}}{1 + (k_{cat}^{stall}/k_{cat}^0 - 1)v_g/v_0}$ (see also Table S3) induced microtubule shrinking soon after cortical or metaphase plate contact. This force-dependent microtubule shrinking was not implemented in the second simulation (with only spindle microtubules). So, the effective average growth rate of microtubules in our simulations represented the mean rate of free growing microtubules and stalled microtubules at the metaphase plate (or at the cortex) (Figure S4A).

Two different spindle models were tested, as described below. (Figures 5A–5C): This model included 500 microtubules per aster. 400 microtubules were allowed to grow uniformly in space, and 100 microtubules per aster were constrained in a cone directed toward the metaphase plate to mimic the higher microtubule density observed *in vivo* in the spindles of *C. elegans* embryos. *C. elegans* blastomeres were represented by 3D ellipsoids. Cell volume, metaphase plate thickness and radius were scaled together with respect to the input microtubule growth rate using realistic values extrapolated from our experimental measurements (Table S2B). Scaling to the input growth rate was done assuming a linear proportionality between microtubule growth rate and other dimensions. Due to their initial proximity to the metaphase plate, spindle microtubules were more likely to be stalled and therefore displayed a lower effective average growth rate than astral microtubules (Figure S4B). This was particularly true for higher initial rates and was reminiscent of the difference in the growth rates we measured *in vivo* between astral and spindle microtubules. This mild difference in the astral and spindle effective growth rates was sufficient to induce a significant deviation of the average microtubule length reached by the two populations (Figure S4C). The average length difference was not evident at low initial growth rates but was particularly clear for rates above 0.3 $\mu\text{m}/\text{sec}$. This result is in agreement with the evolution of $\langle L \rangle$ for astral and spindle microtubules calculated from *in vivo* measured parameters, which became closer between the two types of microtubules as cells get smaller (Table S1). The faster decrease of the average length of astral compared to spindle microtubules is likely due to increasing cortical surface to cell volume ratio as cleavage progresses. Indeed, the cortical surface decreases slower than the cell volume, so that astral microtubules are more likely to encounter the cortex and shrink, as blastomeres get smaller. Our simulation therefore accurately recapitulates two key features of the dynamic behavior of astral and spindle microtubules *in vivo* during embryonic cleavage: 1) spindle microtubules grow slower and are, on average, shorter than astral microtubules during early cleavages and 2) these differences tend to fade as blastomeres become smaller (Figures S4B and S4C).

(Figures 5D–5F): 50 microtubules were constrained in a spindle-shaped cone to reflect the *C. elegans* embryo spindle geometry (Table S2). Importantly, increasing or decreasing the number of microtubules had no effect on the final outcome of the simulations (data not shown). The two asters do not include astral microtubules and grow in an infinite space without a cell boundary.

QUANTIFICATION AND STATISTICAL ANALYSIS

All graphs were made in Prism 6 (GraphPad Software). Statistical analyses, including Student t-tests, one-way ANOVA multiple comparisons, linear regressions and Pearson and Spearman correlation tests were performed in Prism 6 (GraphPad software). Microtubule dynamics parameters have different variances, so we used the unequal variance unpaired t-test with the Welch's correction for normally distributed populations with unequal standard deviation. Tukey or Dunnett tests were performed for multiple comparisons following one-way ANOVA. In Figure 4B, multiplicity adjusted *p* value was estimated for the multiple comparison Tukey's test.

DATA AND SOFTWARE AVAILABILITY

Data Availability

All data presented in this manuscript are available upon request to the lead author (julien.dumont@ijm.fr).